Basic Thermodynamics

Handout 5

Thermodynamics potentials

Define the **enthalpy** H = U + PV

Define the **Helmholtz function** F = U - TS (sometimes called Helmholtz free energy)

Define the **Gibbs function** G = H - TS (sometimes called the Gibbs free energy).

These are all functions of state, so that one can write down the following exact differentials:

$$dU = TdS - pdV$$

$$dH = TdS + Vdp$$

$$dF = -SdT - pdV$$

$$dG = -SdT + Vdp$$

Note that each thermodynamic potential has a pair of independent variables:

$$U = U(S, V);$$
 $H = H(S, p);$ $F = F(T, V);$ $G = G(T, p)$

These can be used to immediately write down various expressions such as

$$S = -\left(\frac{\partial F}{\partial T}\right)_V, \qquad p = -\left(\frac{\partial F}{\partial V}\right)_T$$

This can be used to derive expressions such as:

$$U = F + TS = F - T \left(\frac{\partial F}{\partial T}\right)_{V} = -T^{2} \left(\frac{\partial}{\partial T}\right)_{V} \frac{F}{T}$$

Thermodynamic equilibrium

Consider a p–V system in contact with a large reservoir which is in equilibrium at temperature T_0 and pressure p_0 . The **availability** is defined by

$$A = U - T_0 S + p_0 V \tag{1}$$

The equilibrium state of the system is achieved by minimizing A.

For the following particular cases, minimizing A corresponds to

- \bullet system is thermally isolated and has fixed V maximize S
- ullet system has fixed T and V minimize F
- system has fixed T and p minimize G

 $\begin{array}{c} {\rm ATB} \\ {\rm Michaelmas} \ 2012 \end{array}$