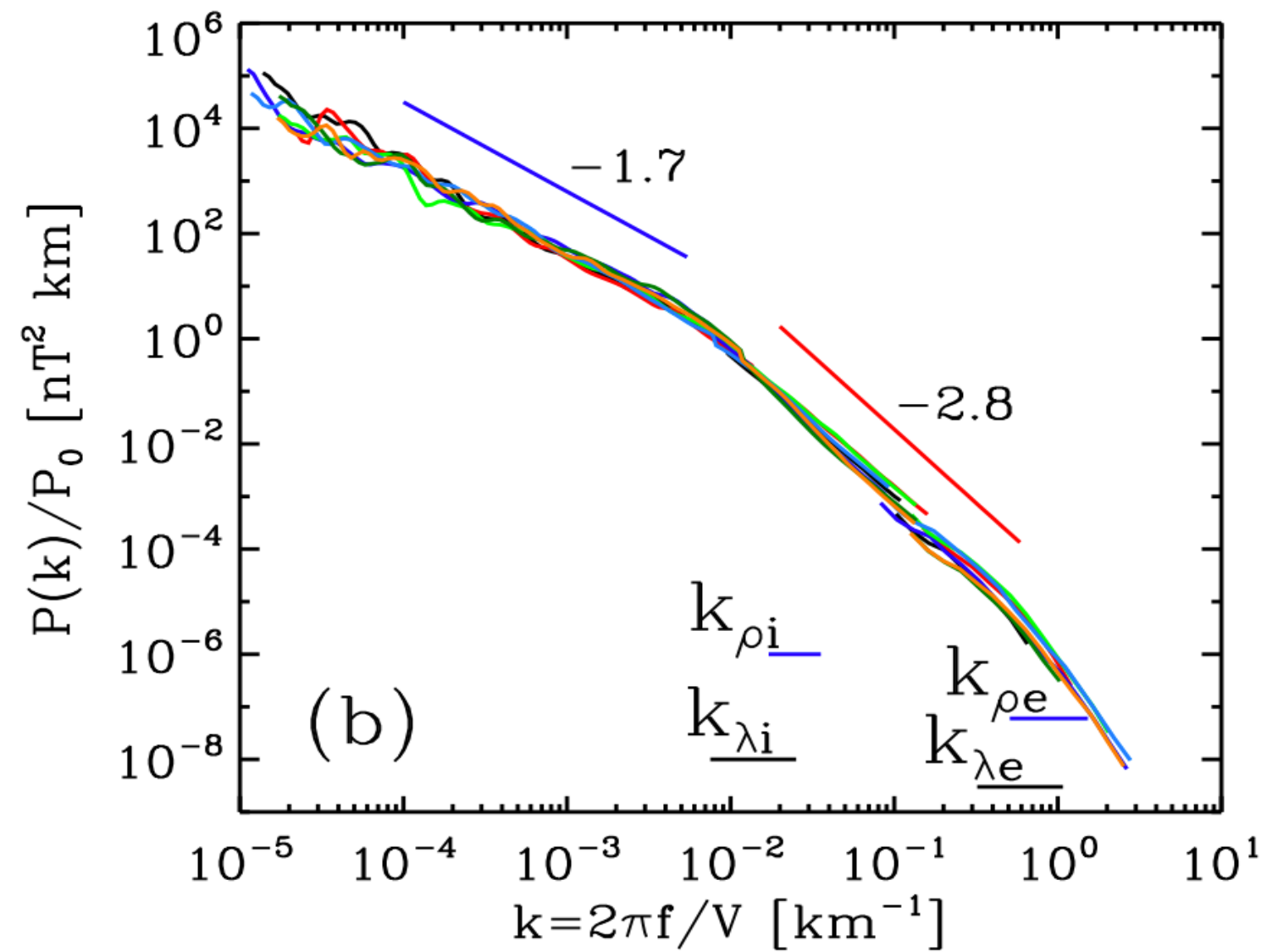


Intermittency and electron heating in kinetic-Alfvén-wave turbulence

Muni Zhou¹, Zhuo Liu¹, Nuno F. Loureiro¹

¹Massachusetts Institute of Technology

Plasma turbulence in the sub-ion-Larmor-radius range



Solar wind magnetic spectrum from
Cluster [Alexandrova+ 2019]

Main questions:

What are the *spectra* of fluctuations?

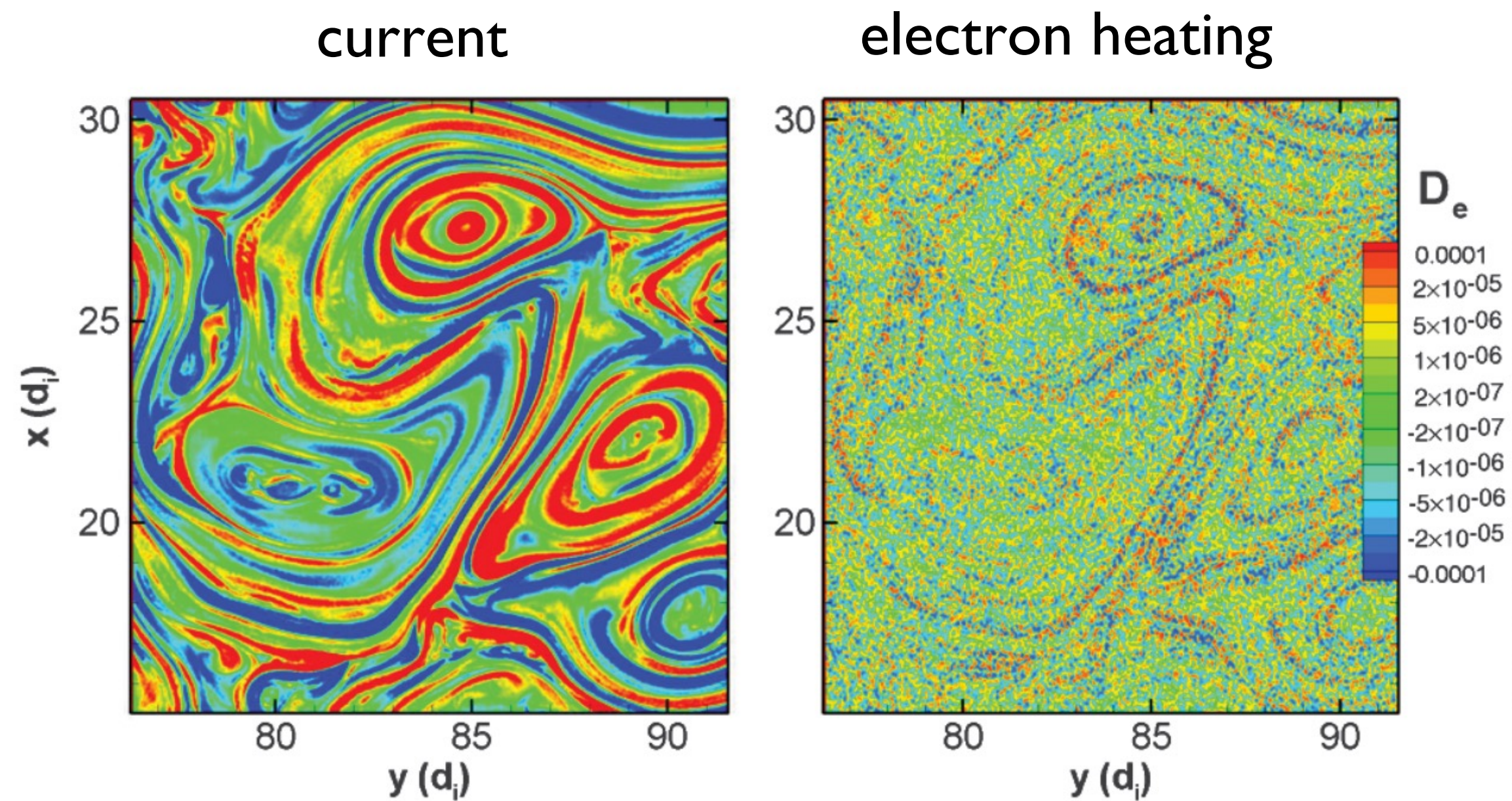
What is the mechanism causing the -2.8 magnetic spectrum measured in the solar wind?

What is the nature of the *dissipative processes*?

How are ions and electrons heated?

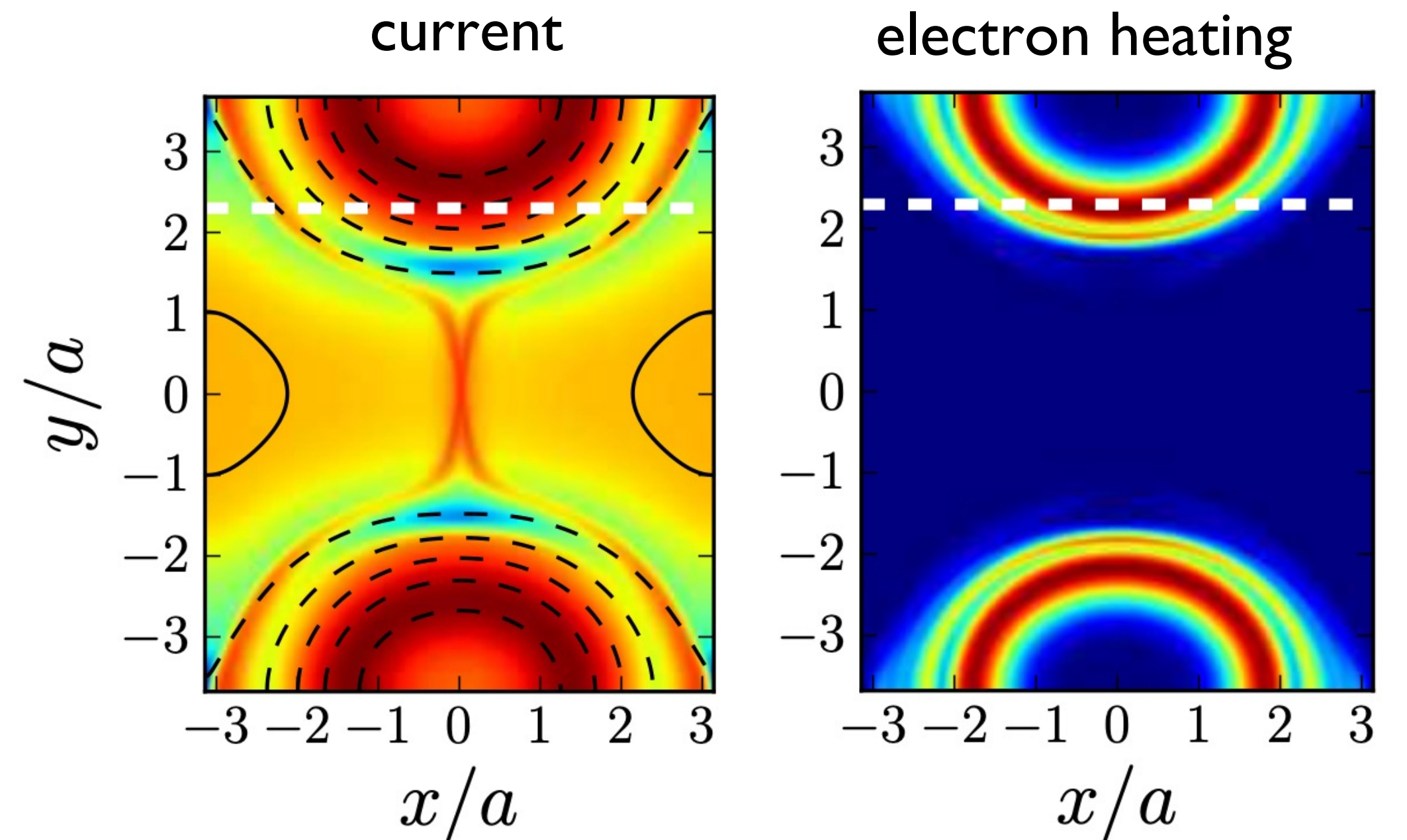
Electron heating

Efficient electron heating is observed in kinetic turbulence simulations around current sheets.



[Wan+ 2012, 2015]

Magnetic reconnection yields efficient electron heating



[Loureiro+ 2013]

Some long-standing discussion: relation between current sheets, reconnection, and heating

What can be the role of reconnection in kinetic turbulence? setting the spectra? facilitating heating?

Spectra and spectral anisotropy

Total magnetic fields $\mathbf{B} = B_0 \hat{\mathbf{z}} + \delta \bar{\mathbf{B}}_{\perp}$, correlation lengths of fluctuations: length $\ell \sim 1/k_{\parallel}$, thickness $\lambda \sim 1/k_{\perp}$, and width ξ

General arguments:

At scales $k_{\perp} \rho_i \gg 1$, equipartition b/w magnetic and density fluctuations gives $\varphi_{\lambda} \sim (\rho_i V_A / c) \delta B_{\perp \lambda}$

Linear time scale is set by propagation of KAWs $\gamma_l \sim \omega_{\text{KAW}} \propto k_{\perp} \rho_s k_{\parallel} V_A \sim \rho_s V_A / (\ell \lambda)$

Dimensionally, the nonlinear eddy-turnover rate is $\gamma_{nl} \sim \varepsilon / (\rho_0 v_{A\lambda}^2 / 2) \sim \varepsilon / (\delta B_{\perp \lambda}^2 / 8\pi)$

Critical balance: $\gamma_l \sim \gamma_{nl}$

Kolmogorov-type cascade of KAW

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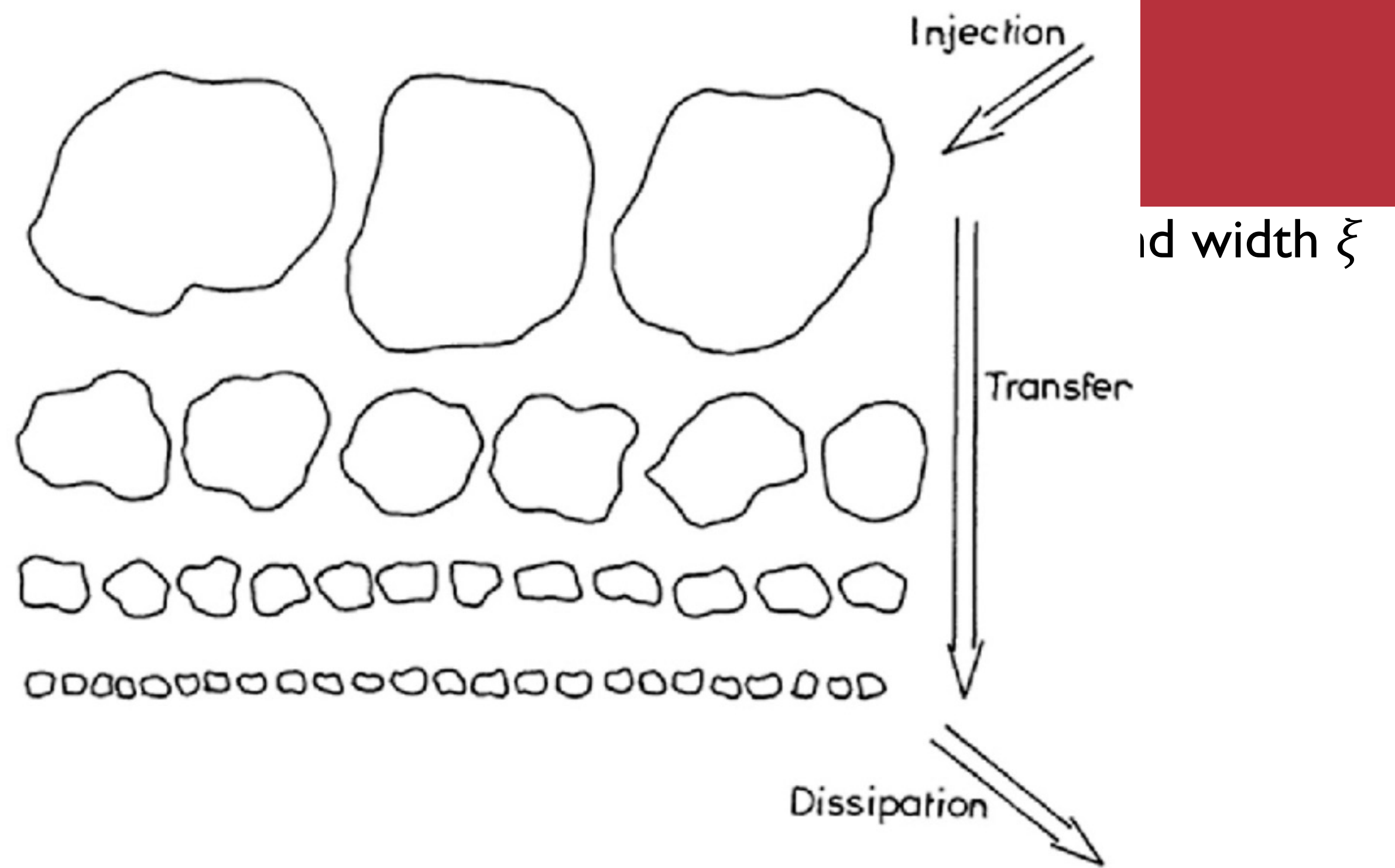
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Critical balance: $\gamma_l \sim \gamma_{nl}$

Specify the nonlinear physics!

IF $\gamma_{nl} \sim u_\lambda / \lambda$, where $u_\lambda \sim (c/B_0) \varphi_\lambda / \lambda$



- Kolmogorov-type cascade of KAWs --- $k_\perp^{-7/3}$
[Cho&Lazarian 2004; Howes+ 2008; Schekochihin+ 2009]

Intermittency

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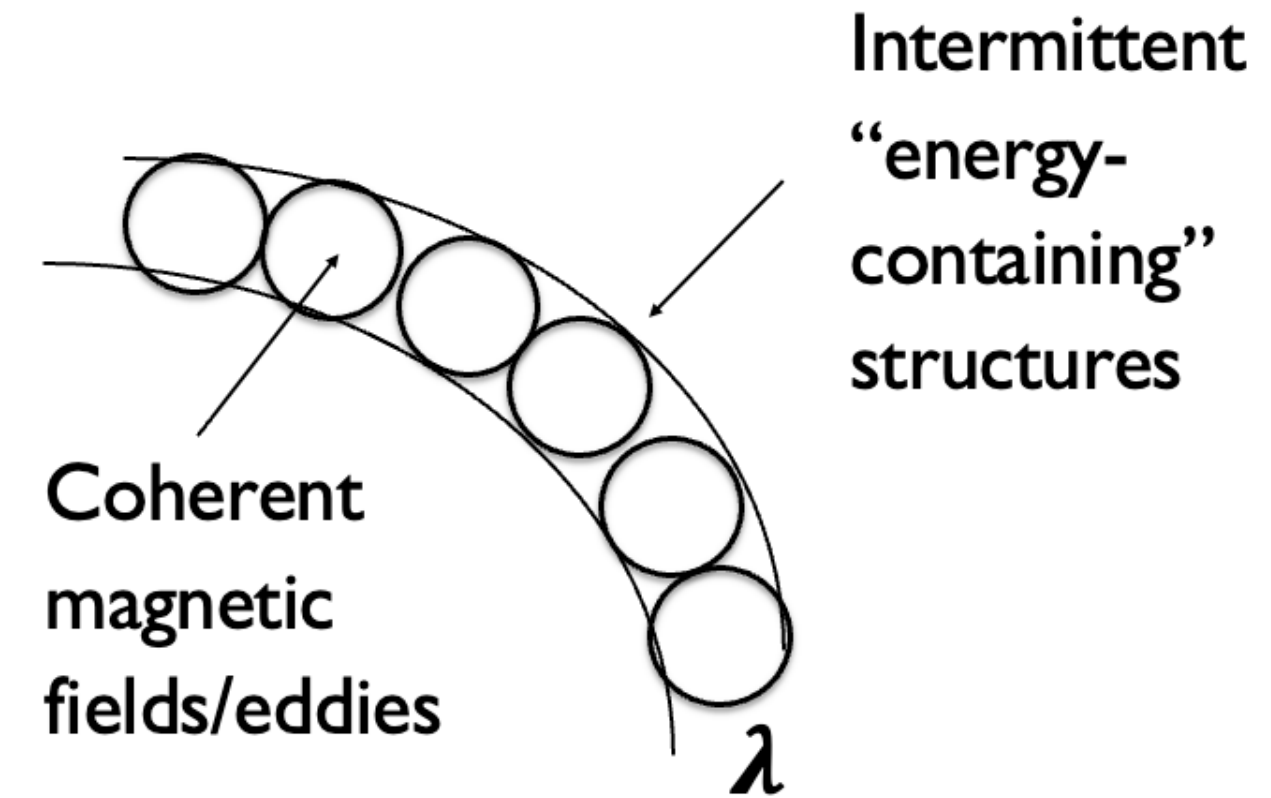
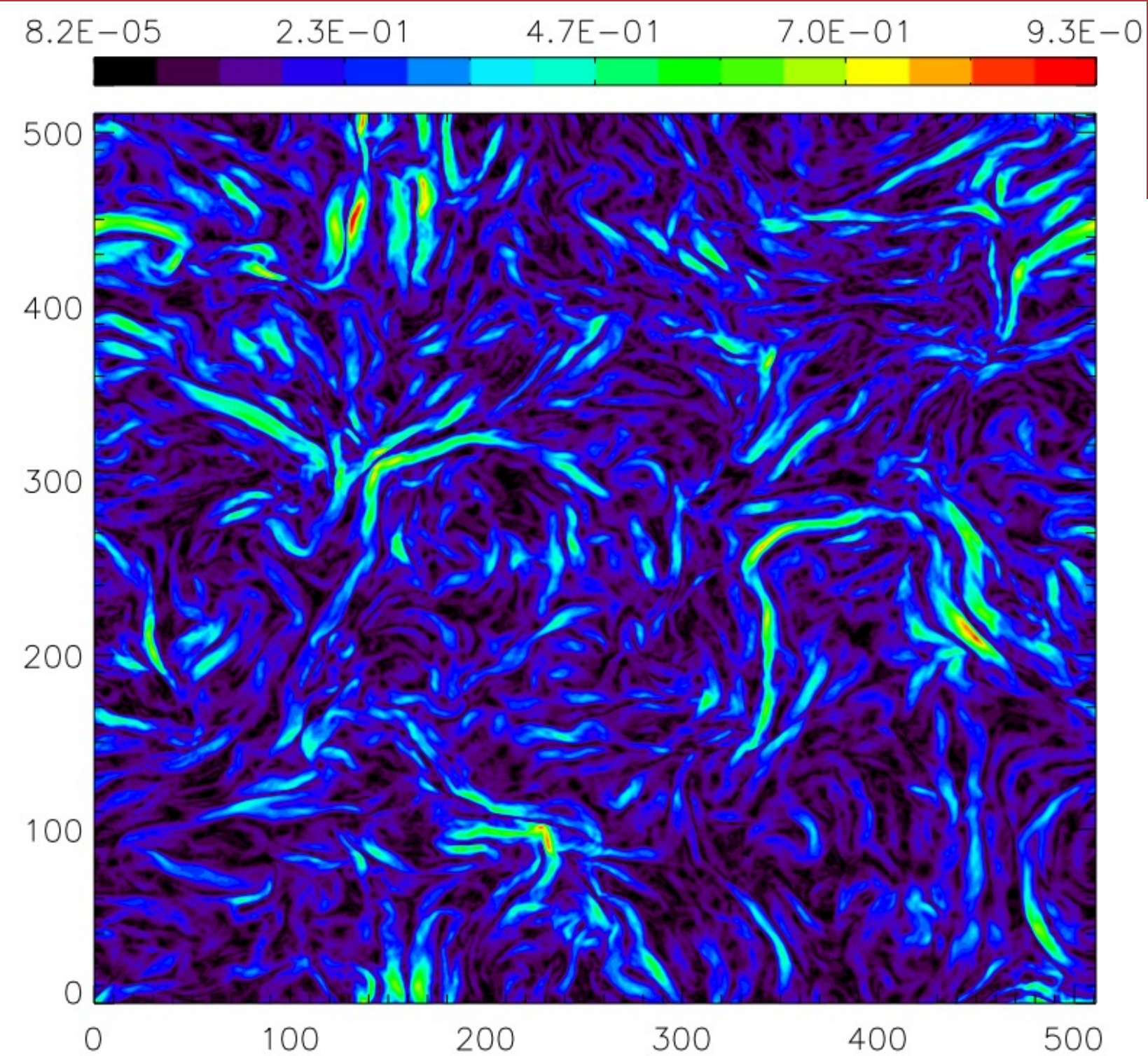
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IF $\gamma_{nl} \sim u_\lambda / \lambda$, where $u_\lambda \sim (c/B_0) \varphi_\lambda / \lambda$

IF $\gamma_{nl} \sim u_\lambda / \lambda$ $\gamma_{nl} \sim \varepsilon / (\delta B_{\perp \lambda}^2 p_\lambda)$

Volume-filling factor $p_\lambda \propto \lambda$.

