

Renormalization-group Effects in Dark-Matter Direct Detection

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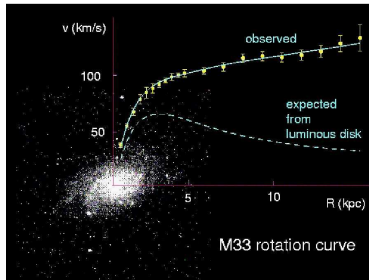


Theory Seminar, Oxford University
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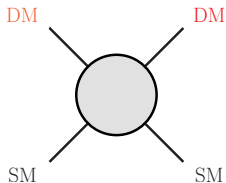
With Fady Bishara, Benjamin Grinstein, Jure Zupan – [work in progress](#)
With Aaron Gootjes-Dreesbach, Maximilian Reininghaus – [work in progress](#)

Dark Matter Facts

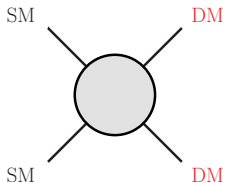
- DM exists
 - All evidence via its gravitation
- Particle nature?
- What we know about DM
 - DM is non-baryonic, cold, and neutral
 - Relic abundance $\Omega_{\text{DM}} h^2 = 0.1198(26)$
[PLANCK / PDG 2014]
- Thermal history motivates interaction with SM



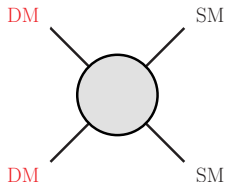
Three roads to discovery



Direct detection

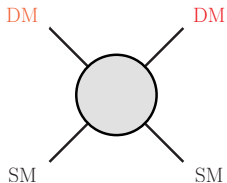


Collider searches

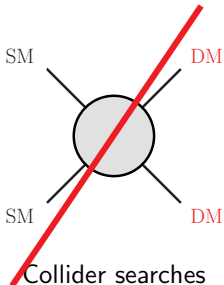


Indirect detection

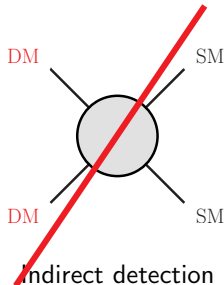
Three roads to discovery



Direct detection



Collider searches



Indirect detection

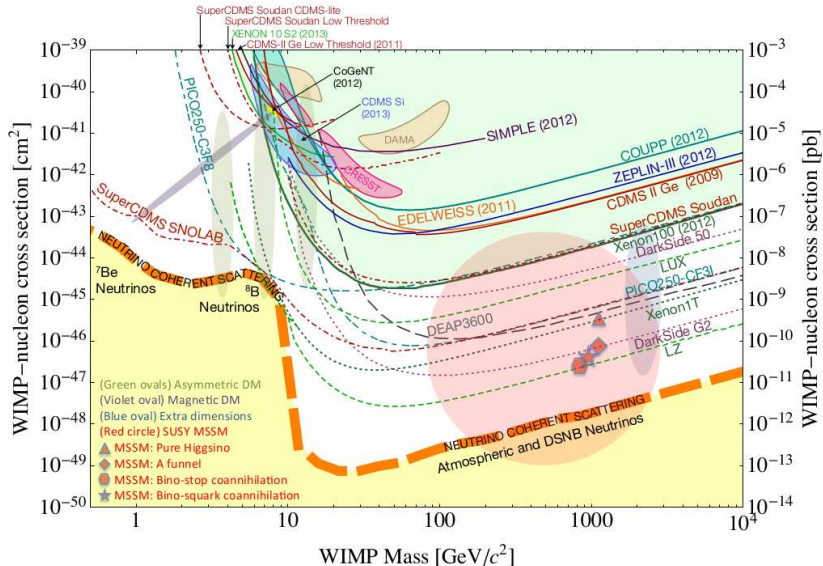
Direct Detection Basics

- Direct detection – scattering on nuclei
 - Complementary information, proves cosmological lifetime
 - Assume velocity distribution (Maxwell); $v \sim 10^{-3}$
 - Maximal momentum transfer is $q \lesssim 200 \text{ MeV}$

