

# Group Theory for Graduates

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## 1 Basic Concepts

Group axioms Generators Cosets & classes Representations Equivalent representations Generation of inequivalent representations Irreducible representations

## 2 Schur's lemmas and orthogonality relations

Orthogonality relations; characters of representations; reduction of representations; the regular representation; reduction of a direct product representation.

## 3 Applications to quantum mechanics

Function spaces; commuting observables; dynamical symmetries; two-particle states & Clebsch-Gordon coefficients; Wigner-Eckart theorem.

## 4 Important Lie Groups

$\mathcal{R}^3$ ;  $\mathcal{R}(3)$ ;  $GL(n, \mathcal{R})$ ;  $SL(n, \mathcal{R})$ ;  $SL(2, \mathcal{C})$ ;  $\mathcal{O}(n)$ ;  $SO(n)$ ;  $U(n)$ ;  $SU(n)$ .

## 5 General theory of Lie Groups

Summary of the theory; proof of key results; concrete calculations.

## 6 Infinitesimal generators

The Lie algebra  $\Lambda(\mathcal{R}(3))$ ; the Lie algebra  $\Lambda(SU(2))$  the Lie algebra  $\Lambda(SU(3))$

## 7 Representations of Lie groups

Representations of  $\Lambda(SU(2)) = \Lambda(\mathcal{R}(3))$ ; characters of the  $D^{(j)}$  irreps; integration over a Lie group; Casimir operators.

## 8 Representations of $SU(3)$

Quarks and  $SU(3)$ ; Young's tableaux; colour;

## 9 The Lorentz Groups

The Lie Algebra  $\Lambda(\mathbb{L})$ ; the Lorentz group with inversions; the Poincaré group.

Most topics are covered in either vol. 1 or vol. 2 of *Group Theory in Physics* by Elliott & Dawber (OUP).