2D “energy containing” sheets



- Kolmogorov-type cascade of KAWs --- $k_\perp^{-7/3}$
[Cho&Lazarian 2004; Howes+ 2008; Schekochihin+ 2009]
- Intermittency --- $k_\perp^{-8/3}$ and $k_\parallel^{-7/2}$
[Boldyrev&Perez 2012]

Tearing mediation

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Critical balance: $\gamma_l \sim \gamma_{nl}$

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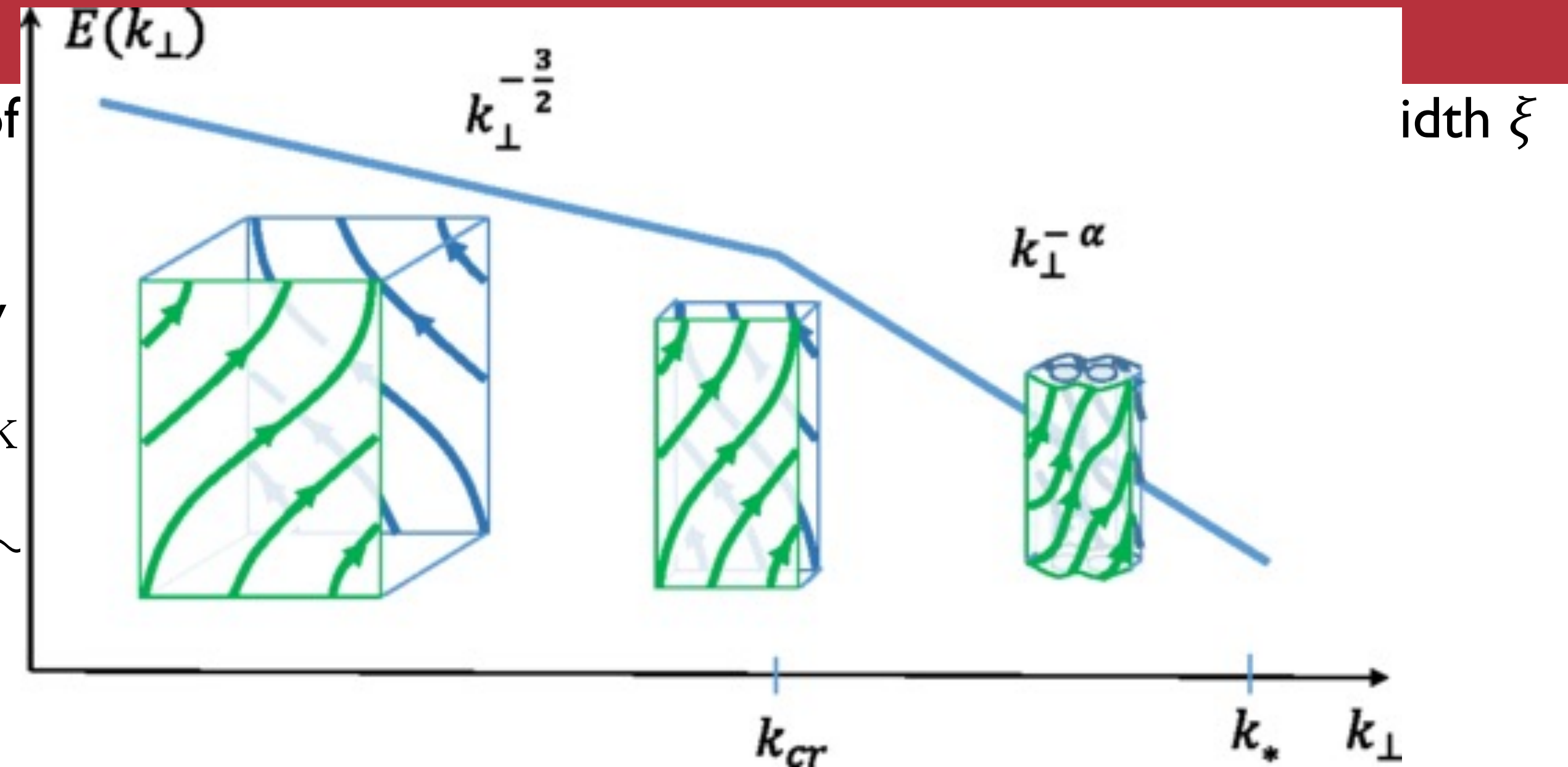
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IF $\gamma_{nl} \sim \gamma_t \sim v_{A\lambda} \rho_i d_e^{1/2} \lambda^{-5/2}$



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Isothermal limit --- Spectra and spectral anisotropy

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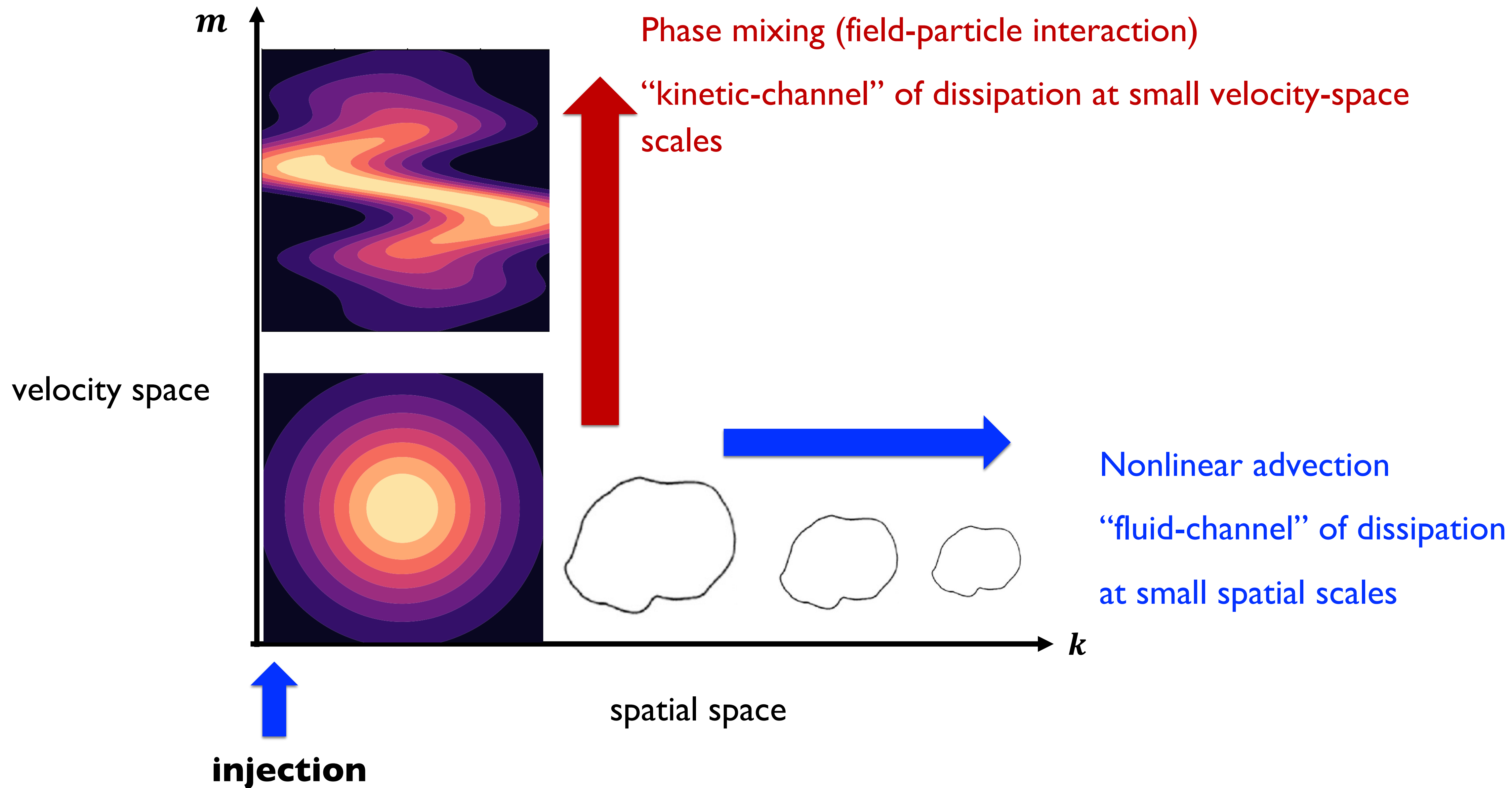
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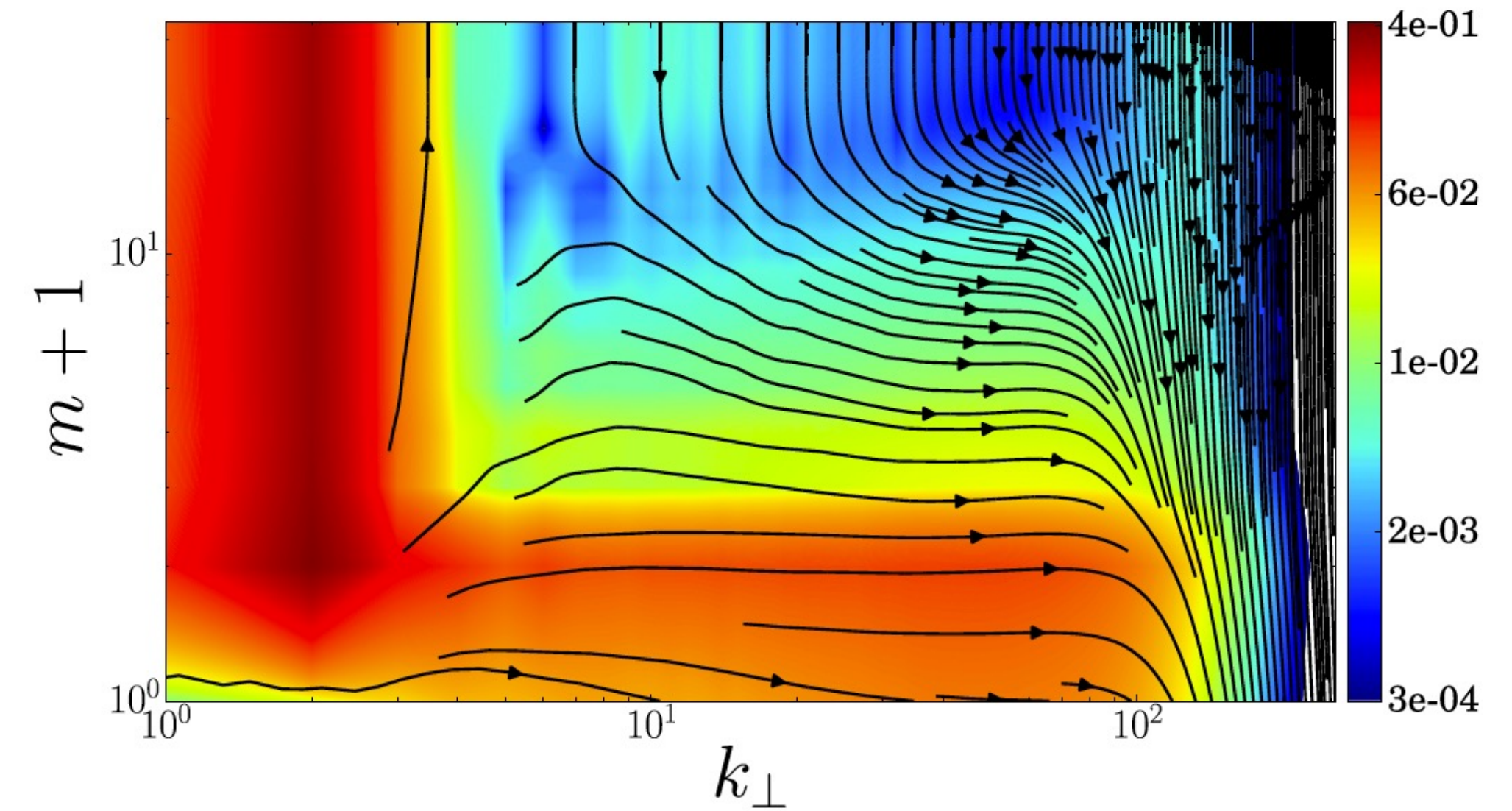
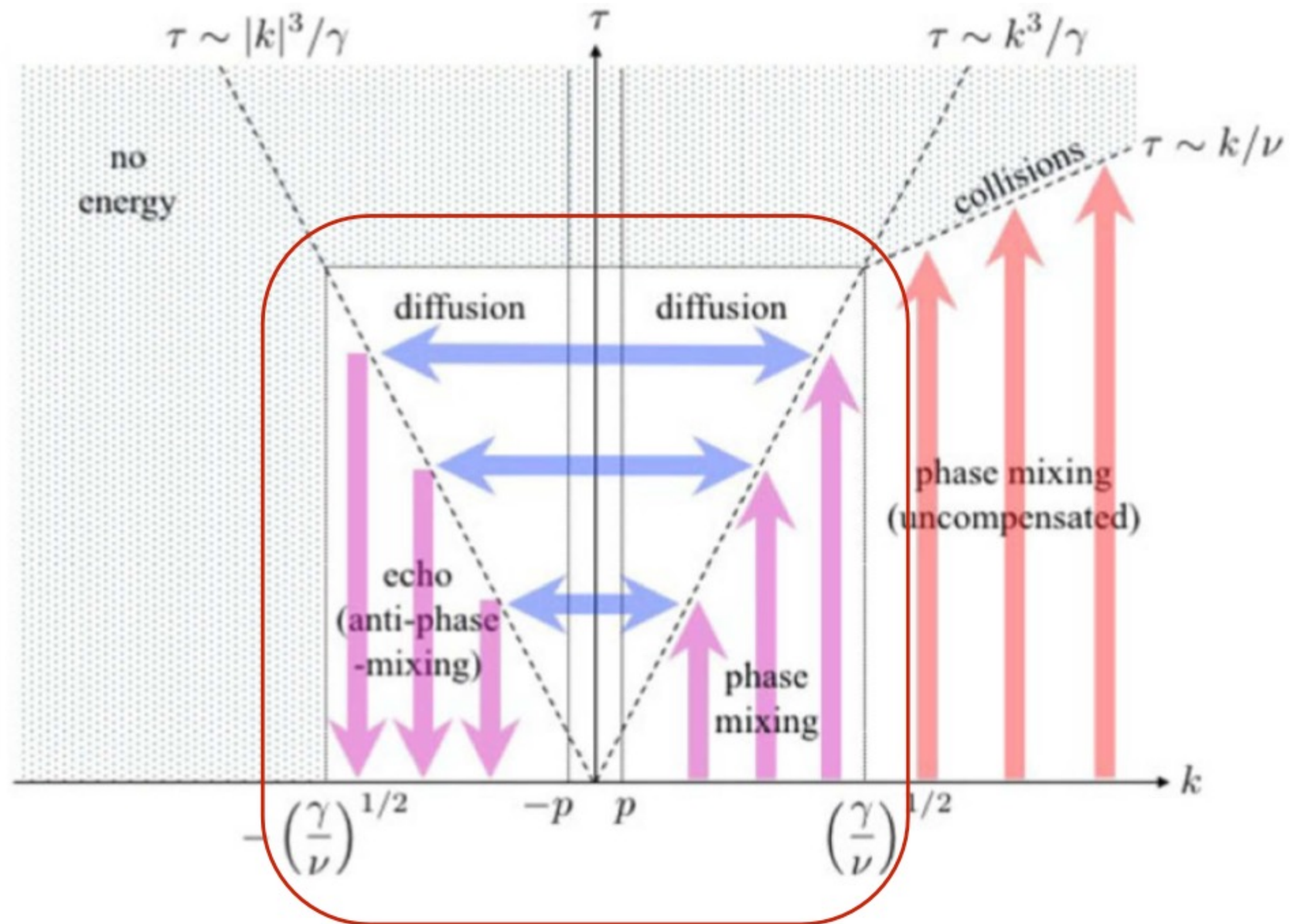
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Studying phase-space dynamics is crucial to understand particle heating



Anti-phase-mixing and plasma echoes

Schekochihin+ 2016; Adkins & Schekochihin 2018



Confirmed by simulations in the inertial range with compressive fluctuations [Meyrand+ 2018]

Q: is it obvious that echoes are expected in the sub- ρ_i range with electromagnetic fluctuations?

Kinetic Reduced Electron Heating Model (KREHM) framework

A rigorous asymptotic reduction of gyrokinetics (GK) valid in the limit of low electron plasma-beta $\beta_e \sim m_e/m_i$ [Zocco+ 2011]

Ions become isothermal.

GK Poisson's law containing FLR $\delta n_e/n_{0e} = 1/\tau(\hat{\Gamma}_0 - 1)e\varphi/T_{0e}$

Electrons are described by $\delta f_e = g_e + (\delta n_e/n_{0e} + 2v_{\parallel}u_{\parallel e}/v_{\text{the}}^2)F_{0e}$

Continuity:

$$\frac{1}{n_{0e}} \frac{d\delta n_e}{dt} = -\hat{b} \cdot \nabla \frac{e}{cm_e} d_e^2 \nabla_{\perp}^2 A_{\parallel}$$

Ohm's law

$$\frac{d}{dt}(A_{\parallel} - d_e^2 \nabla_{\perp}^2 A_{\parallel}) = -c \frac{\partial \varphi}{\partial z} + \frac{cT_{e0}}{e} \hat{b} \cdot \nabla \left(\frac{\delta n_e}{n_{0e}} + \frac{\delta T_{\parallel e}}{T_{0e}} \right)$$

Kinetic equation

$$\frac{dg_e}{dt} + v_{\parallel} \hat{b} \cdot \nabla \left(g_e - \frac{\delta T_{\parallel e}}{T_{0e}} F_{0e} \right) = C[g_e] + \left(1 - \frac{v_{\parallel}^2}{v_{\text{the}}^2} \right) F_{0e} \hat{b} \cdot \nabla \frac{e}{cm_e} d_e^2 \nabla_{\perp}^2 A_{\parallel}$$

Hermite expansion: $g_e(r, v_{\parallel}, t) = \sum_{m=0}^{\infty} H_m(v_{\parallel}/v_{\text{the}}) g_m(r, t) F_{0e}(v_{\parallel}) / \sqrt{2^m m!}$

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Kinetic equation

$$\frac{dg_m}{dt} = -v_{\text{the}} \hat{b} \cdot \nabla \left(\sqrt{\frac{m+1}{2}} g_{m+1} + \sqrt{\frac{m}{2}} g_{m-1} - \delta_{m,1} g_2 \right) - \sqrt{2} \delta_{m,2} \hat{b} \cdot \nabla \frac{e}{cm_e} d_e^2 \nabla_{\perp}^2 A_{\parallel}$$

g_m : Hermite moments of g_e

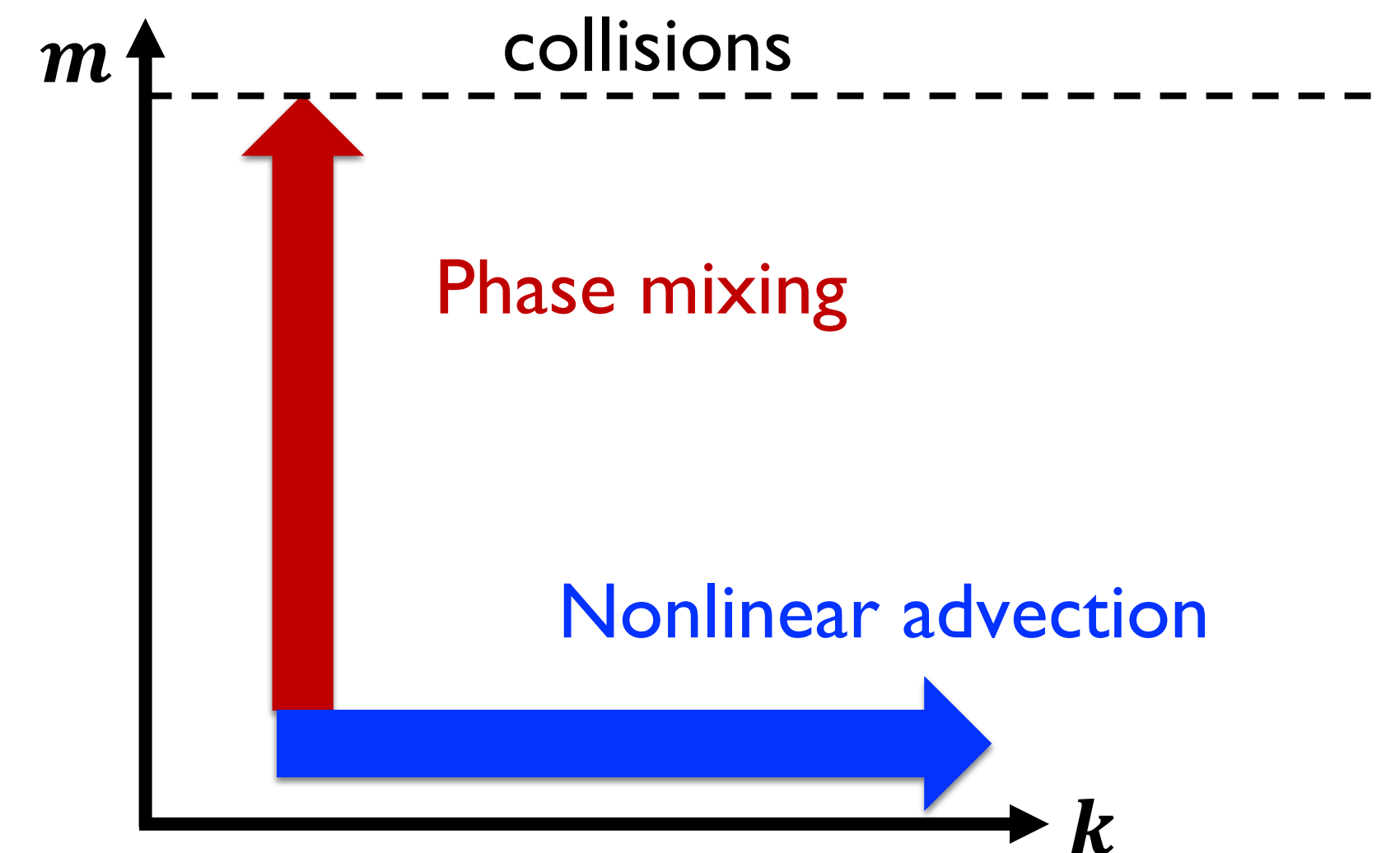
With kinetic electrons --- Phase space cascade and electron heating

$$\frac{dg_m}{dt} = \frac{\partial g_m}{\partial t} + \frac{c}{B_0} \{\varphi, g_m\}$$