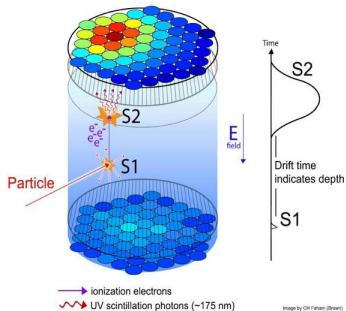
$$\frac{dR}{dE_R} = \frac{\rho_0}{m_A m_\chi} \int_{v_{min}} dv v f_1(v) \frac{d\sigma}{dE_R}(v, E_R).$$

[Lewin & Smith, *Astropart.Phys.*6 (1996)]

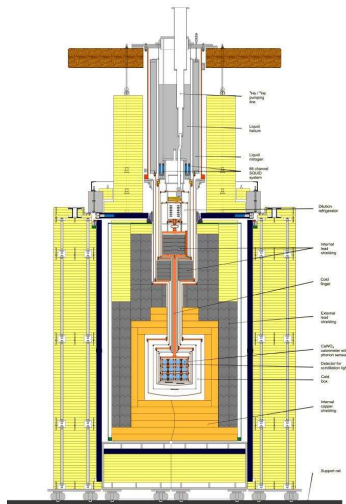
Direct Detection Limits



Direct Detection Experiments

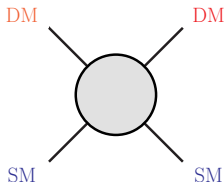


LUX



CRESST

Direct Detection



- What is the meaning of “SM”?
 - Write models at high energies – $SM \equiv Q_L, q_R, L_L, \ell_R, g, \dots$
 - Scattering nonrelativistic, at very low energies – $SM \equiv p, n, (\pi,) \dots$
- Use appropriate EFT (effective theory)
- UV operators have **characteristic behaviour in the nonrelativistic limit**

Nonrelativistic limit

- Traditionally, consider point-like nucleus (+ form factor)
 - “spin independent” vs. “**spin dependent**” scattering
 - **momentum / velocity - suppressed** interactions

- NR limit of SM currents

- Axial vector: $\bar{p}\gamma^\mu\gamma_5 p \rightsquigarrow \Psi_p^\dagger\left(\frac{\vec{q}\cdot\vec{S}_p}{m_N}, 2\vec{S}_p\right)\Psi_p$

- Vector: $\bar{p}\gamma^\mu p \rightsquigarrow \Psi_p^\dagger\left(1, \frac{\vec{q}}{2m_N} - i\frac{\vec{q}\times\vec{S}_p}{m_N}\right)\Psi_p$

- NR limit of DM currents

- Axial vector: $\bar{\chi}\gamma^\mu\gamma_5\chi \rightsquigarrow \Psi_\chi^\dagger\left(\vec{v}^\perp\cdot\vec{S}_\chi + \frac{\vec{q}\cdot\vec{S}_\chi}{2m_N}, \vec{S}_\chi\right)\Psi_\chi$

- Vector: $\bar{\chi}\gamma^\mu\chi \rightsquigarrow \Psi_\chi^\dagger\left(1, \vec{v}^\perp + \frac{\vec{q}}{2m_N} + i\frac{\vec{q}\times\vec{S}_\chi}{m_\chi}\right)\Psi_\chi$

- For extended nucleus, have six basic nuclear responses

[Fitzpatrick et al., 1203.3542]

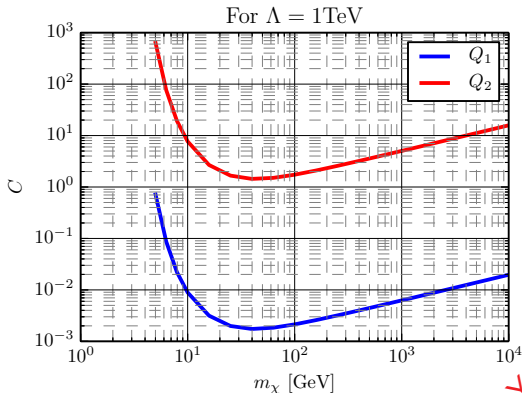
Velocity Suppression

- Recall DM velocity
 $v \sim 10^{-3}$

- Example:

- $Q_1 = (\bar{\chi}\gamma_\mu\chi)(\bar{q}\gamma^\mu q)$
not suppressed

- $Q_2 = (\bar{\chi}\gamma_\mu\gamma_5\chi)(\bar{q}\gamma^\mu q)$
velocity suppressed



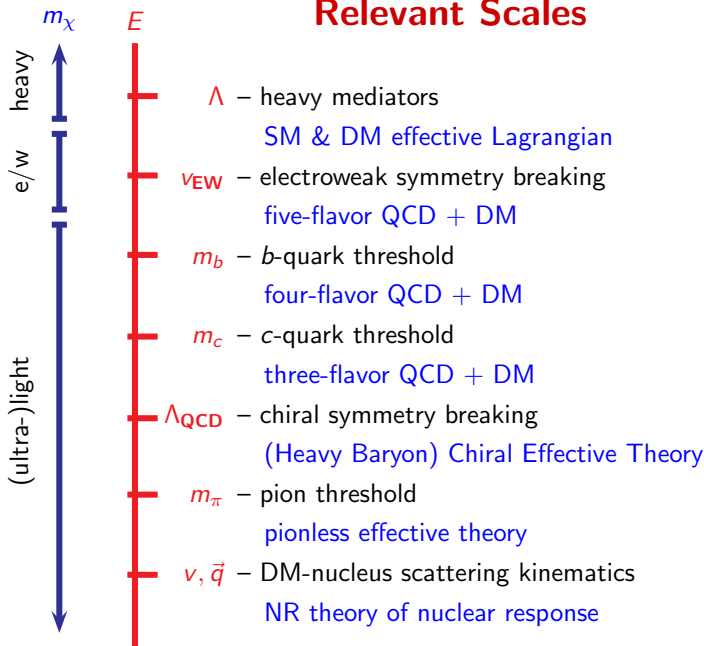
[Data from LUX collaboration, 1310.8214]

PRELIMINARY

Why complete EFT?

- A complete EFT framework for all scales is needed for the consistent interpretation of direct detection data.
 - Consistent power counting
 - Connect all scales from the UV to the atomic nuclei
 - Keep dependence on UV physics explicit

Relevant Scales



Why mixing effects?

- Momentum-dependent interactions are **leading** in many UV models
- Electroweak loops can **mix suppressed and unsuppressed operators**
[Freytsis & Ligeti, 1012.5317; see also Haisch et al. 1302.4454; Crivellin et al. 1402.1173, 1408.5046; D'Eramo et al. 1409.2893]
 - Calculate **all relevant radiative corrections**

The setup

- Assume DM is an **electroweak multiplet** χ , with $m_\chi \sim v_{\text{ew}}$
 - Here, DM is a Dirac fermion
- Several examples:
 - Neutralinos in the MSSM (bino, higgsino, wino)
 - Minimal Dark Matter [Cirelli et al. hep-ph/0512090, ...]
 - “Technibaryons” [Nussinov, Phys.Lett. B165 (1985) 55, ...]
- **Potential mediators** ϕ , integrated out at $\Lambda \sim m_\phi \gg m_\chi$
 - Dim.4 gauge interactions
 - Higher-dimensional effective operators

Effective Lagrangian above v_{EW}

- Construct operators in unbroken e/w phase

$$\mathcal{L}^{\text{eff}} = \mathcal{L}^{\text{SM}} + \mathcal{L}^{\text{DM}} + \sum \frac{C_j^{(5)}}{\Lambda} Q_j^{(5)} + \sum \frac{C_j^{(6)}}{\Lambda^2} Q_j^{(6)} + \dots$$

- Expansion in inverse mediator mass Λ
- Generalizes “SM-EFT” [Buchmüller et al. 1986, Grzadkowski et al. 2010]

Mixing – General Structure

- RGE (Renormalization Group Equations):

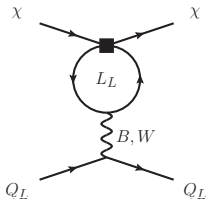
$$\frac{d}{d \log \mu} C(\mu) = \gamma^T C(\mu)$$

- Do we need to sum the logs?