Source of free energy in velocity space $\hat{\mathbf{b}} \cdot \nabla J_{\parallel}$

$$\boxed{\frac{dg_m}{dt}} = -v_{\text{the}} \hat{\mathbf{b}} \cdot \nabla \left(\underbrace{\sqrt{\frac{m+1}{2}} g_{m+1} + \sqrt{\frac{m}{2}} g_{m-1}}_{\text{collisions}} - \delta_{m,1} g_2 \right) - \sqrt{2} \delta_{m,2} \hat{\mathbf{b}} \cdot \nabla J_{\parallel}$$

$$\approx k_{\parallel} v_{\text{the}} g_m / \sqrt{m} \sim \frac{v_{\text{the}}}{B_0} \{A_{\parallel}, g_m\} / \sqrt{m}$$



Critical Hermite moments and echos?

$$\frac{dg_m}{dt} = \frac{\partial g_m}{\partial t} + \frac{c}{B_0} \{\varphi, g_m\}$$

Source of free energy in velocity space $\hat{\mathbf{b}} \cdot \nabla J_{\parallel}$

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$$\approx k_{\parallel} v_{\text{the}} g_m / \sqrt{m} \sim \frac{v_{\text{the}}}{B_0} \{A_{\parallel}, g_m\} / \sqrt{m}$$

At each scale λ , there is a critical Hermite order m_{cr} :

nonlinear advection rate \sim Phase mixing rate

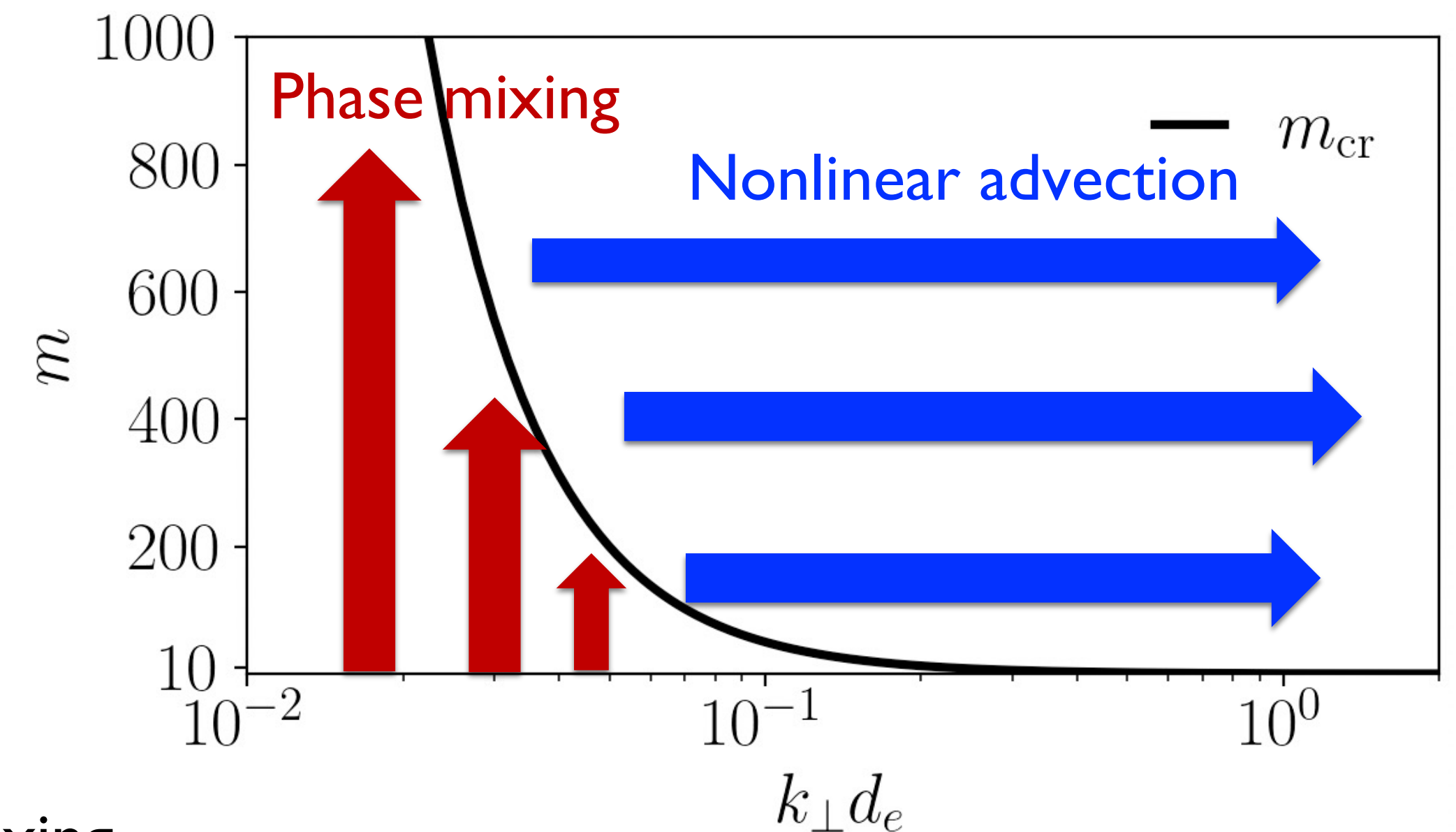
$$\frac{c}{B_0} \{\varphi, g_{m_{cr}}\} \sim \frac{v_{\text{the}}}{B_0} \{A_{\parallel}, g_{m_{cr}}\} / \sqrt{m_{cr}}$$

$$m_{cr}(\lambda) \sim (\lambda/d_e)^2 / (2\tau^2)$$

Above m_{cr} plasma echo is expected to happen and impede phase mixing

In weakly collisional plasmas, the collisional cut off $\gg m_{cr}$

Why is efficient electron heating observed in solar wind [Chen+ 2019] and in kinetic simulations[e.g. Howes+2016-2018]?



A zeroth-order solution of g_e in the velocity space and its Hermite spectrum

$$\frac{dg_m}{dt} = \frac{\partial g_m}{\partial t} + \frac{c}{B_0} \{\varphi, g_m\}$$

Source of free energy in velocity space $\hat{\mathbf{b}} \cdot \nabla J_{\parallel}$

$$\boxed{\frac{dg_m}{dt}} = -v_{\text{the}} \hat{\mathbf{b}} \cdot \nabla \left(\underbrace{\sqrt{\frac{m+1}{2}} g_{m+1} + \sqrt{\frac{m}{2}} g_{m-1} - \delta_{m,1} g_2}_{\approx k_{\parallel} v_{\text{the}} g_m / \sqrt{m}} \right) - \sqrt{2} \delta_{m,2} \hat{\mathbf{b}} \cdot \nabla J_{\parallel}$$

$$\approx k_{\parallel} v_{\text{the}} g_m / \sqrt{m} \sim \frac{v_{\text{the}}}{B_0} \{A_{\parallel}, g_m\} / \sqrt{m}$$

In the phase-mixing dominated regime, *l.h.s.* \ll *r.h.s.*

To the lowest order:

$$g_{m+1} = -\sqrt{m/(m+1)} g_{m-1} \quad \text{for } m \geq 3, \text{ and}$$

$$g_3 = -\sqrt{2/3} (\rho_s/d_e) J_{\parallel}$$

The Hermite spectrum of g_e :

$$E_m \equiv \langle |g_m|^2 / 2 \rangle \approx \langle |g_{m+1}| |g_{m-1}| \rangle / 2$$

$$E_{m+1}/E_{m-1} \approx g_{m+1} g_m / (g_{m-1} g_{m-2}) = \sqrt{(m-1)/(m+1)}$$

$$E_m \propto m^{-1/2}$$

Turbulence at scales below the electron skin depth

In the range $\lambda \ll d_e \lesssim \rho_i$, fluctuations become electrostatic.

Equipartition between density fluctuations and kinetic energy of parallel electron flows:

$$(\delta n_e/n_{0e})^2 n_{0e} T_{0e} \sim d_e^2 |\nabla_{\perp}^2 A_z|^2 / 8\pi \longrightarrow \varphi_{\lambda} \sim (\rho_i V_A / c) d_e \delta B_{\perp \lambda} / \lambda$$

Assuming standard Kolmogorov-type cascade: $\varepsilon \sim \gamma_{nl} e^2 n_{0e} \varphi^2 / T_{0e}$ $\gamma_{nl} \sim \varphi_{\lambda} / \lambda^2$

$$E_{\varphi}(k_{\perp}) \propto k_{\perp}^{-7/3}, \quad E_B(k_{\perp}) \propto k_{\perp}^{-13/3}.$$

Critical m_{cr} where phase-mixing rate balance nonlinear-advection rate:

$$m_{cr} \sim (\lambda/d_e)^4 / (2\tau^2)$$

At $k_{\perp} d_e \gg 1$, nonlinear advection is always faster than phase mixing --- fluid-channel of dissipation should dominate \rightarrow steep Hermite spectrum

Numerical simulations

We perform simulations for turbulence in the kinetic range by solving KREHM equations

White-noise forcing added to the continuity equation (forcing density perturbation) at box scale

Balanced turbulence

Energy injection balanced by dissipation through hyper-collision at large m or through hyper-diffusion at large k_{\perp}

- **Isothermal** limit, i.e., $g_e = 0$: Energy **spectra** of fluctuations, spectral anisotropy, intermittency
- **electron kinetic** physics accounted for ($g_e \neq 0$): **phase space dynamics**, electron heating

Spectra and spectral anisotropy

Existing models:

- Kolmogorov-type cascade of KAWs --- $k_{\perp}^{-7/3}$. [Cho&Lazarian 2004; Howes+ 2008; Schekochihin+ 2009]
- Intermittency --- $k_{\perp}^{-8/3}$ and $k_{\parallel}^{-7/2}$ [Boldyrev&Perez 2012]
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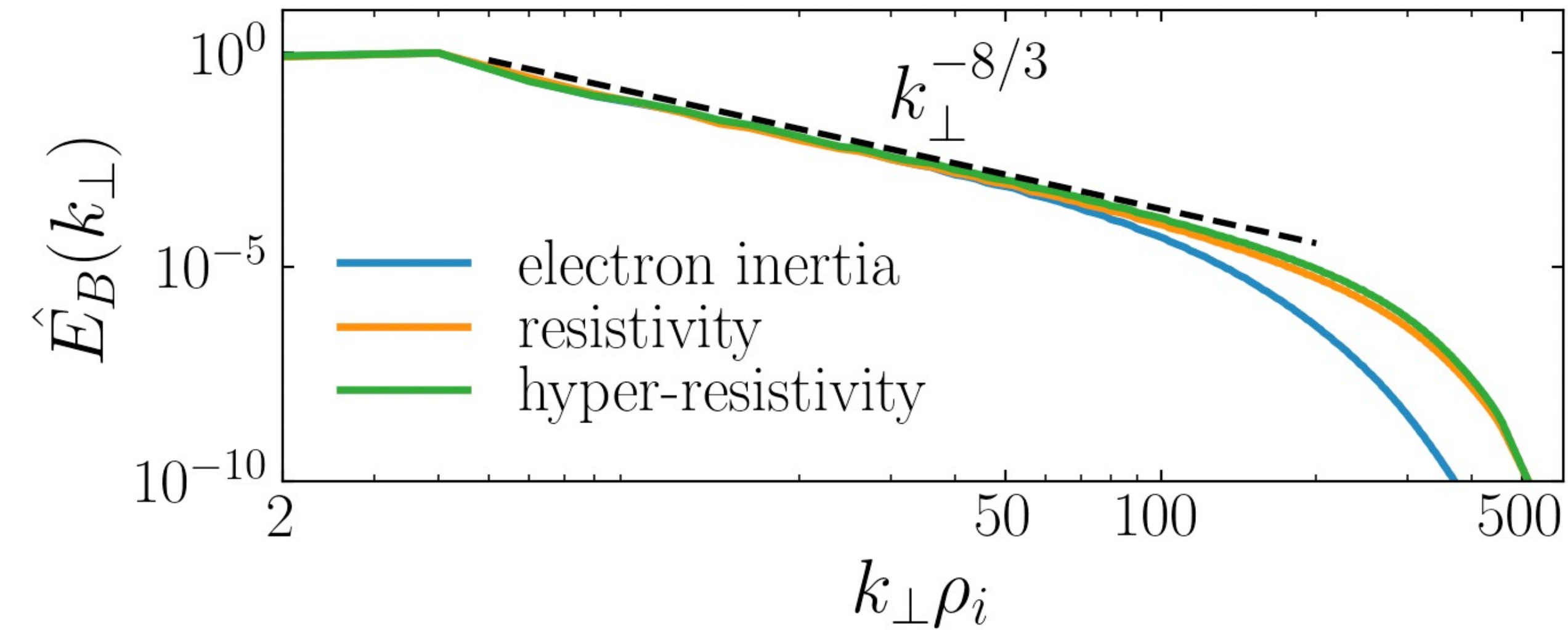
Our approach to distinguish the role of intermittency vs tearing mediation:

In numerical simulations, **the frozen flux** constraint can instead be **broken by (hyper) resistivity** $\eta_H \nabla_{\perp}^{\alpha}$:

$$E_B(k_{\perp}) dk_{\perp} \propto k_{\perp}^{-(7n\alpha+2\alpha+2)/(3n\alpha+2)} dk_{\perp}.$$

n is the parameter for the configuration of magnetic fields: n=1 Harris sheet; n=2 sinusoidal profile

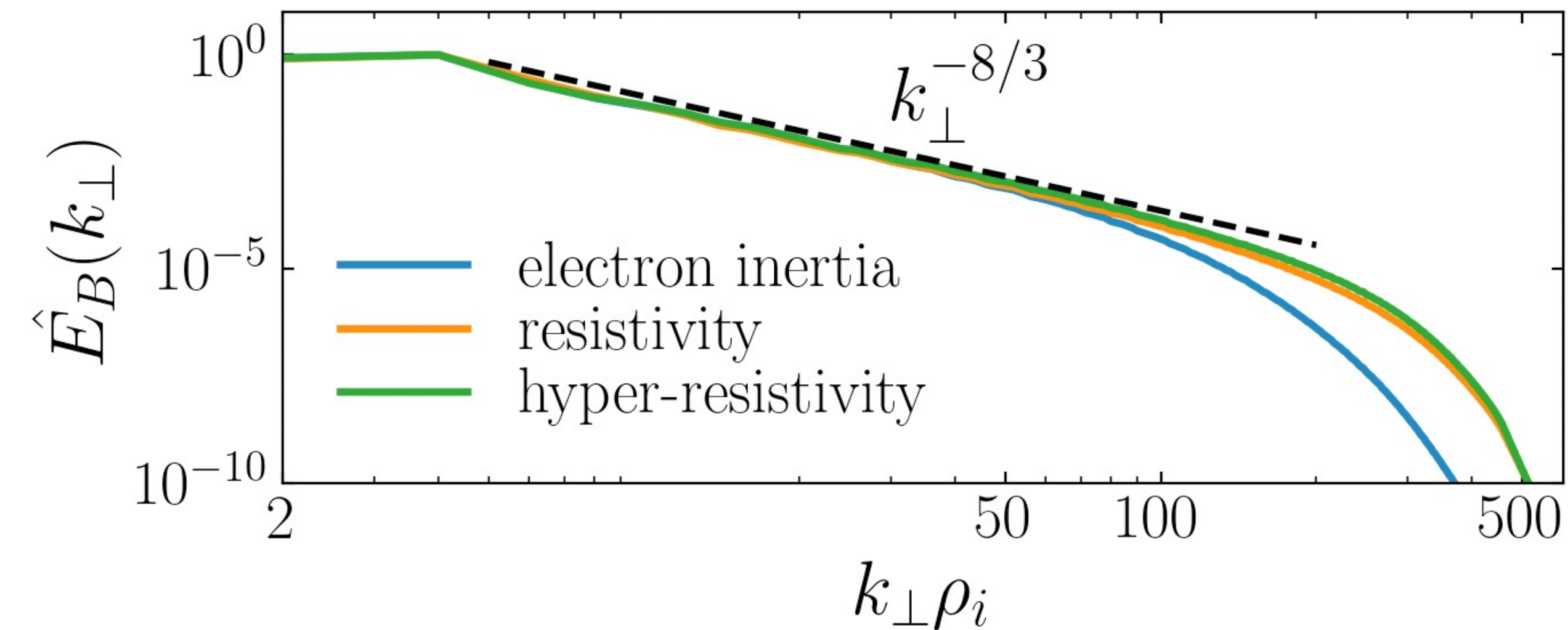
Isothermal simulations – Energy spectra



Simulations are performed in the sub- ρ_i range, with the **flux-unfreezing mechanism** being the main difference.

$\sim k_\perp^{-8/3}$ spectrum; predicted by the intermittency model and the tearing-mediation model

Energy spectra is not set by tearing mediation



Simulations are performed in the sub- ρ_i range, with the **flux-unfreezing mechanism** being the main difference.

If the spectra are set by the tearing mediation:

$$E_B(k_{\perp})dk_{\perp} \propto k_{\perp}^{-(7\alpha+3)/(3\alpha+1)}$$

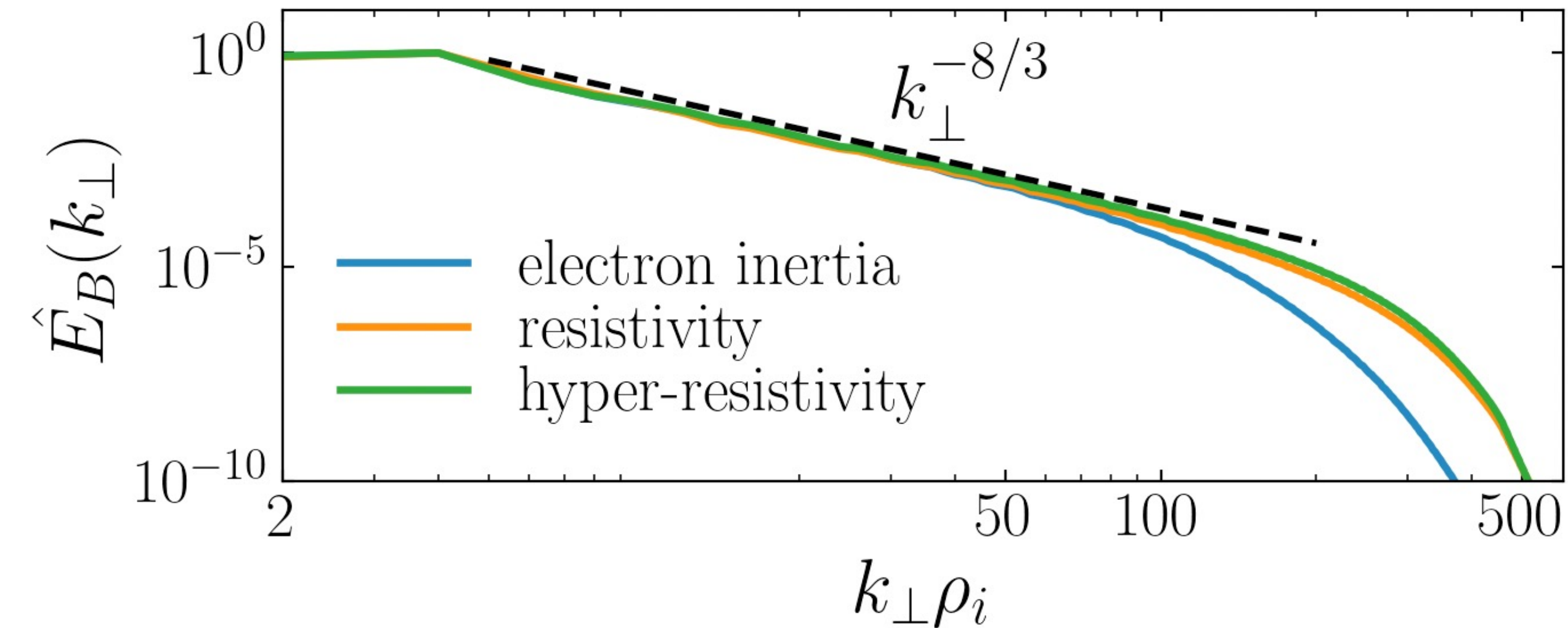
Electron inertia: -8/3

Resistivity: -2.4

Hyper-resistivity: -2.6

*The overlap of the spectra **rules out tearing-mediation** as the physical mechanism underpinning the energy cascade.*

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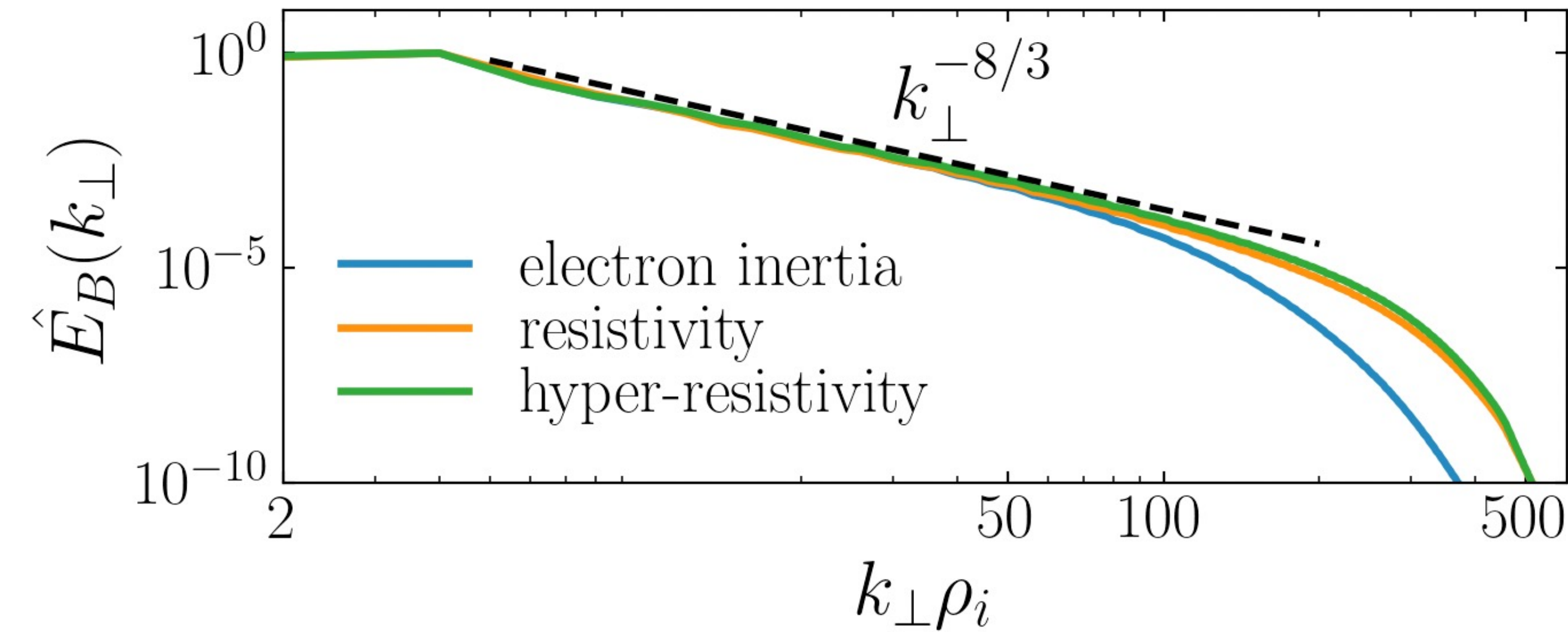
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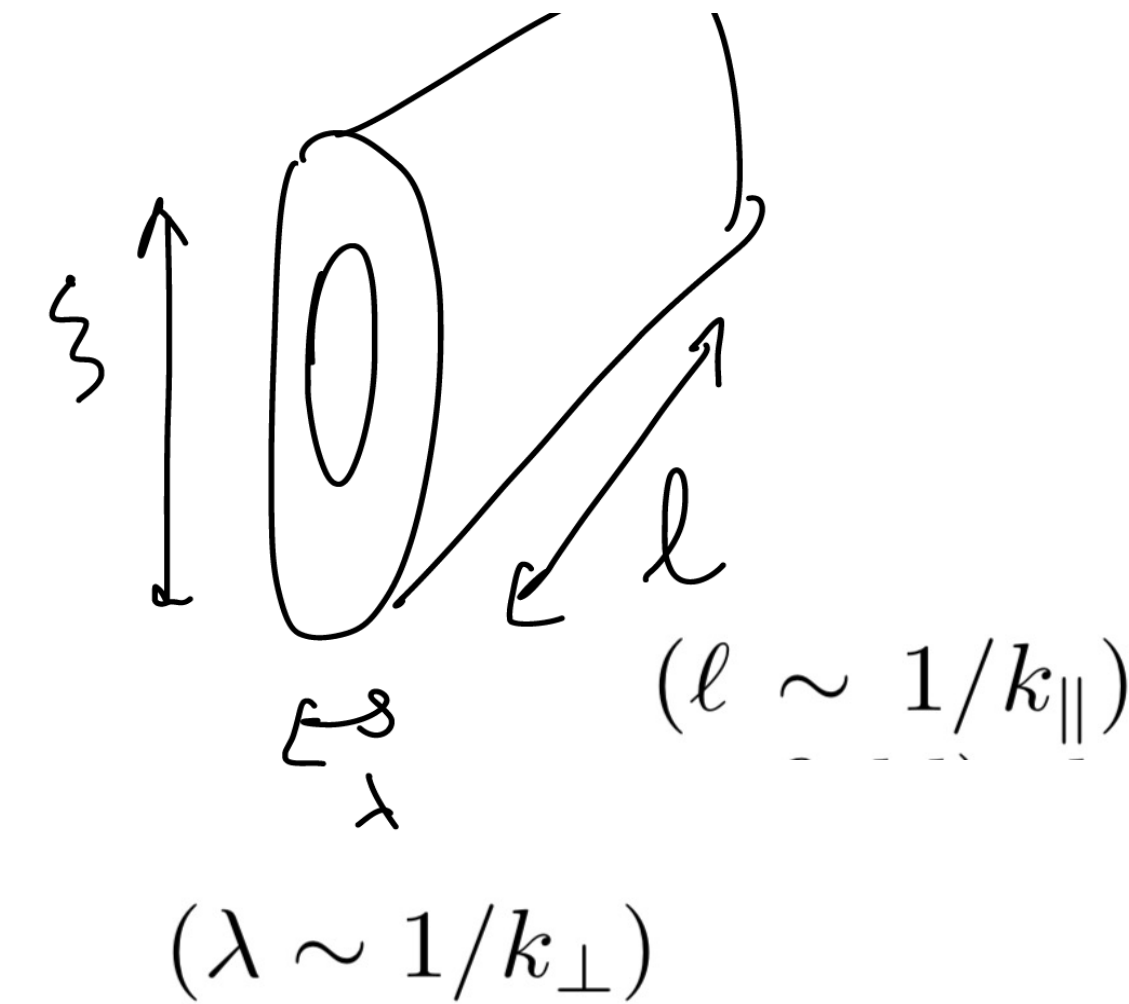
Spectral anisotropy shows no evidence of progressive alignment



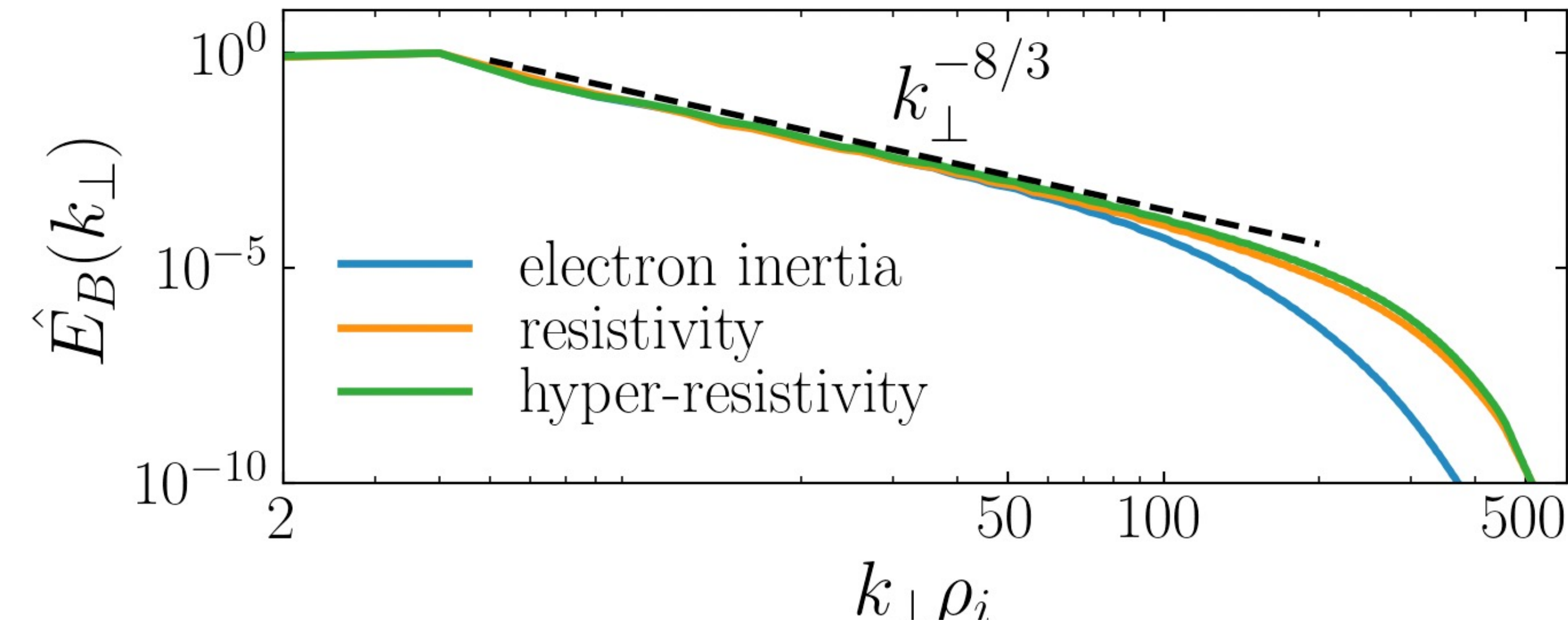
Why don't the turbulence eddies become tearing unstable?

3D structure functions of the magnetic fields:

$$S_2(\delta \mathbf{r}) \equiv \langle |\Delta \mathbf{B}(\mathbf{r}, \delta \mathbf{r})|^2 \rangle_{\mathbf{r}}$$



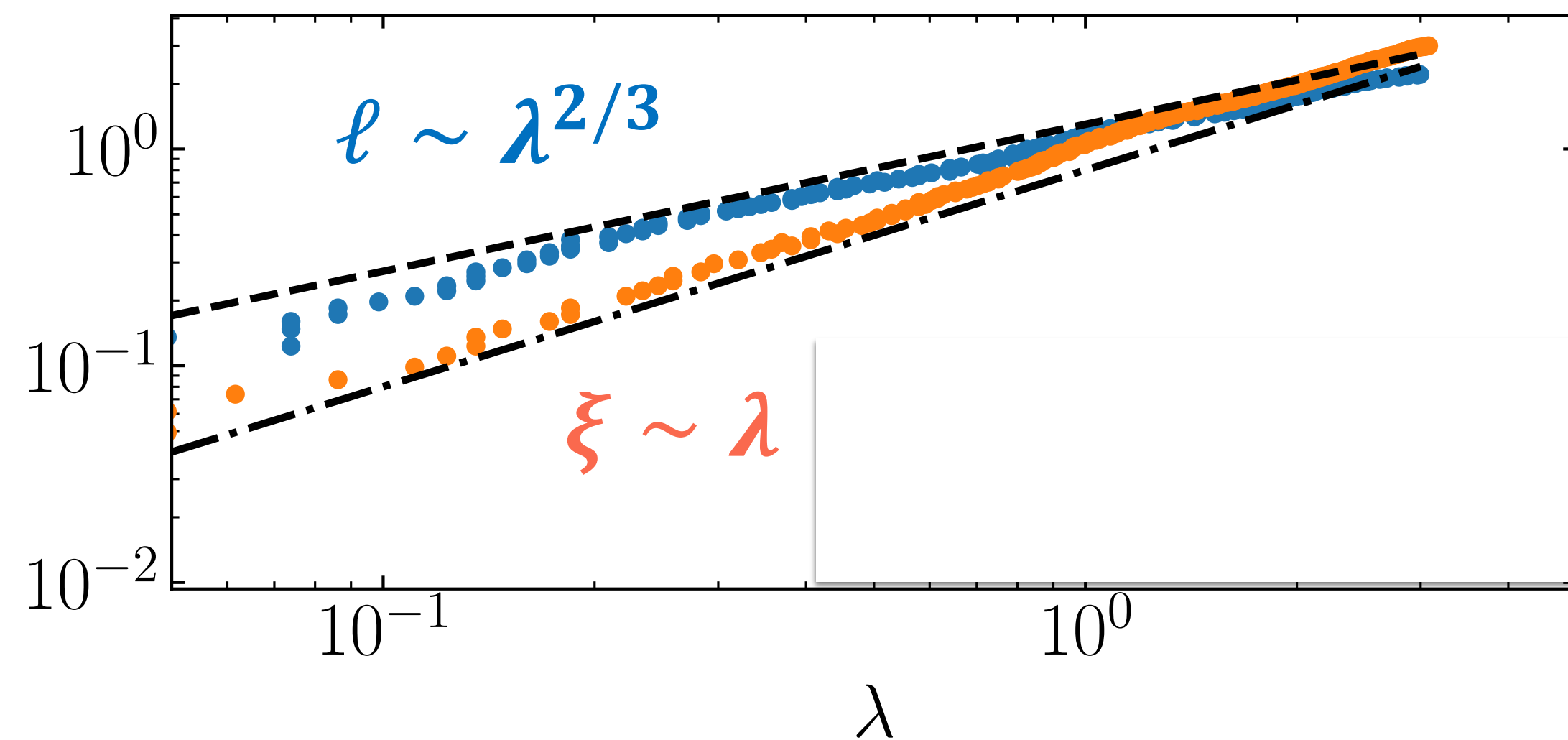
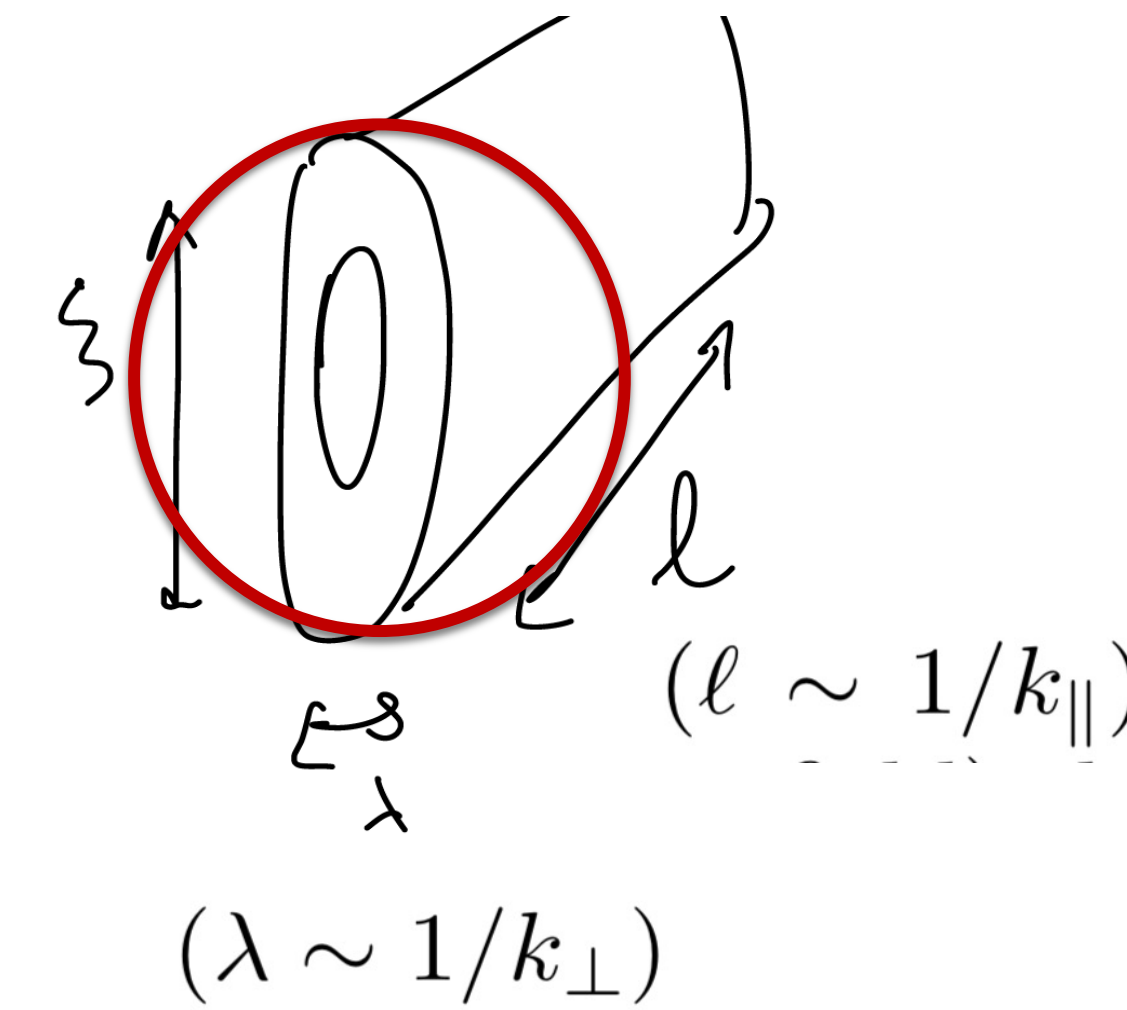
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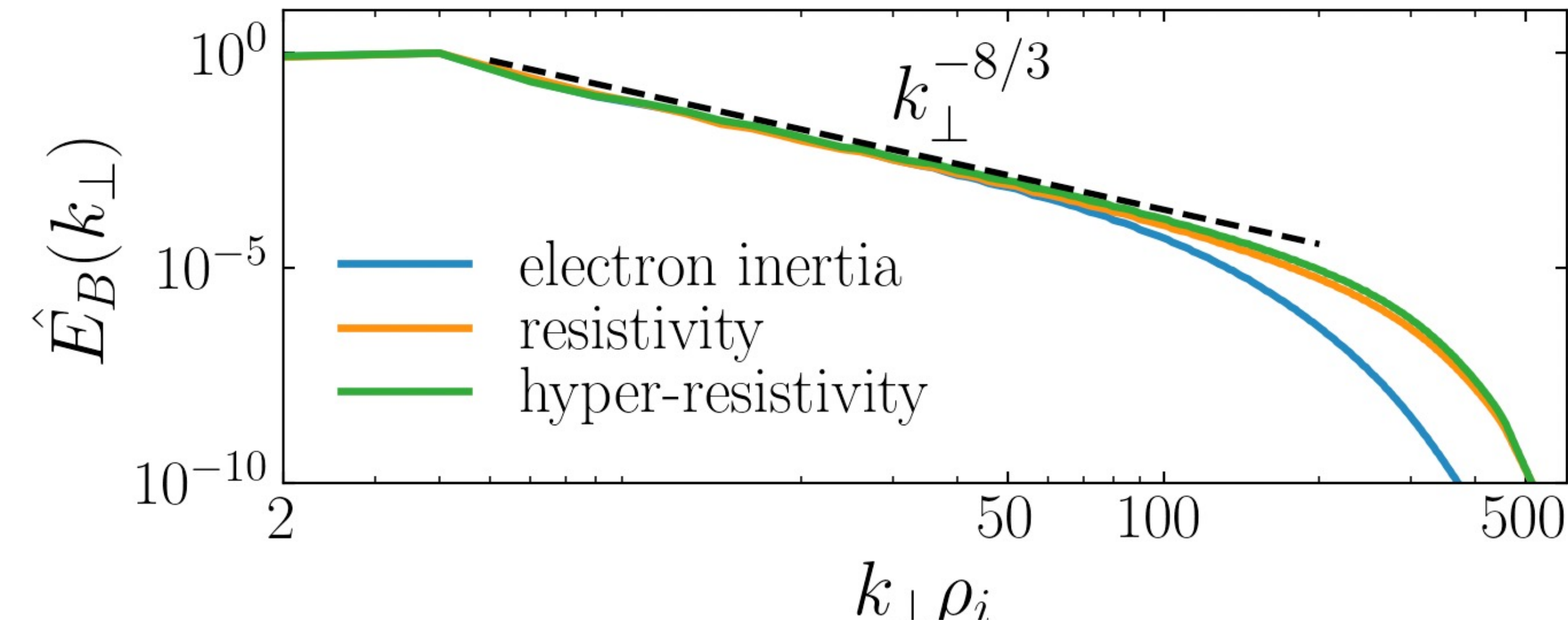
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Isotropic morphology of eddies in perpendicular planes
 – *no progressive alignment for tearing mediation*