- $\alpha_1(\mu_{EW}) \approx 0.01$, $\alpha_2(\mu_{EW}) \approx 0.03$, $\alpha_\lambda(\mu_{EW}) \approx 0.04$, $\alpha_t(\mu_{EW}) \approx 0.08$
- No – would need $\Lambda \sim 10^4$ TeV

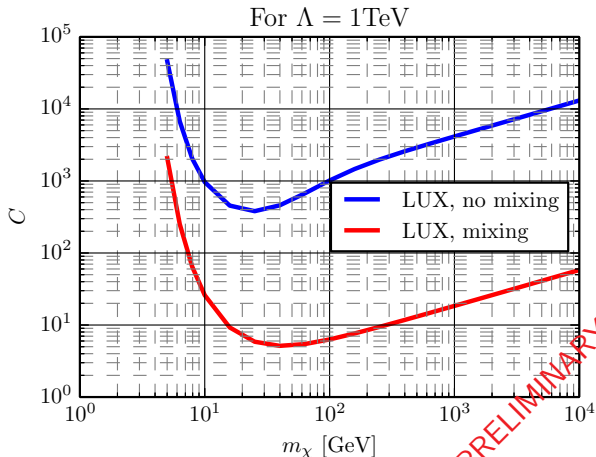
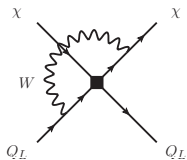
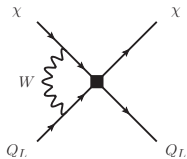
- Importance of RGE:

- Mixing of suppressed and unsuppressed operators
- Penguin insertions mix lepton and quark operators



Mixing Example – W Exchange

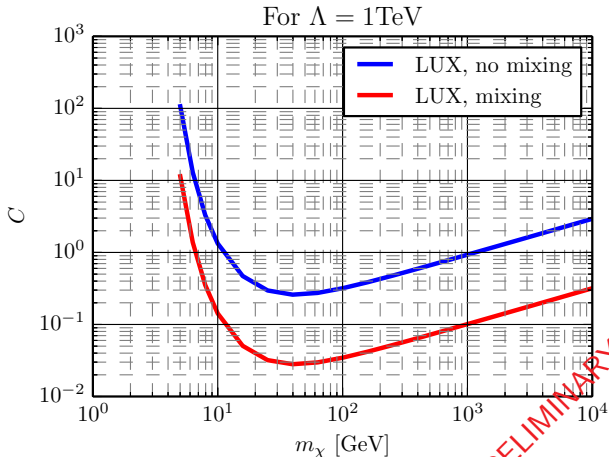
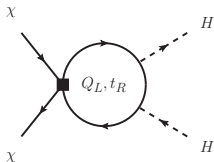
$$(\bar{\chi}\gamma_{\mu}\gamma_5\chi)(\bar{Q}_L^i\gamma^{\mu}Q_L^i) \quad \Rightarrow \quad (\bar{\chi}\gamma_{\mu}\tilde{\tau}^a\chi)(\bar{Q}_L^i\gamma^{\mu}\tau^a Q_L^i),$$



PRELIMINARY

Mixing Example – top Yukawa

$$(\bar{\chi}\gamma_{\mu}\chi)(\bar{u}_R^i\gamma^{\mu}u_R^i) - (\bar{\chi}\gamma_{\mu}\chi)(\bar{Q}_L^i\gamma^{\mu}Q_L^i) \Rightarrow (\bar{\chi}\gamma^{\mu}\chi)(H^{\dagger}i\overleftrightarrow{D}_{\mu}H)$$



[See also Crivellin et al., 1402.1173]

PRELIMINARY

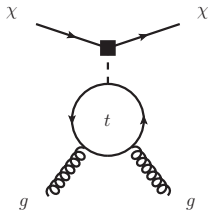
Effective Lagrangian below v_{EW}

- E/w symmetry breaking introduces a new scale v_{EW}
- Now have double expansion in $1/\Lambda$ and $1/v_{EW}$

$$\mathcal{L}^{\text{eff}} = \mathcal{L}^{(4)}|_{n_f} + \mathcal{L}^{\text{DM}}|_{n_f} + \sum \hat{\mathcal{C}}_j^{(5)}|_{n_f} Q_j^{(5)} + \sum \hat{\mathcal{C}}_j^{(6)}|_{n_f} Q_j^{(6)} + \sum \hat{\mathcal{C}}_j^{(7)}|_{n_f} Q_j^{(7)} + \dots$$