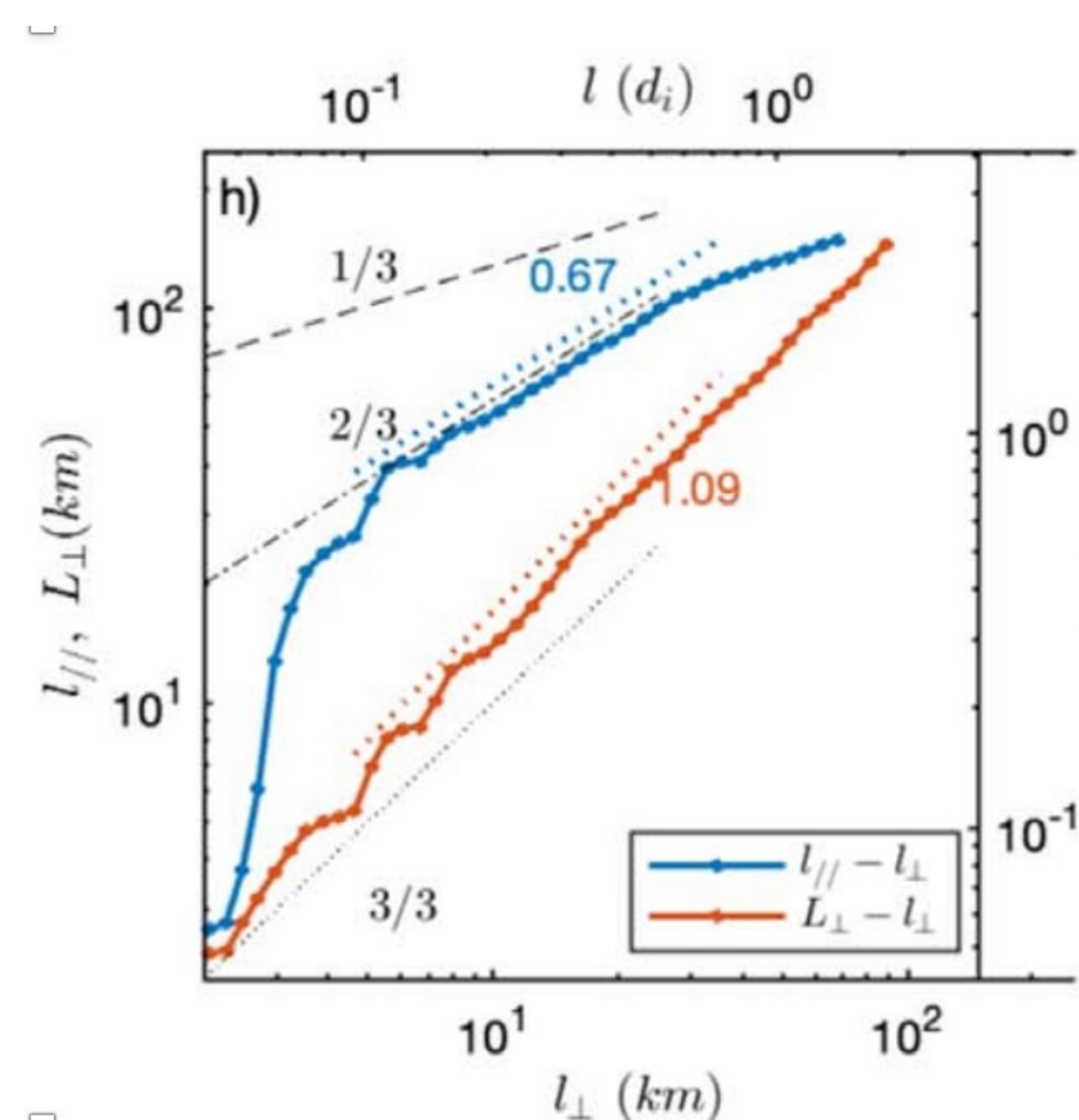
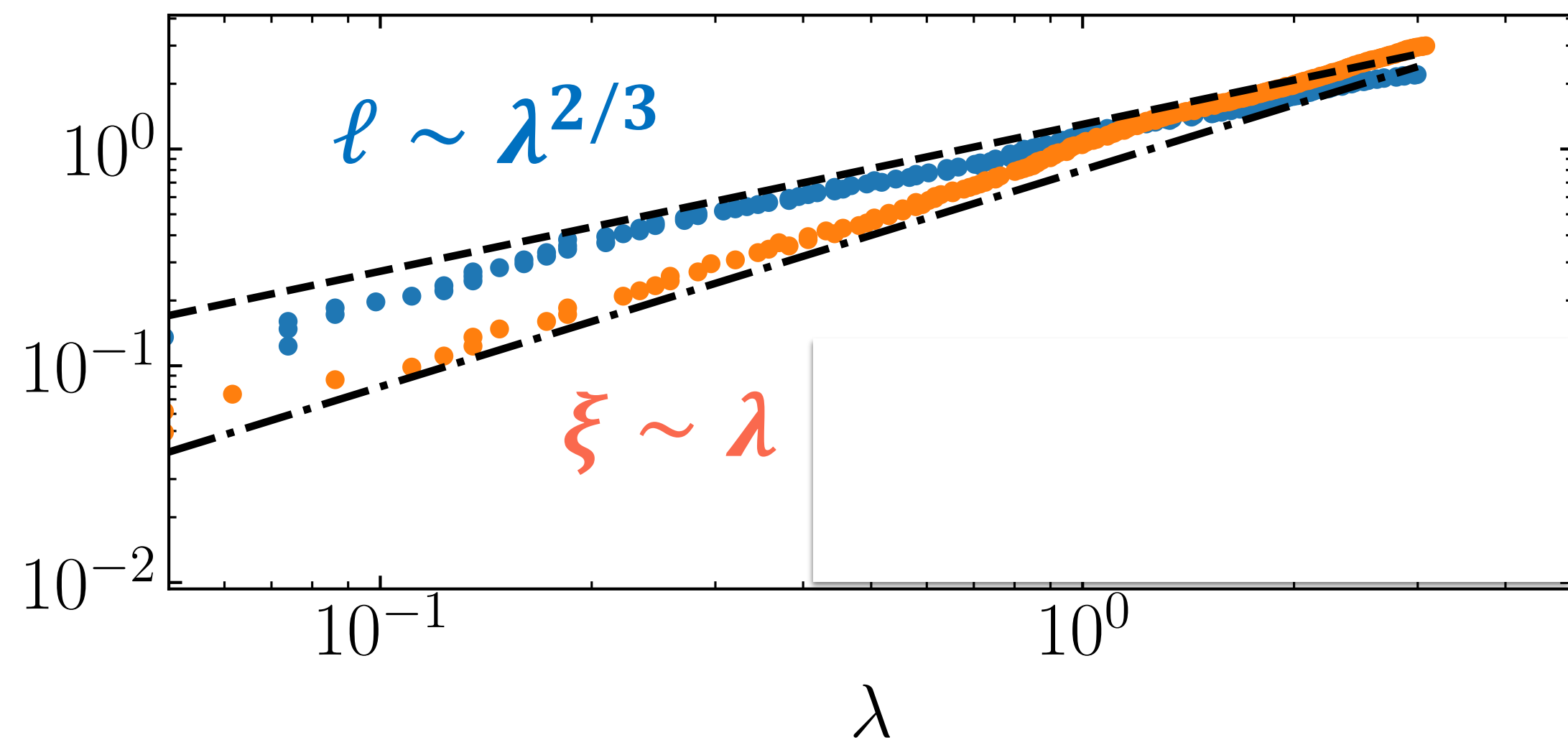
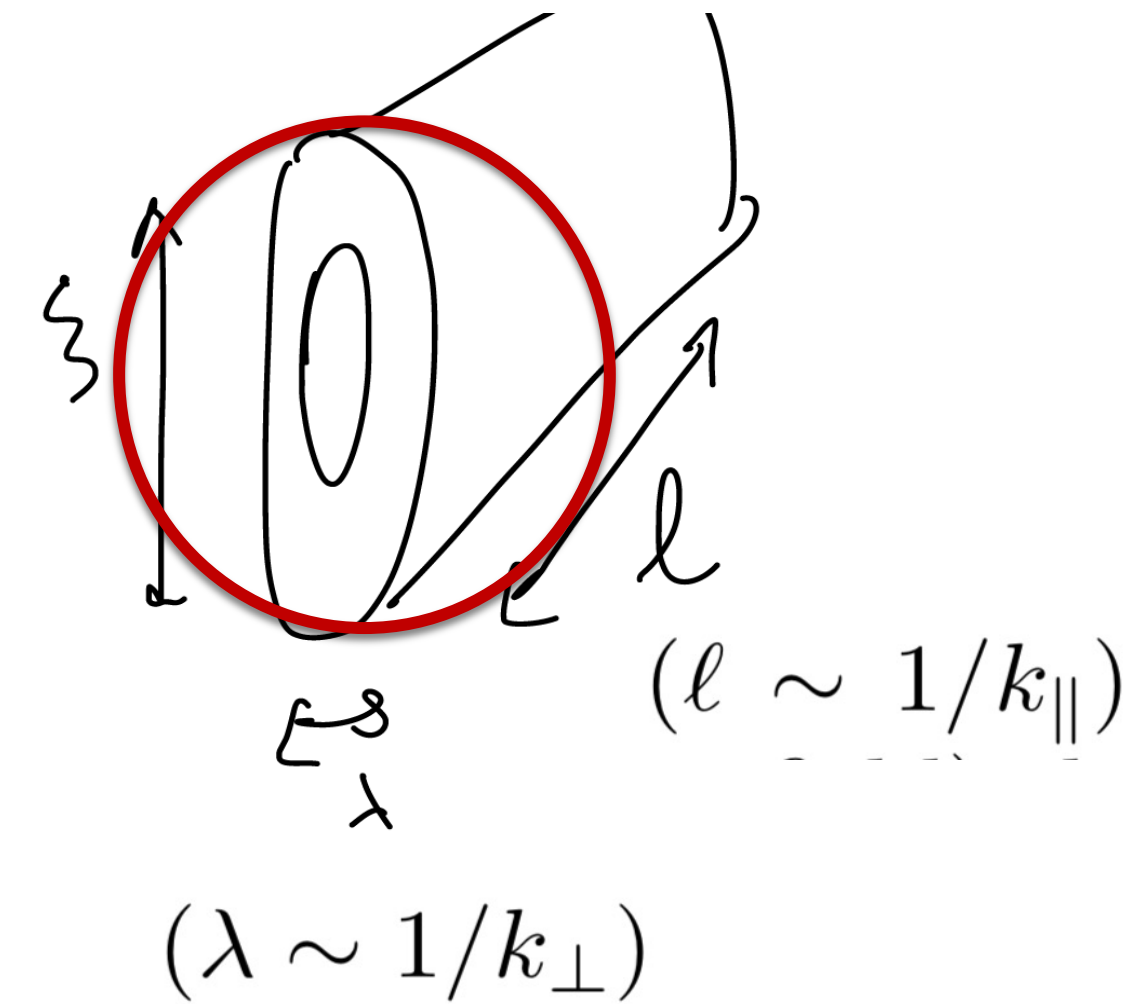
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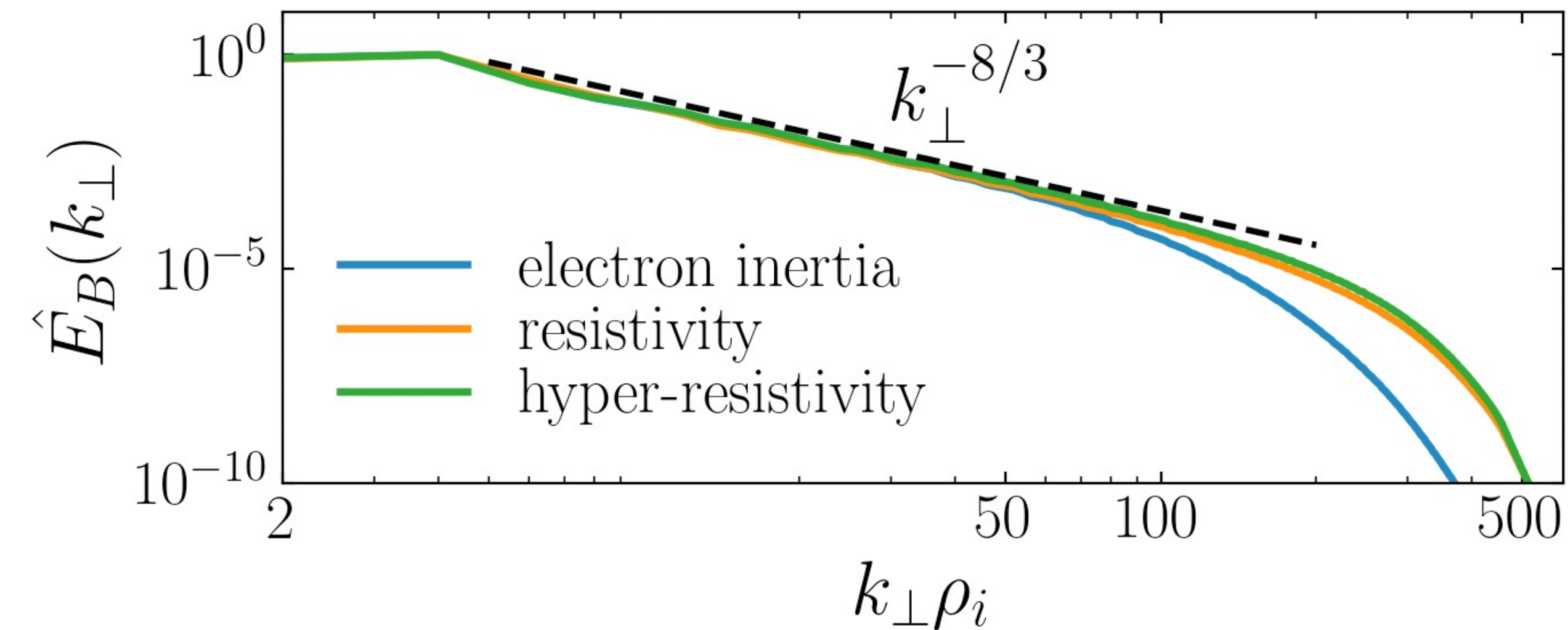


Solar wind measurements from MMS and PSP

[Wang+ 2020; Zhang+2022;]

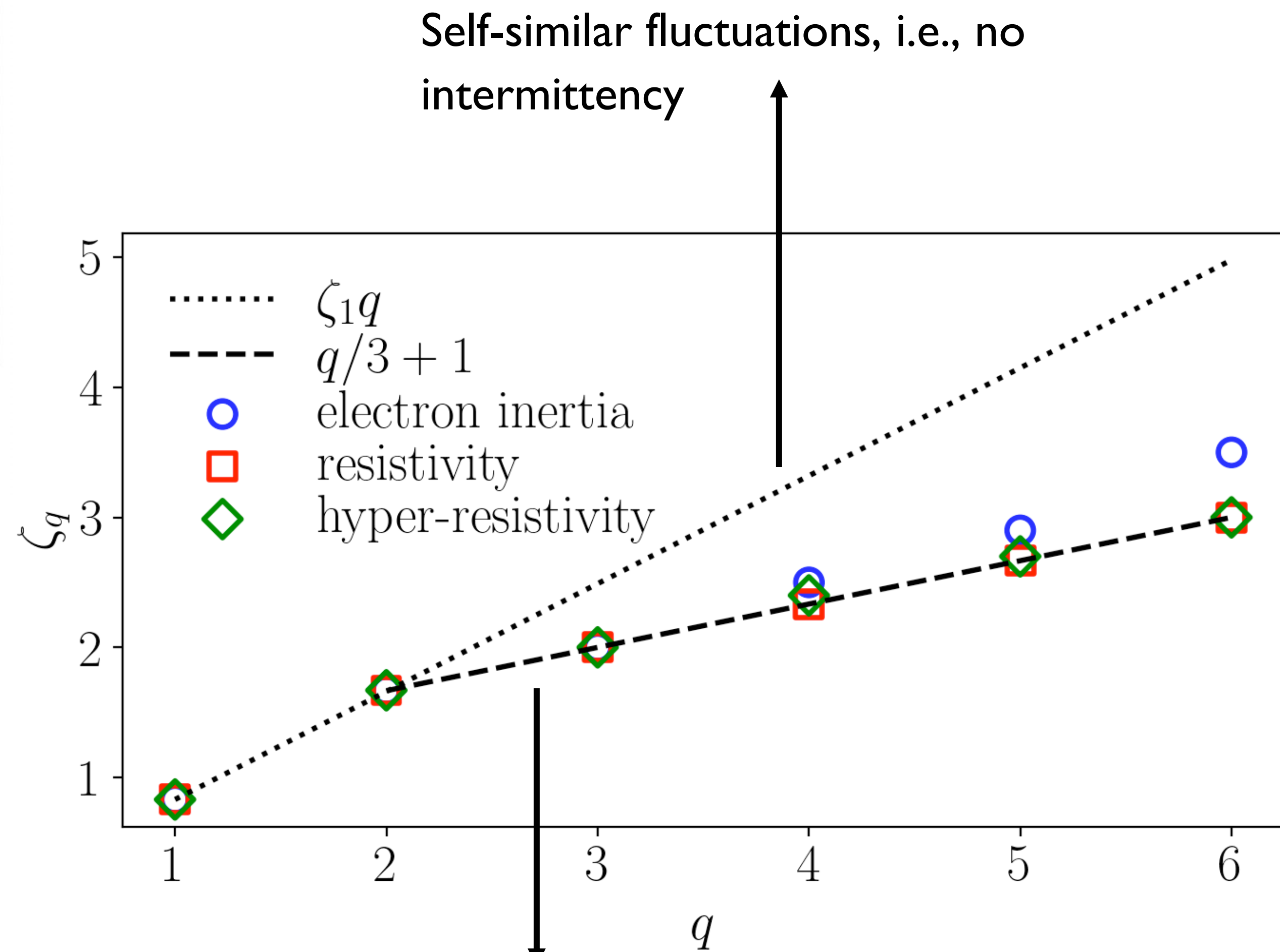
Isotropic morphology of eddies in perpendicular planes
 – *no progressive alignment for tearing mediation*

High-order structure function indicates 2D intermittent structures



Using higher order structure functions to quantify intermittency

$$S_q(\delta \mathbf{r}) \equiv \langle |\Delta \mathbf{B}(\mathbf{r}, \delta \mathbf{r})|^q \rangle_{\mathbf{r}} \sim \delta \mathbf{r}^{\zeta_q}$$



2D Intermittent structures;

Main assumption to derive the -8/3 spectrum by Boldyrev&Perez 2012

Simulations with kinetic electrons

MHD transition to sub- ρ_i ,
 d_e unresolved

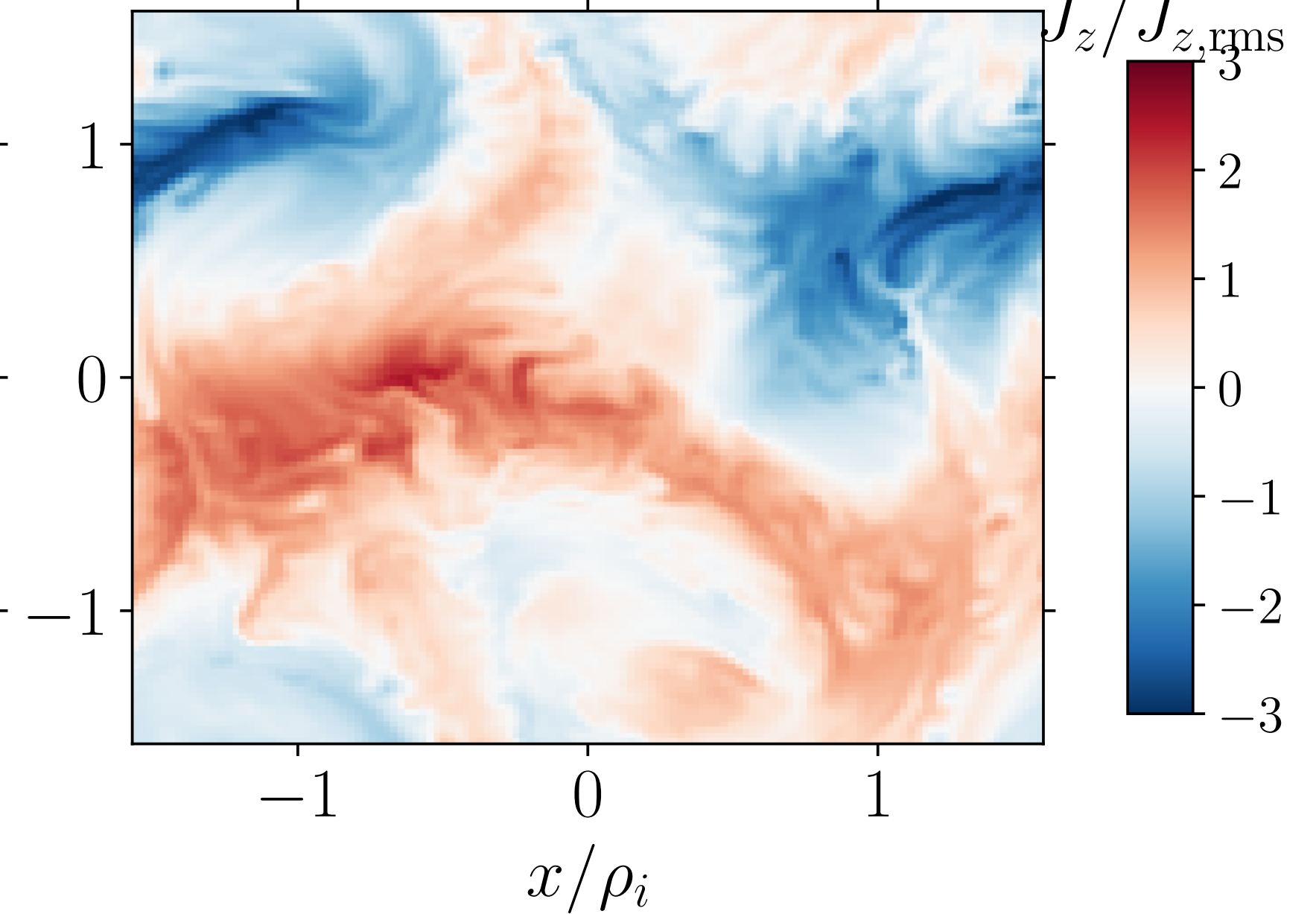
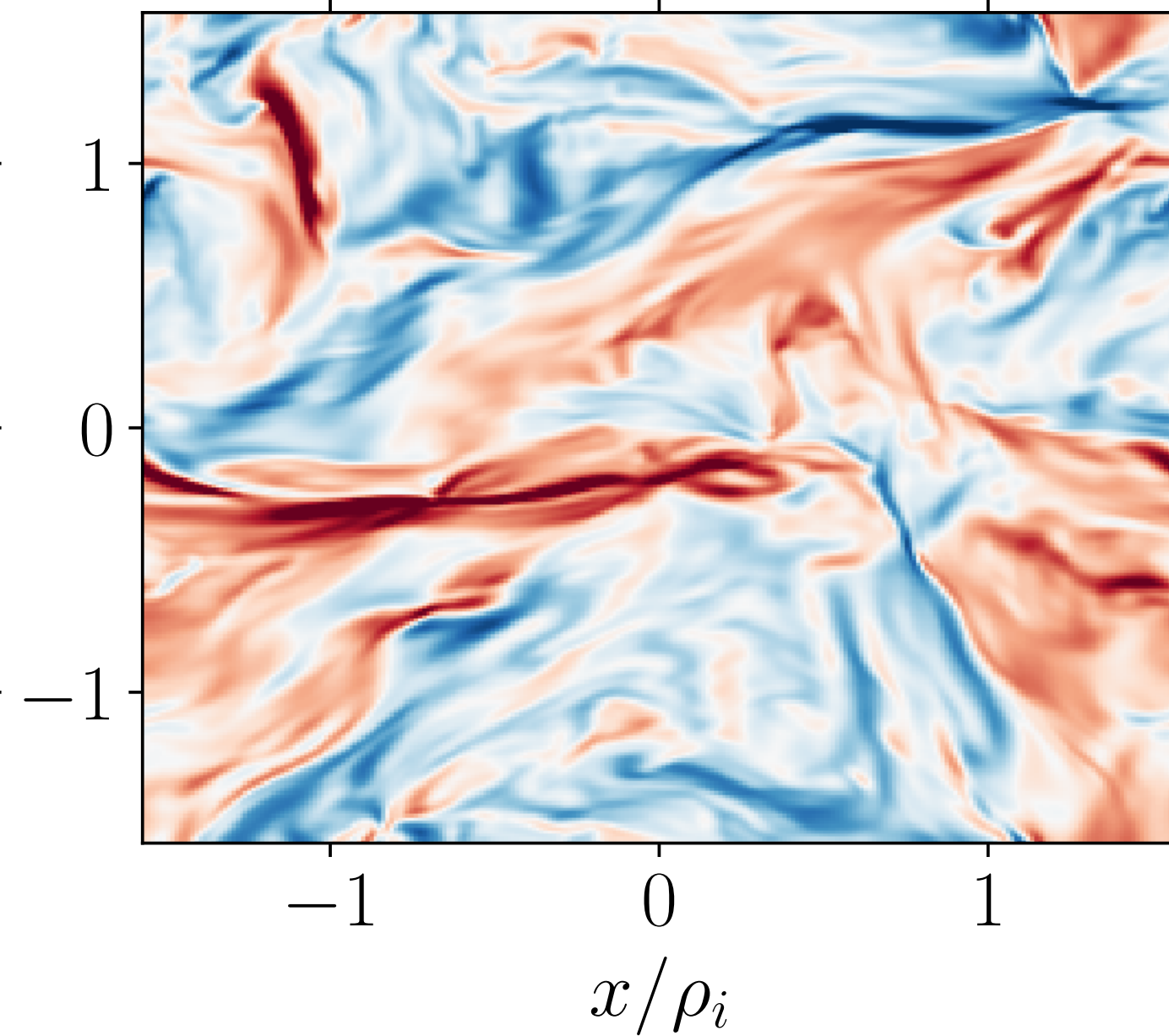
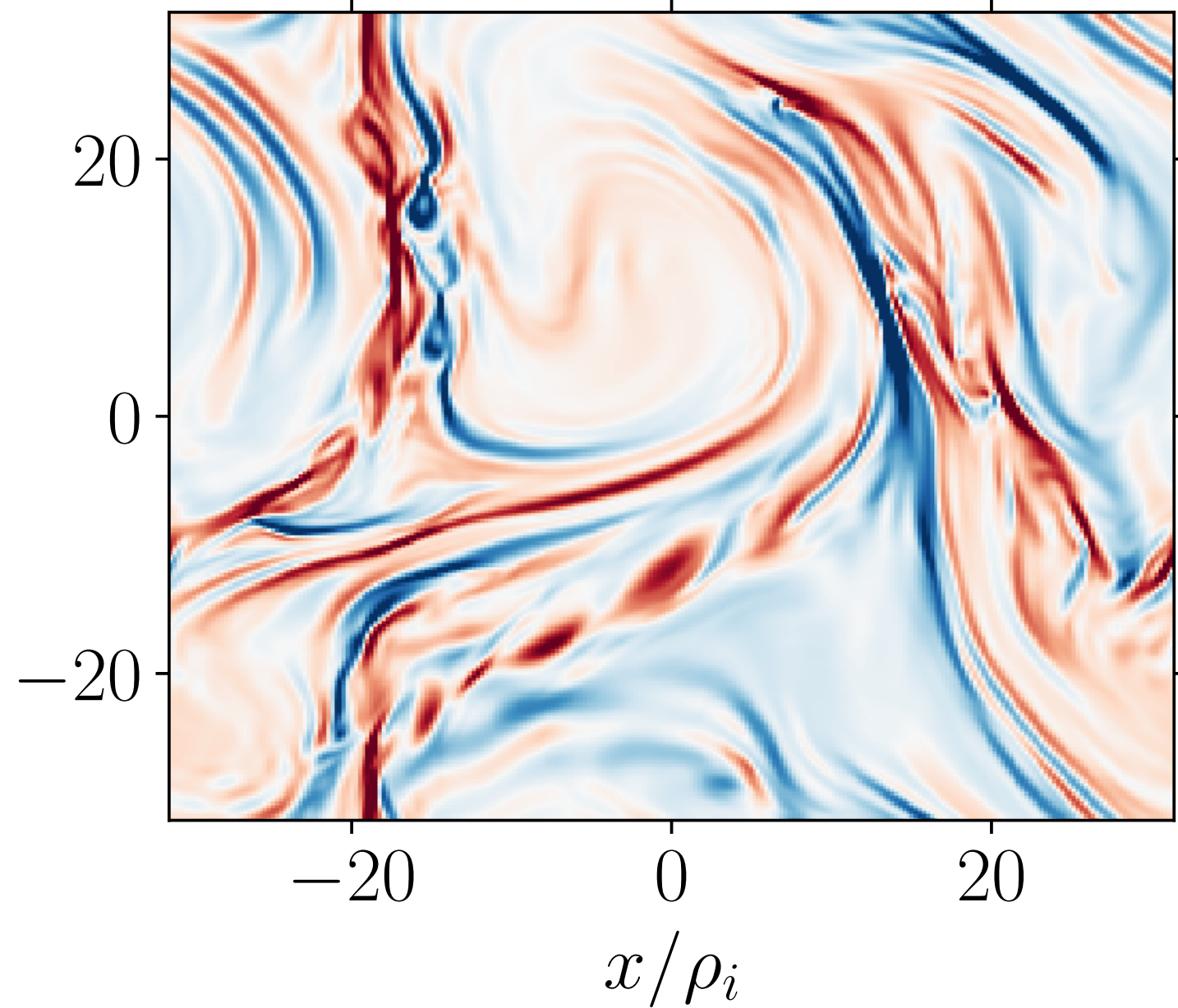
sub- ρ_i , d_e resolved

sub- d_e

Run K1

Run K2a

Run K3



$$\frac{\rho_i}{L} = 0.1; k_{\perp, \max} d_e = 1$$

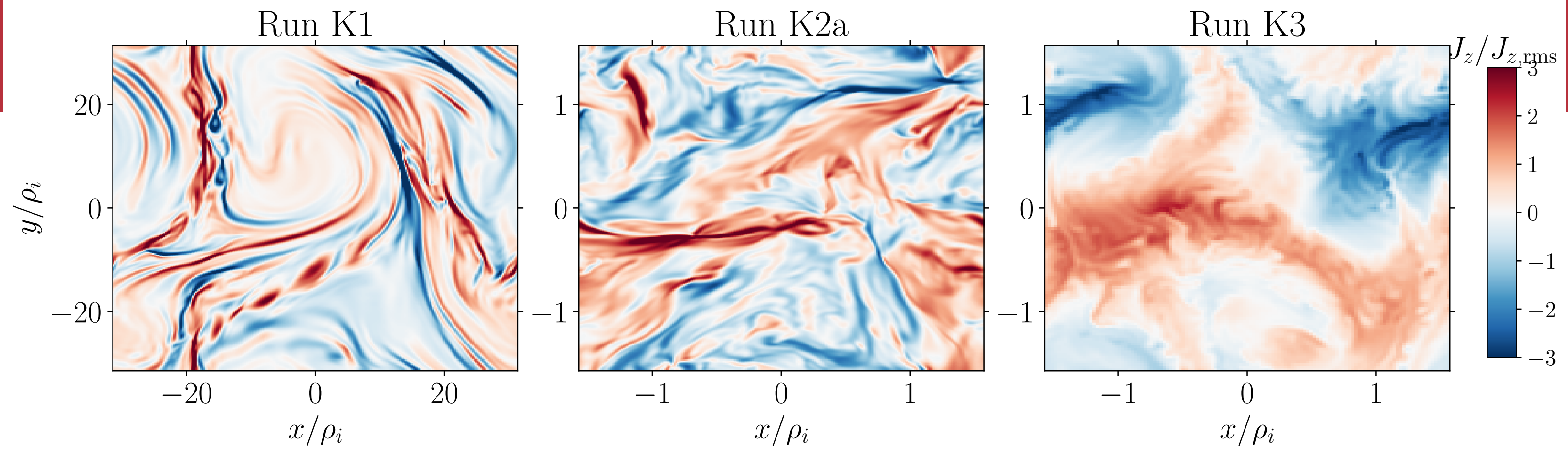
$$\frac{\rho_i}{L} = 2; k_{\perp, \max} d_e = 10$$

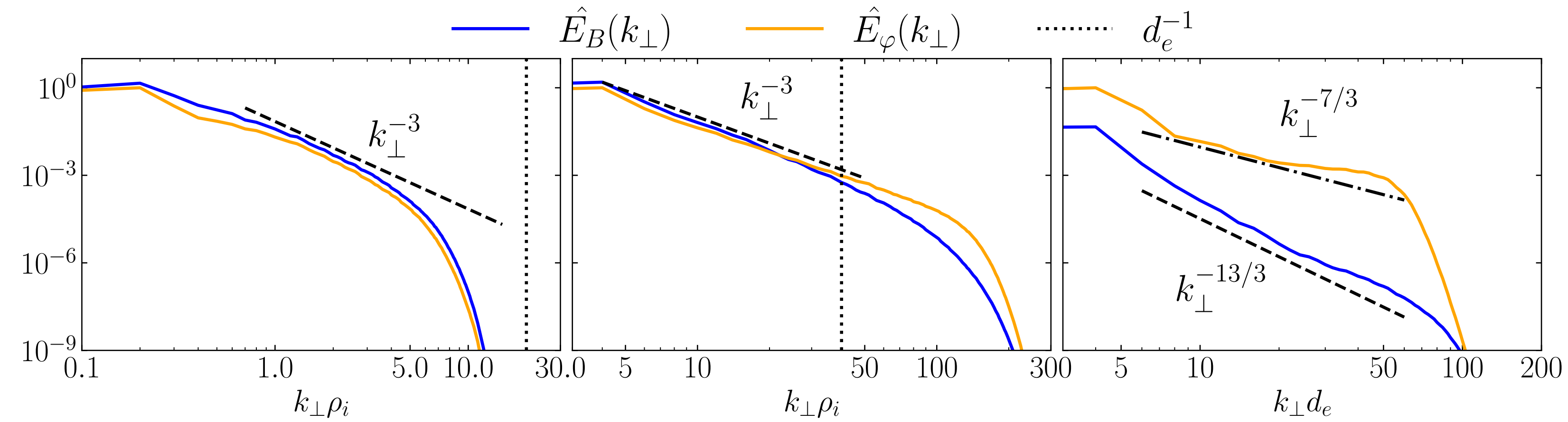
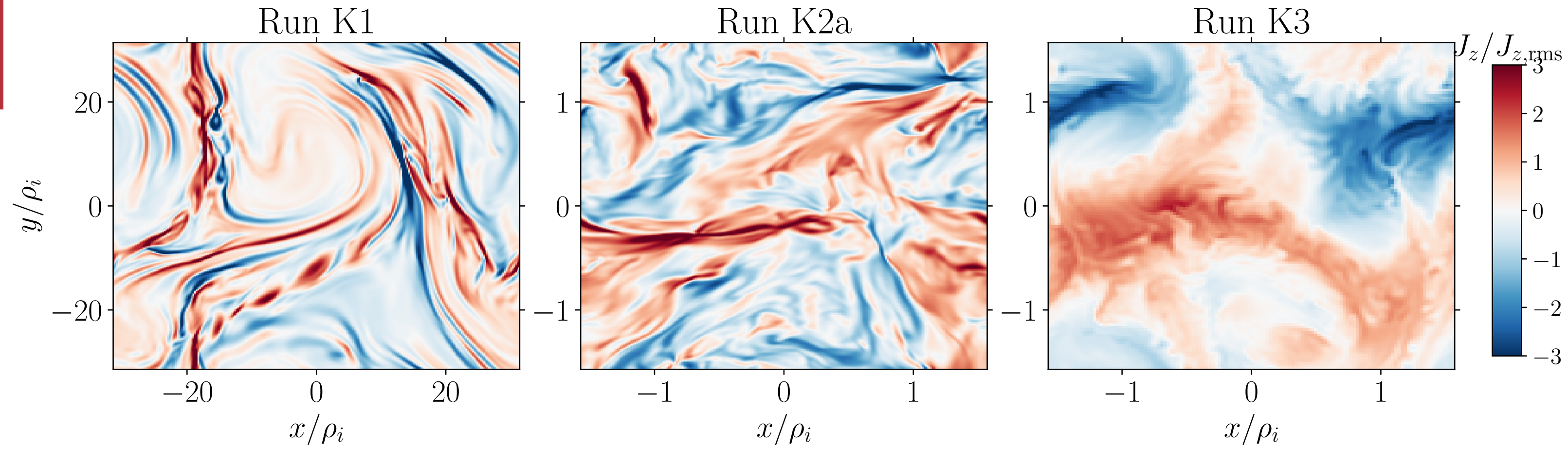
$$\rho_i = d_e = 2L$$

MHD to ρ_i

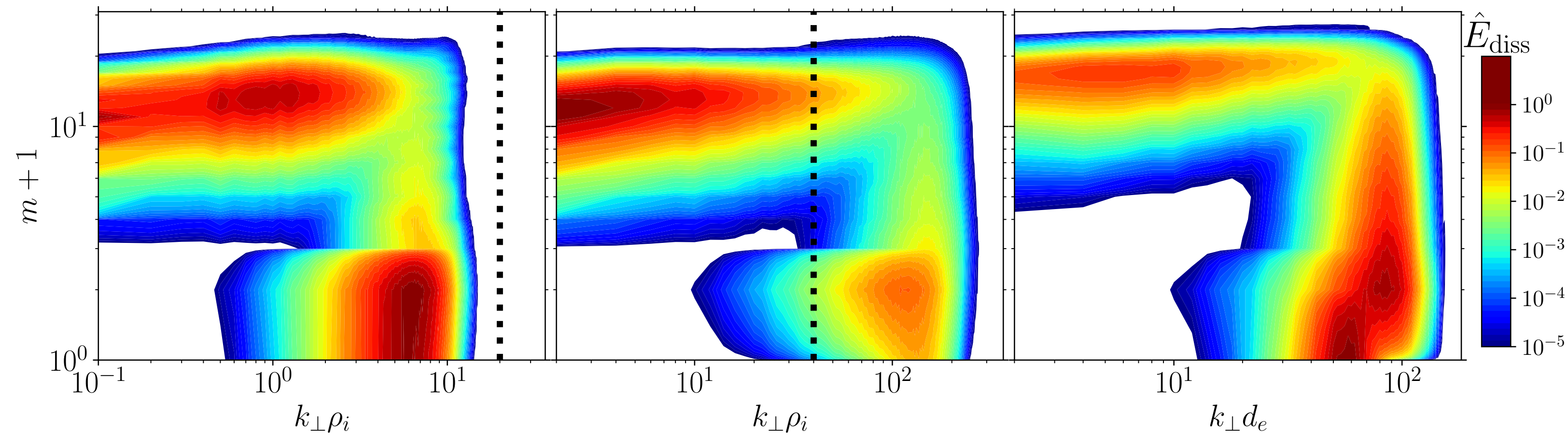
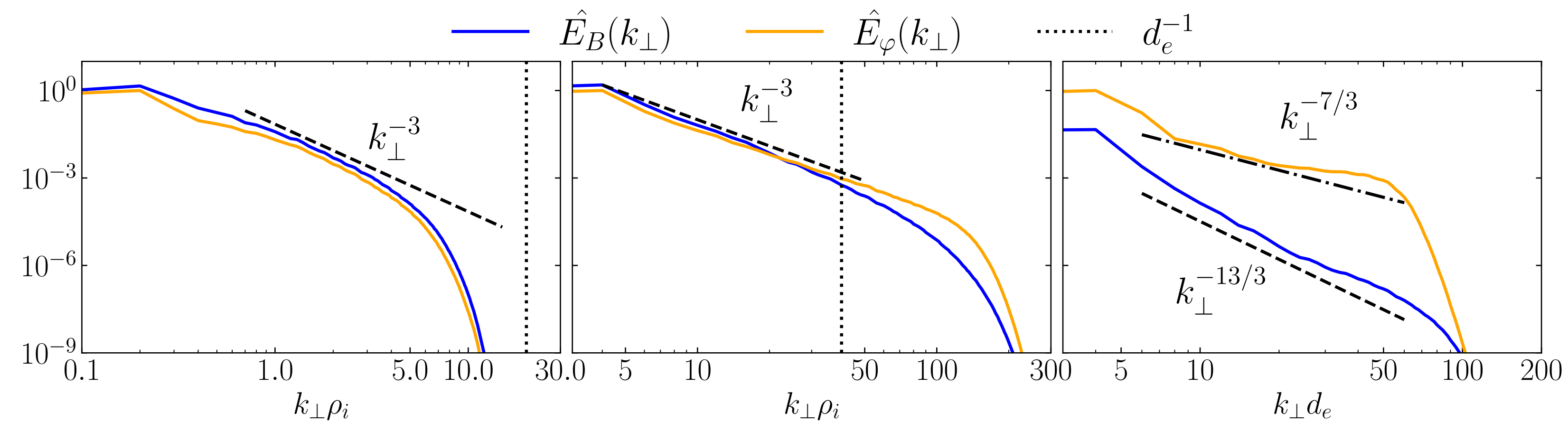
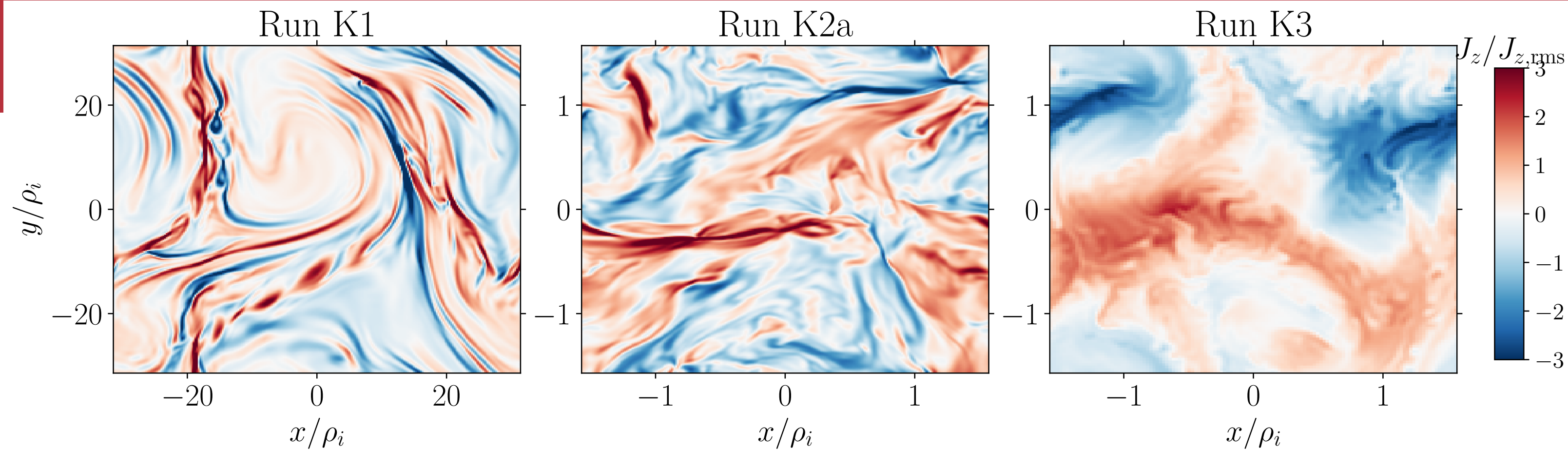
sub- ρ_i

sub- d_e



MHD to ρ_i **sub- ρ_i** **sub- d_e** In the sub- ρ_i range:spectra become steeper (than $k_{\perp}^{-8/3}$)In the sub- d_e range:

$$E_{\varphi}(k_{\perp}) \propto k_{\perp}^{-7/3}, \quad E_B(k_{\perp}) \propto k_{\perp}^{-13/3}.$$

MHD to ρ_i **sub- ρ_i** **sub- d_e** 

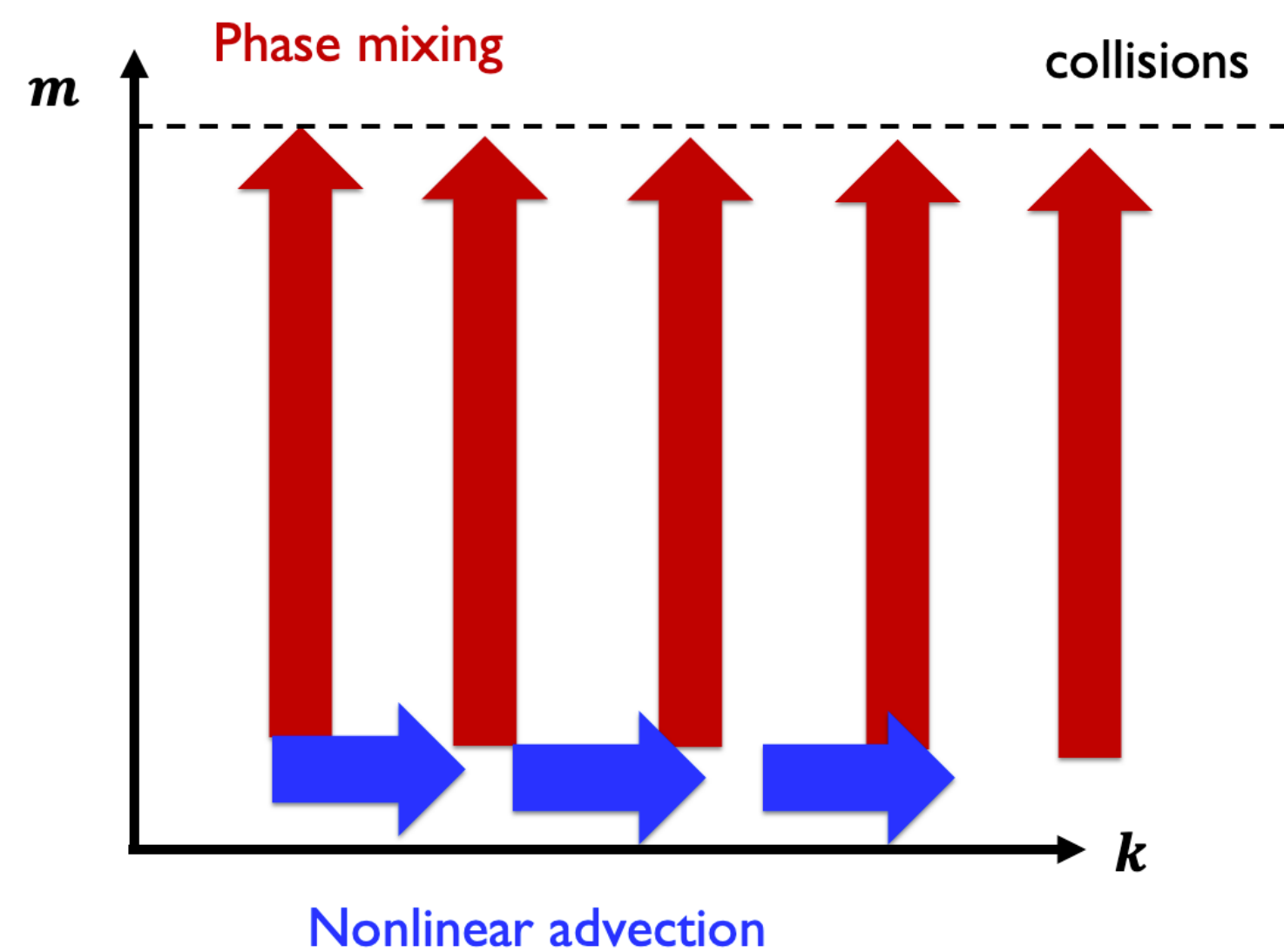
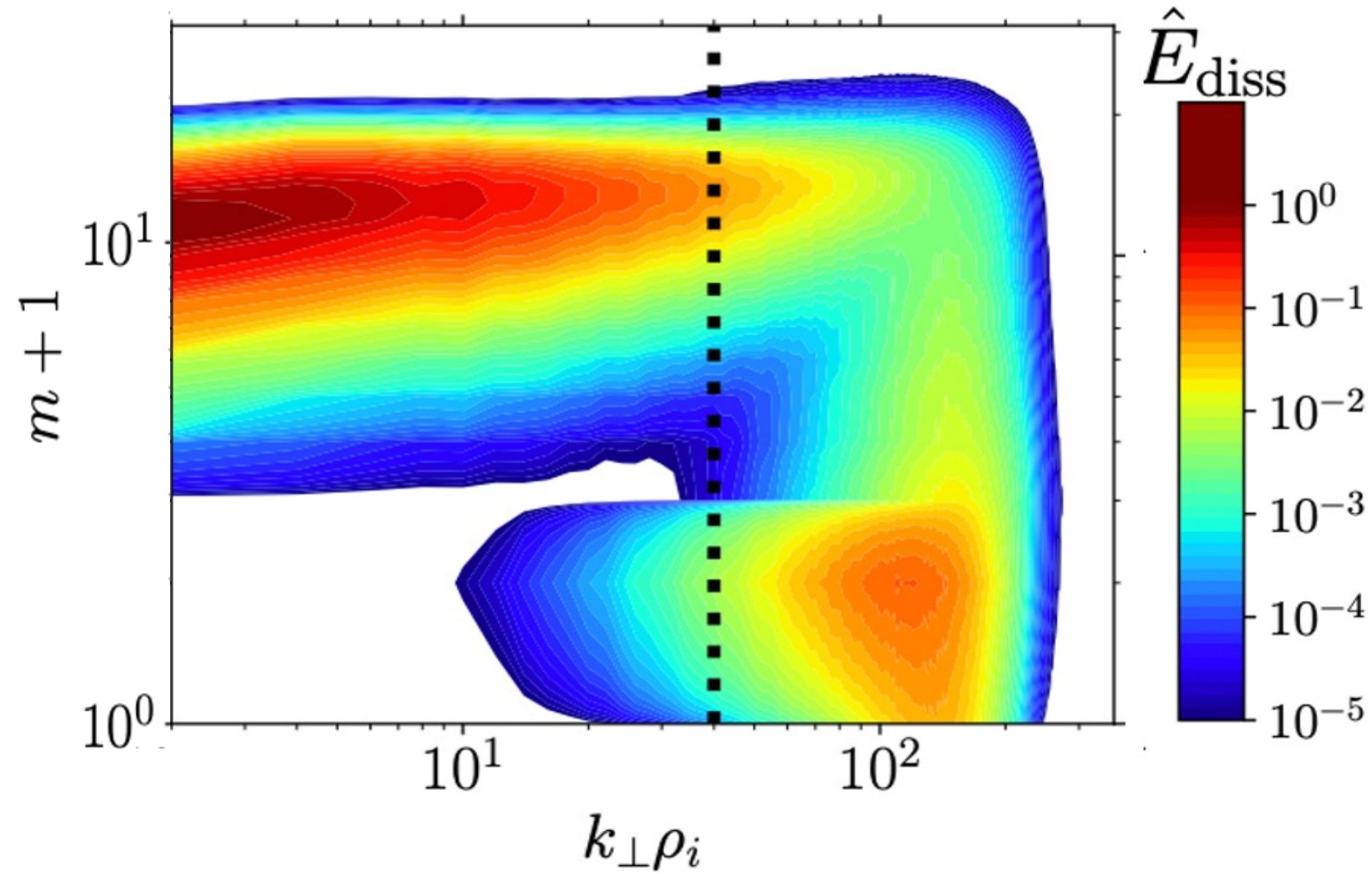
High- m dissipation turns on at ρ_i .

In the range $\rho_i < \lambda < d_e$, the “kinetic dissipation” dominates.

In the range $d_e > \lambda$, the “fluid dissipation” dominates.

Landau damped EM energy matches electron heating

sub- ρ_i turbulence

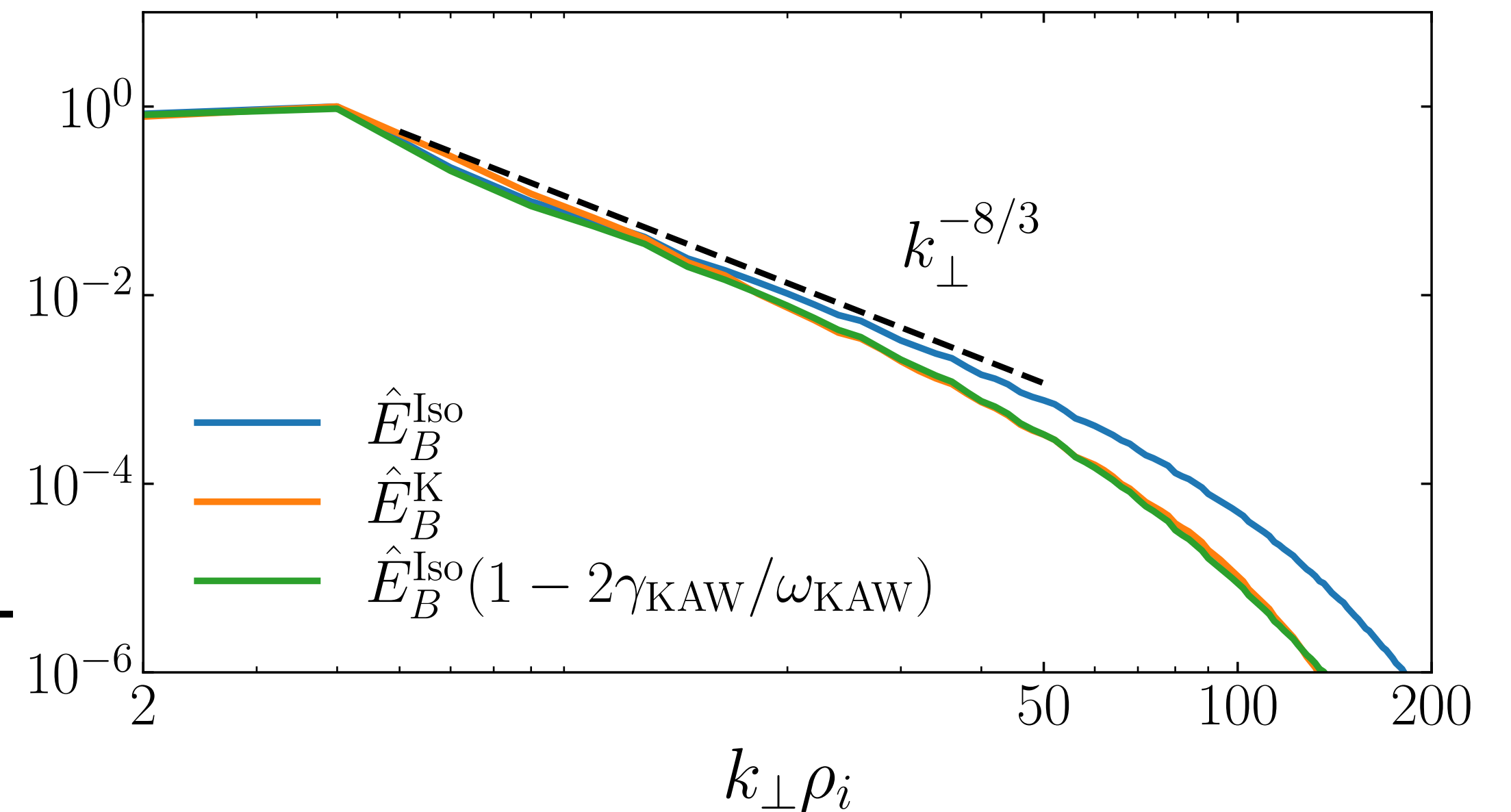


EM fluctuations are Landau-damped at each scale independently \rightarrow phase mixing domination

From the linear dispersion relation of KAWs: damping rate γ_{KAW} and frequency ω_{KAW}

$$\hat{E}_B^K(k_{\perp}) \approx \hat{E}_B^{\text{iso}}(k_{\perp}) \left(1 - 2\gamma_{KAW}/\omega_{KAW}\right).$$

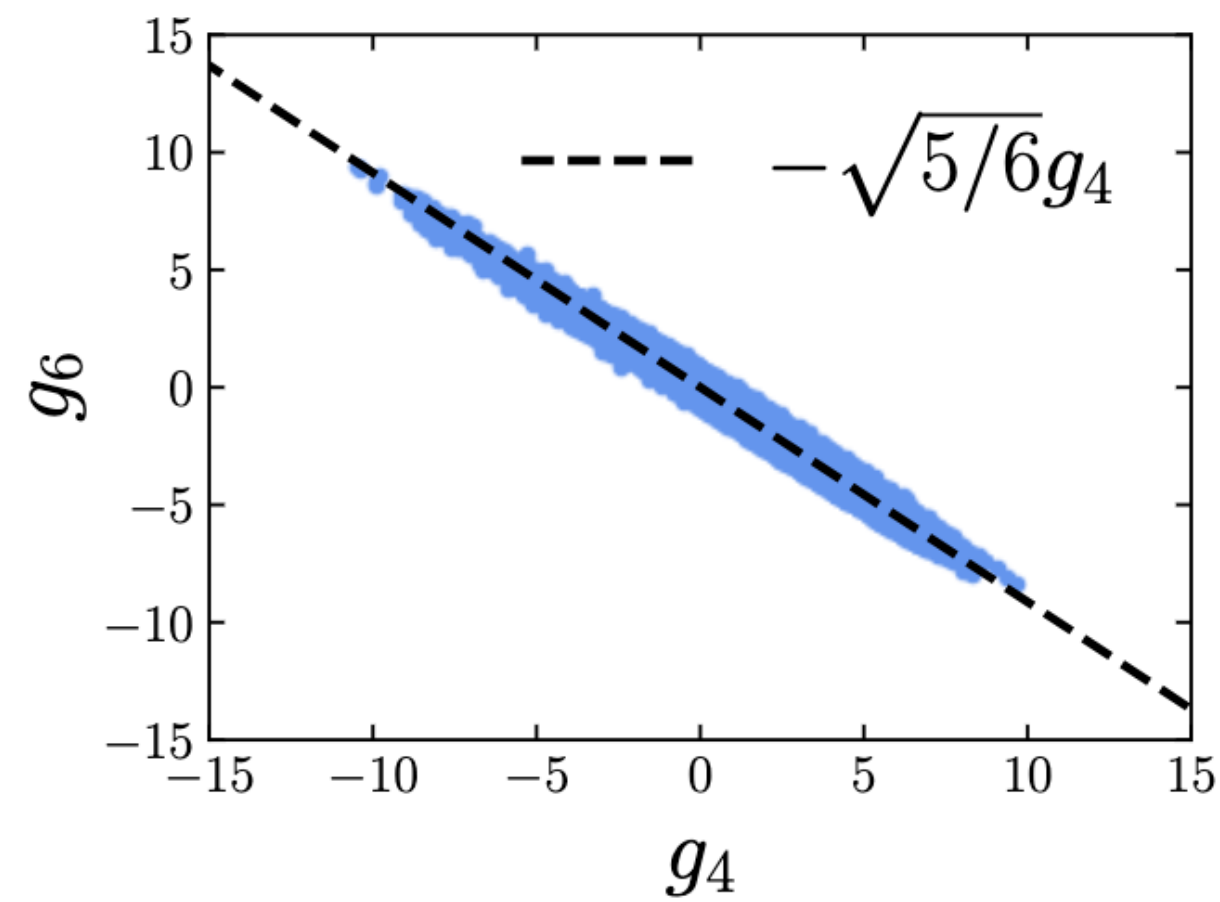
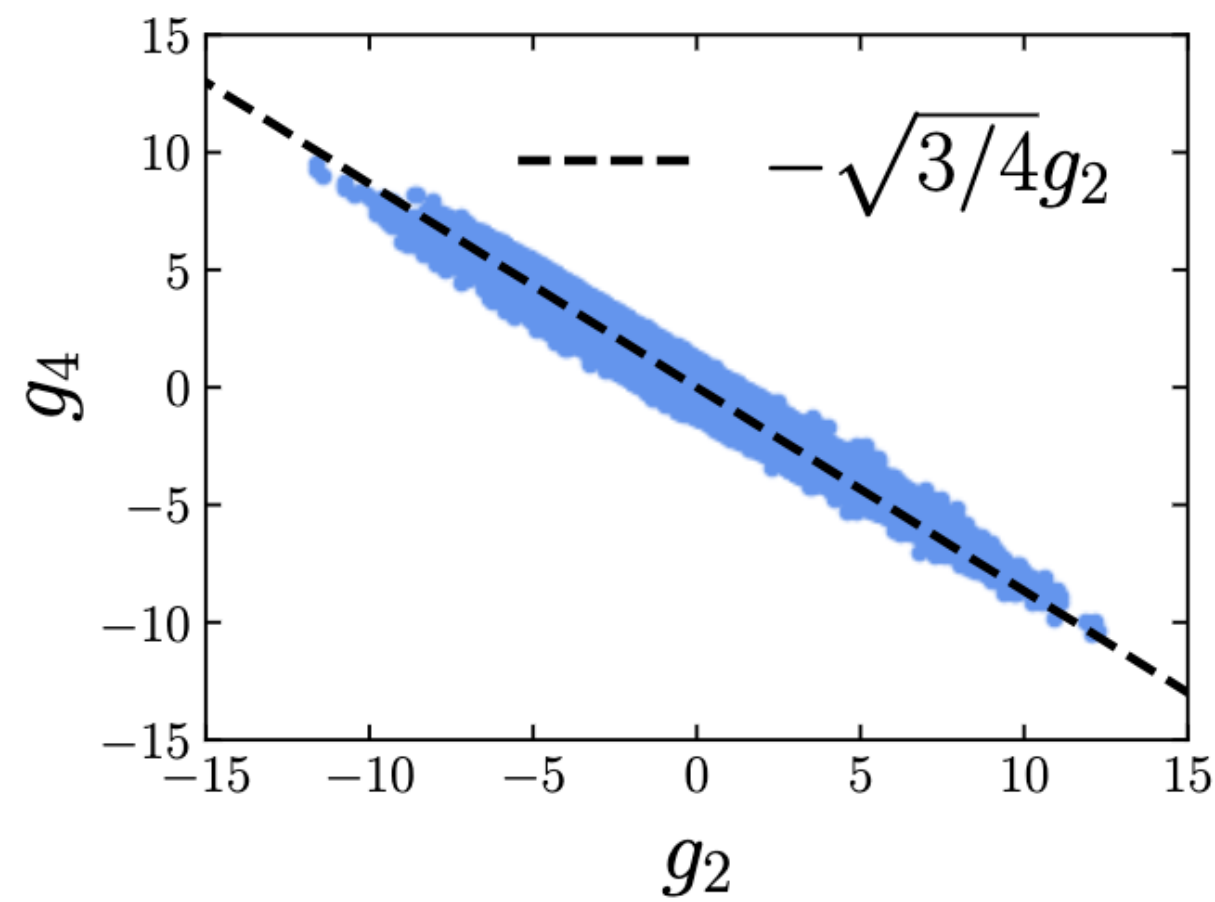
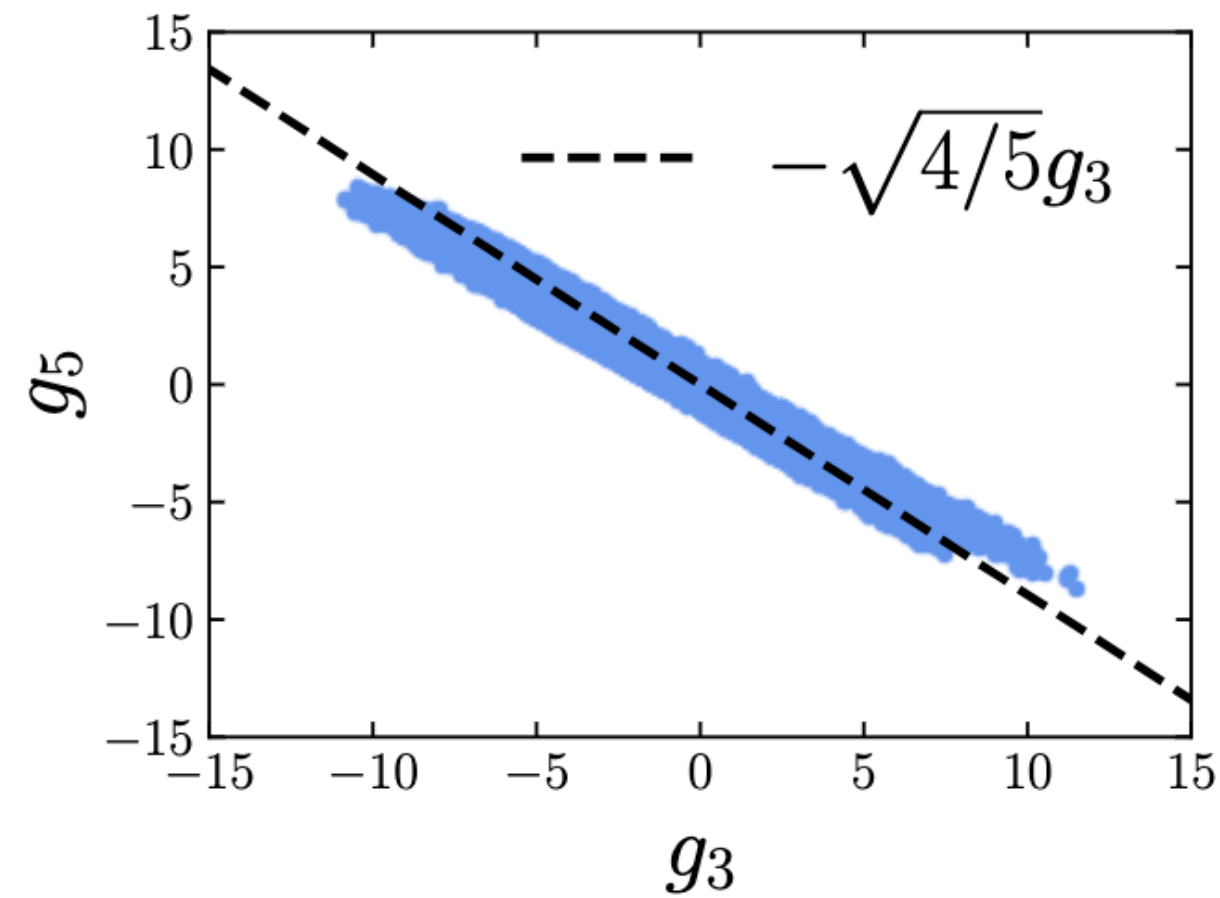
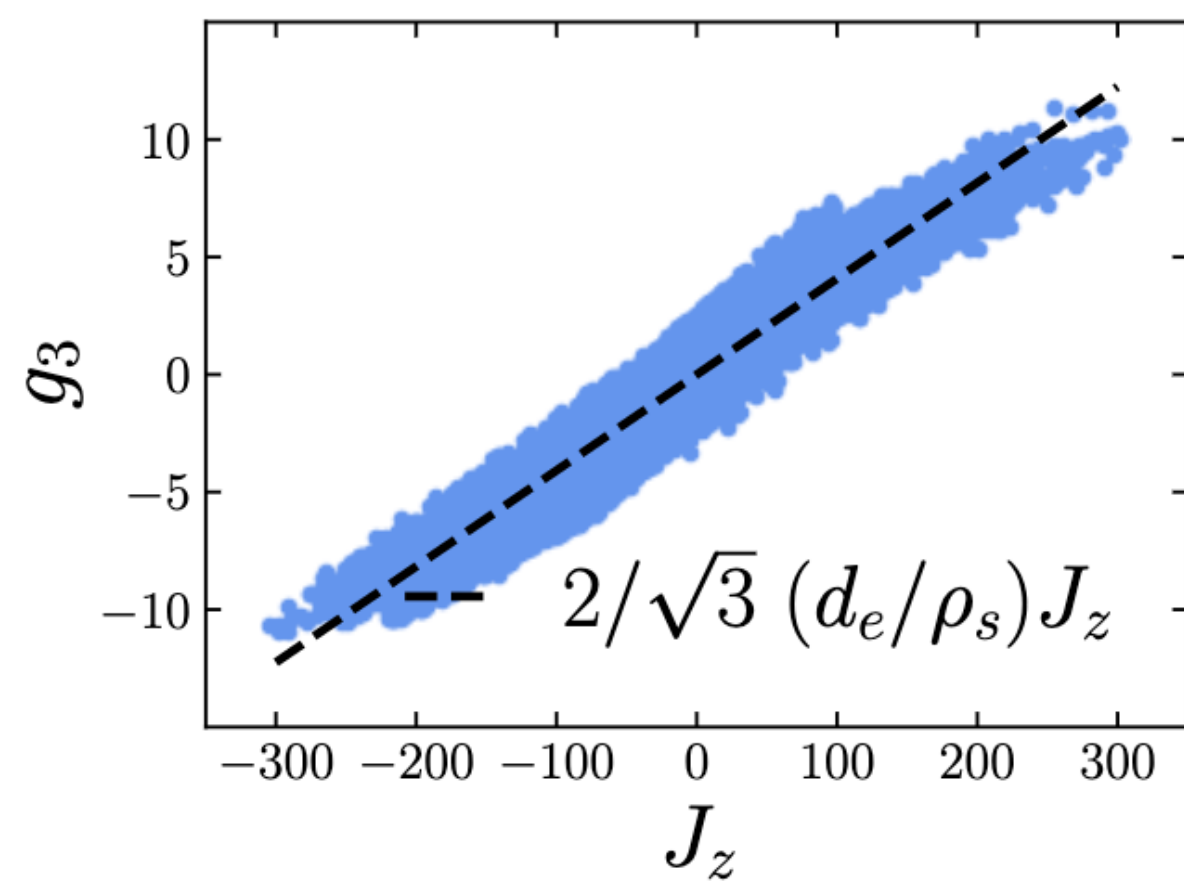
\uparrow
 $\sim \gamma_{nl}$ (critical balance)



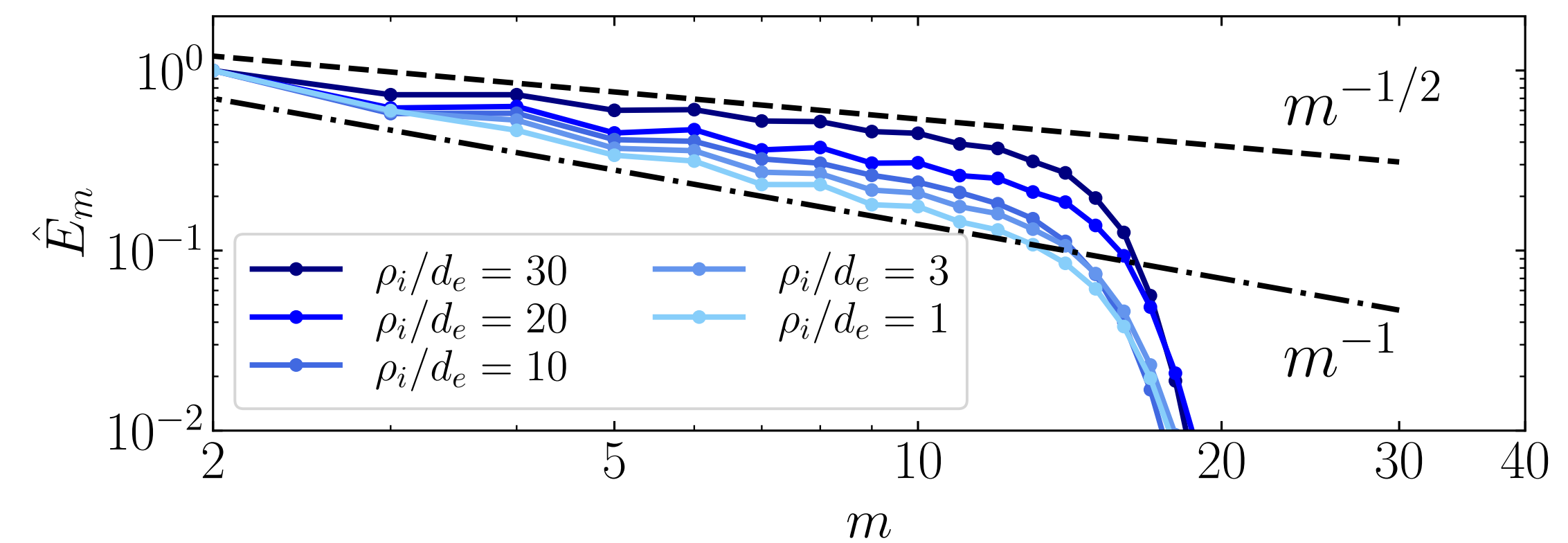
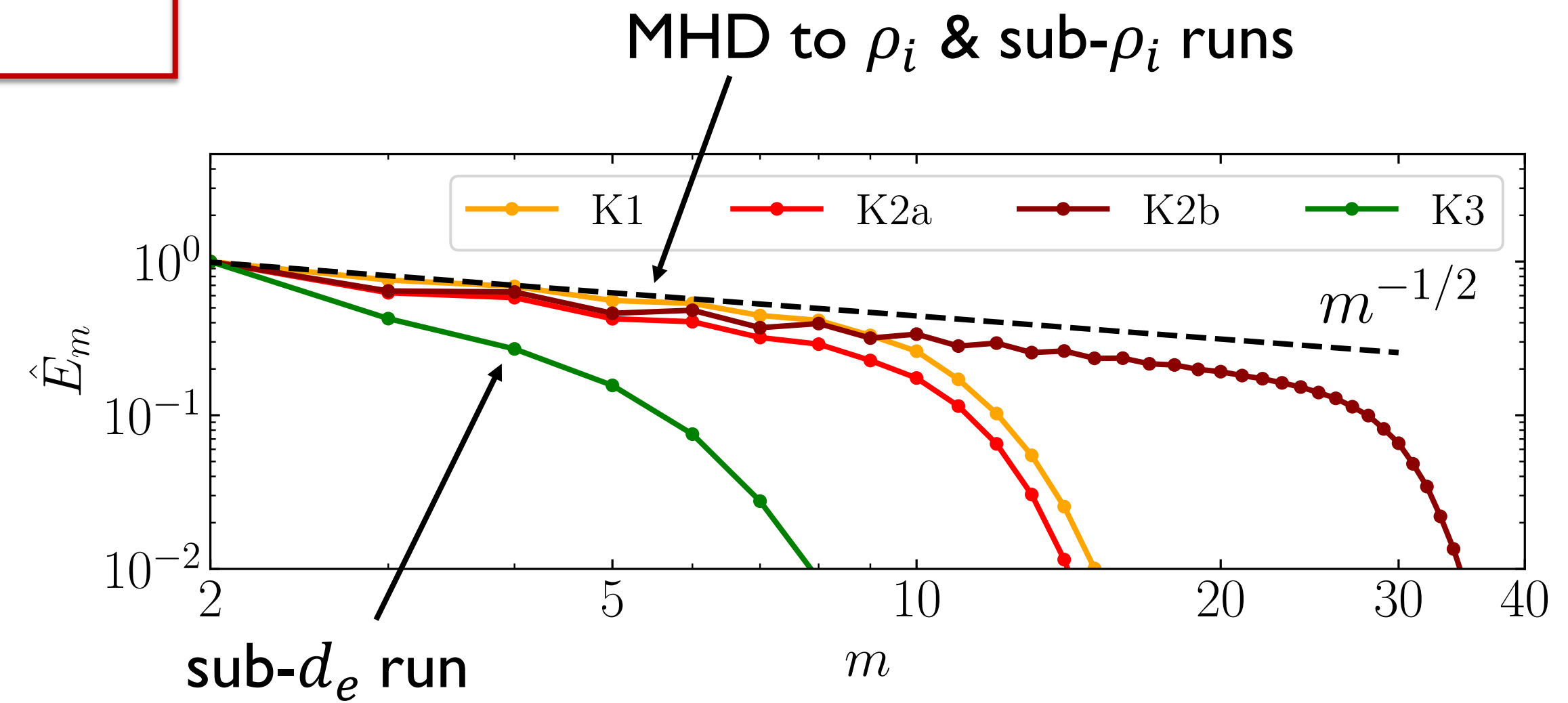
A zeroth-order solution of g_e in the velocity space and its Hermite spectrum

$$g_{m+1} = -\sqrt{m/(m+1)}g_{m-1} \quad \text{for } m \geq 3, \text{ and}$$

$$g_3 = -\sqrt{2/3} (\rho_s/d_e) J_{\parallel}$$



Velocity-space spectrum:



With kinetic electrons --- Phase space cascade and electron heating

Assuming φ and A_{\parallel} have the same configuration/gradients

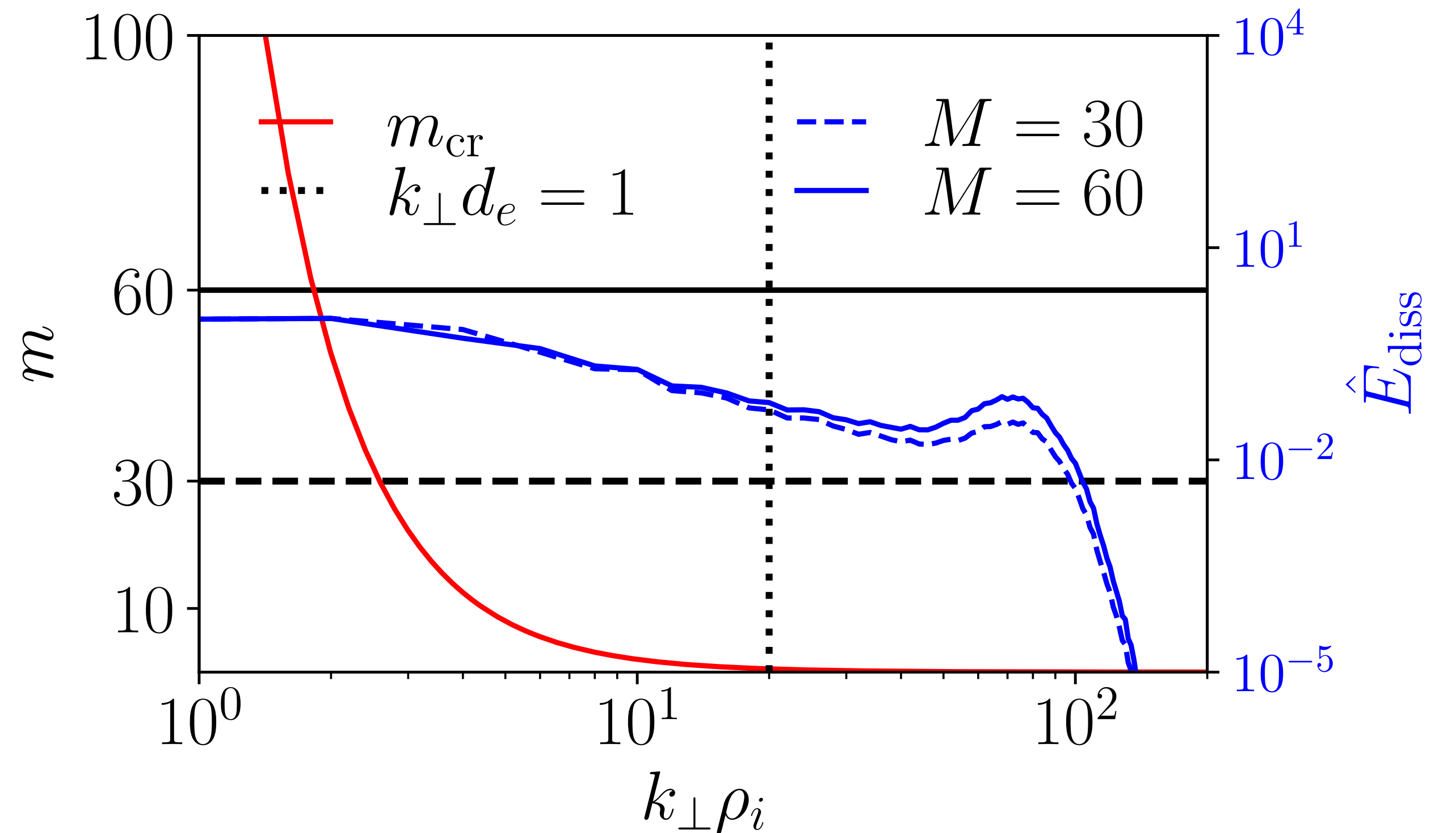
At each scale λ , there is a critical Hermite order m_{cr} :

Nonlinear advection rate \sim Phase mixing rate

$$\frac{c}{B_0} \{\varphi, g_{m_{cr}}\} \sim \frac{v_{the}}{B_0} \{A_{\parallel}, g_{m_{cr}}\} / \sqrt{m_{cr}}$$

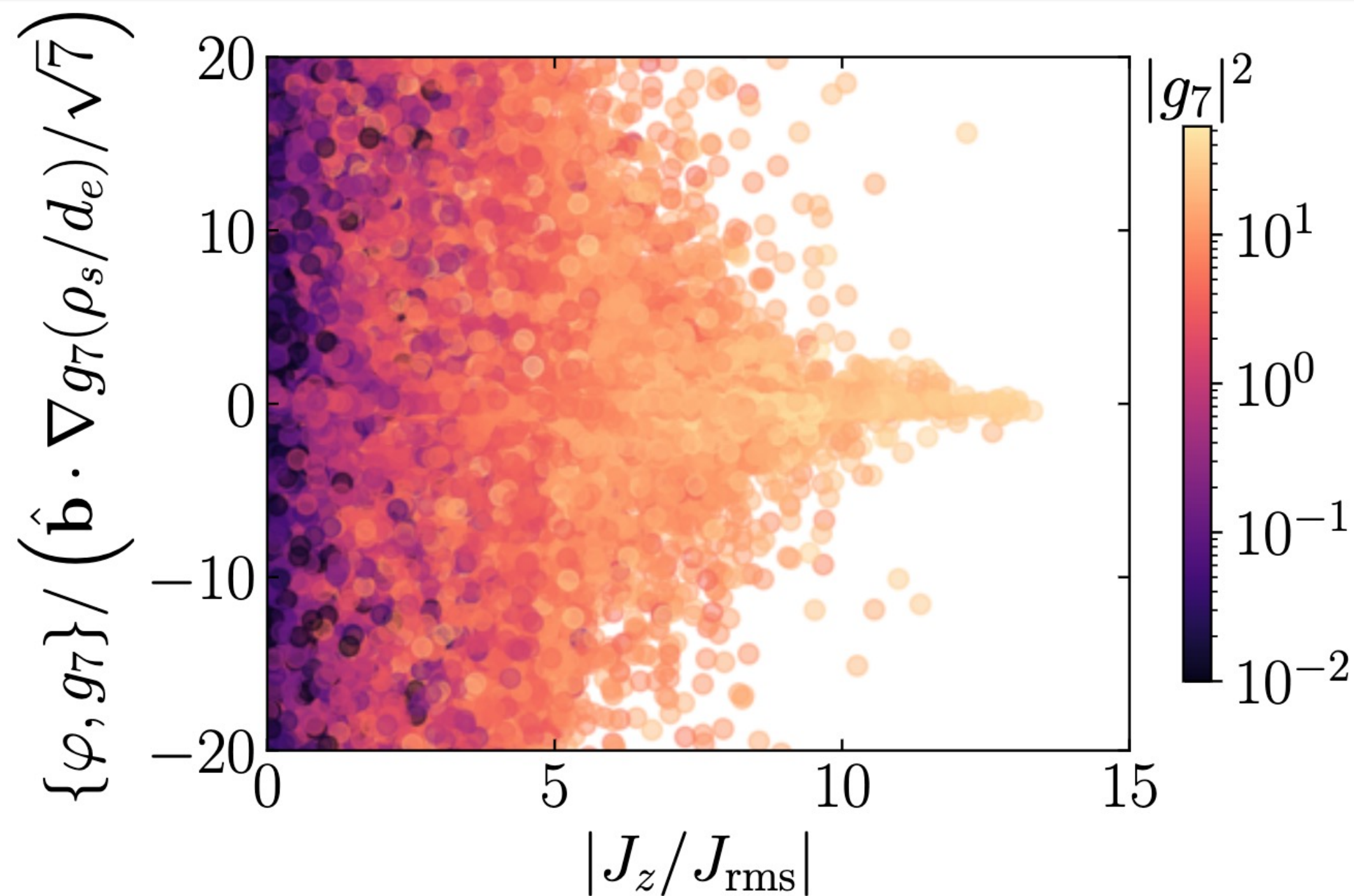
$$m_{cr}(\lambda) \sim (\lambda/d_e)^2 / (2\tau^2)$$

For both cases, there is a sufficiently wide dynamical range that echo could happen.



Local weakening of nonlinearity around current sheets enables strong phase mixing

$$g_{m+1} = -\sqrt{m/(m+1)}g_{m-1} \quad \text{for } m \geq 3, \text{ and}$$
$$g_3 = -\sqrt{2/3} (\rho_s/d_e)J_{\parallel}$$

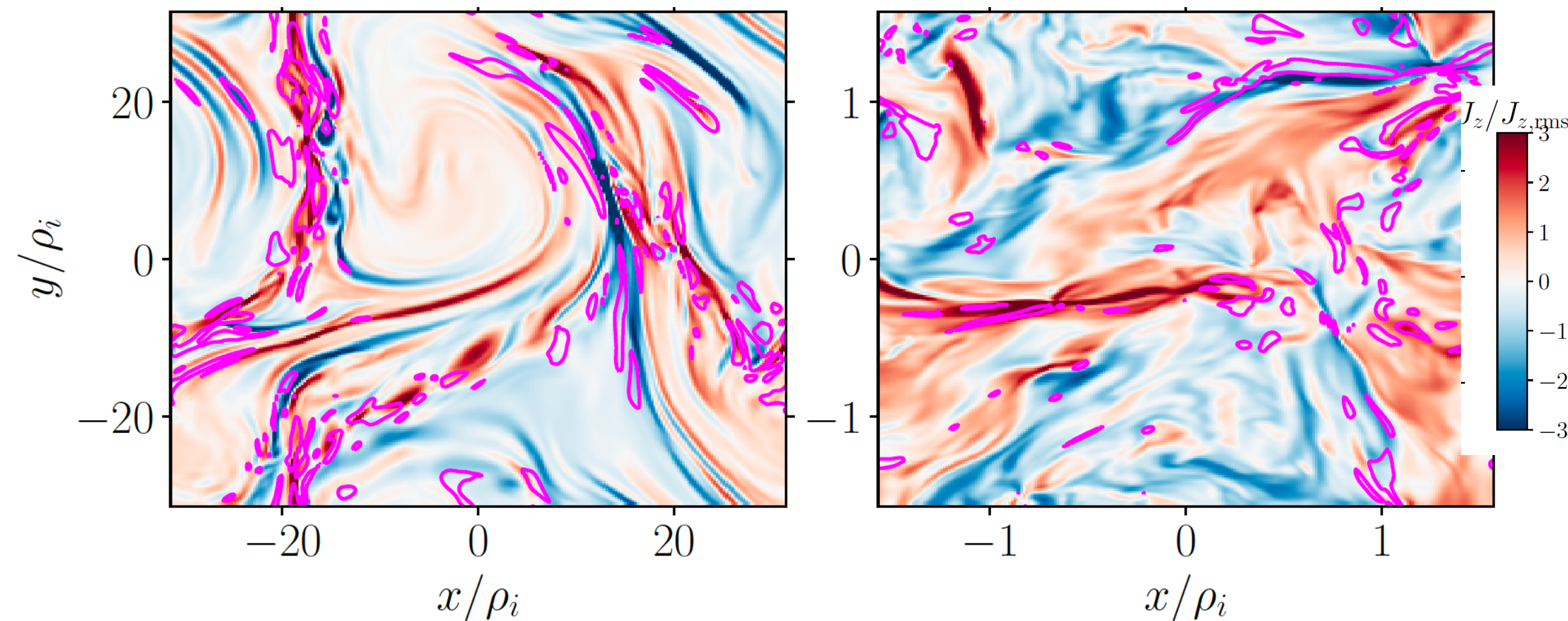
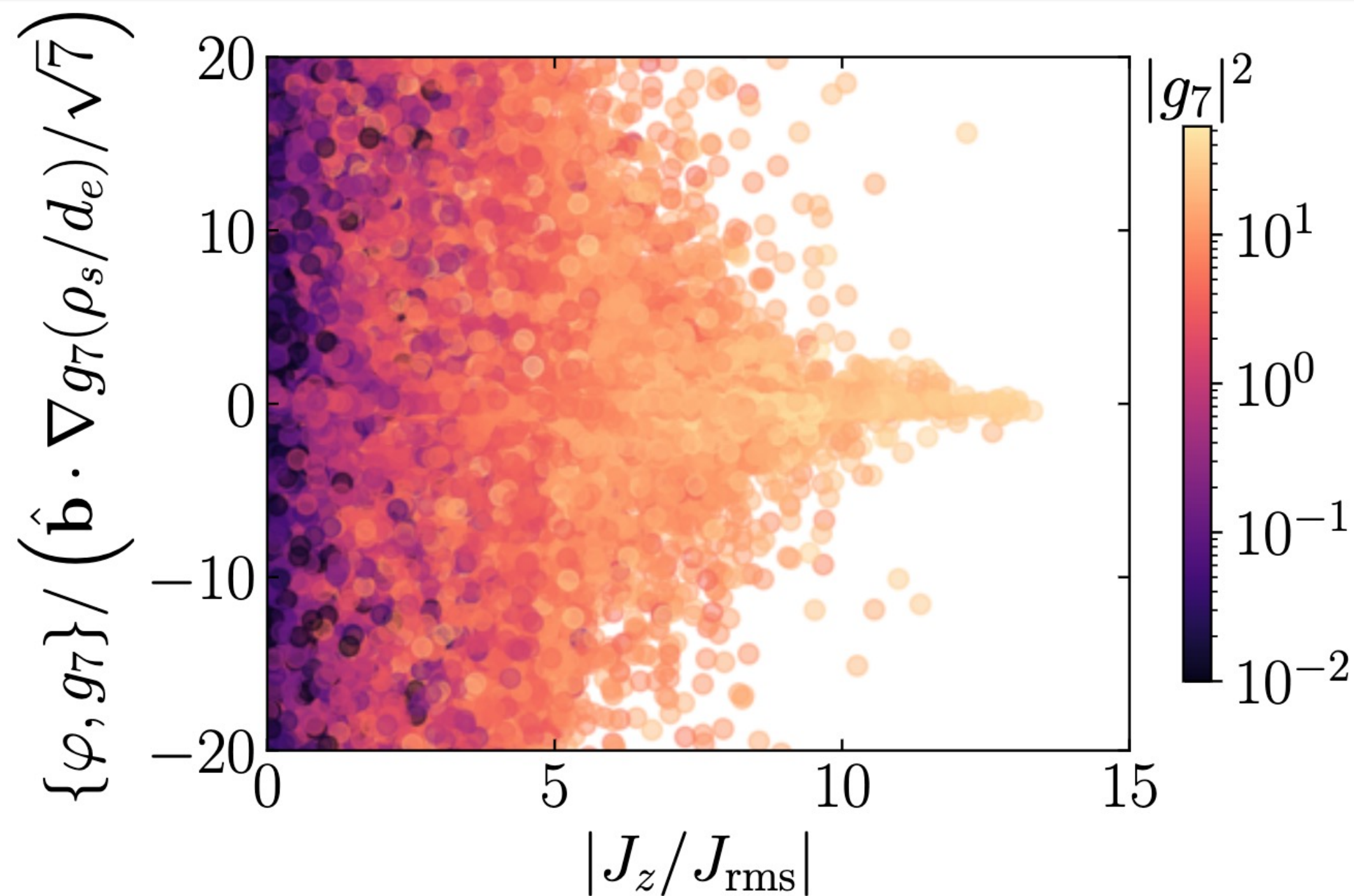


The ratio of the nonlinear-advection rate to phase-mixing rate as a function of normalized current density. The positions with large energy density of g_m (with **strong current** density) have **locally weakened nonlinearity**.

Heating occurs around current sheets

$$g_{m+1} = -\sqrt{m/(m+1)}g_{m-1} \quad \text{for } m \geq 3, \text{ and}$$

$$g_3 = -\sqrt{2/3} (\rho_s/d_e)J_{\parallel}$$



Magenta contours indicates regions with strong collisional dissipation.

The ratio of the nonlinear-advection rate to phase-mixing rate as a function of normalized current density. The positions with large energy density of g_m (with **strong current** density) have **locally weakened nonlinearity**.

We study the kinetic turbulence in the **low- β limit**, composed of KAWs.

In this specific regime:

- The magnetic and density **energy spectra** in kinetic turbulence is set by **intermittency**.
- The **kinetic channel** (via phase mixing) of energy dissipates dominates the fluid channel, energy dissipated at small scales in velocity space.
- **Electron heating** is caused by **Landau damping of KAWs** in this regime.
- Energy dissipation/electron heating occurs mostly around **current sheets**, due to the **local weakening of nonlinearity**.