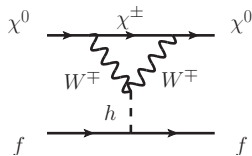
$$\hat{\mathcal{C}}_a^{(d)}|_{n_f} = \sum_n \frac{\mathcal{C}_a^{(d-n,n)}|_{n_f}}{\Lambda^{d-4-n} v_{EW}^n}.$$

- E.g. integrating out Higgs and top results in $Q_1^{(7)} \propto \mathcal{C}^{(5,2)}(\bar{\chi}\chi) G^{a,\mu\nu} G_{\mu\nu}^a / (\Lambda v_{EW}^2)$



Matching

- E.g. “Higgs penguin” contribution for $Y = 0$
 - $m_\chi \sim v_{\text{ew}}$: DM is “HQET” field in EFT
 - Match onto $\mathcal{Q}^{(7)} = m_f(\bar{\chi}\chi)(\bar{f}f)$
 - $x = m_\chi/M_W$

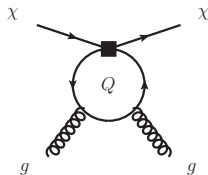
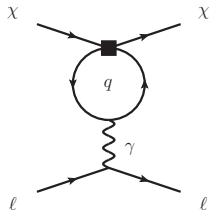


$$\mathcal{C}_{5,f}^{(4,3)} = \frac{J(J+1)}{2\pi^2 s_W^2 \lambda} \left[\frac{(2x^2 - 1) \left[5x + 2\sqrt{\frac{1+4x}{x^2}} \log \left(\frac{1}{2x} + \frac{1}{2}\sqrt{\frac{1+4x}{x^2}} \right) \right]}{4x^2 - 1} + \frac{2 \log x}{x} \right],$$

- Similar matching conditions for higher-dimensional operators

Running and Matching at Flavor Thresholds

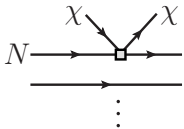
- QCD / QED running is well-known [E.g. Hill et al., 1409.8290]
- Penguin insertions will mix lepton and quark operators
- Matching at flavor thresholds



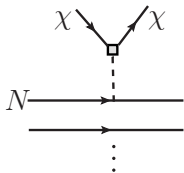
Transition to the nucleon picture

- Recall maximum momentum transfer in DM scattering is $q_{\max} \approx 200 \text{ MeV}$
- Expansion in $q/(4\pi f_\pi)$ is good to $\mathcal{O}(20\%)$
- Can use Heavy Baryon Chiral Perturbation Theory (HBChPT)
[Jenkins and Manohar, Phys.Lett. B255 (1991) 558]
 - Hadronic degrees of freedom are pions, nucleons, . . .
- Treat DM currents as $SU(3)_L \times SU(3)_R$ flavor-symmetric spurions
- Can write hadronization of quark currents explicitly, e.g.:
 - Pseudo-scalar meson current: $\bar{q}i\gamma_5 q \rightarrow -B_0 f_\pi m_u (\pi^0 + \eta/\sqrt{3}) + \dots$
 - Nuclear vector current: $\bar{u}\gamma^\mu u \rightarrow \bar{p}\gamma^\mu p, \quad \bar{d}\gamma^\mu d \rightarrow \bar{n}\gamma^\mu n, \dots$
- Describe hadronic physics in terms of few parameters (f_π, g_A, \dots)

Chiral power counting – LO



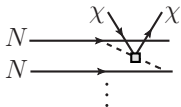
- Only leading diagram for $\bar{q}\gamma^\mu q$, $\bar{q}q$, $G_{\mu\nu}G^{\mu\nu}$, $\tilde{G}_{\mu\nu}G^{\mu\nu}$
- Leading diagram for $\bar{q}\gamma^\mu\gamma_5 q$



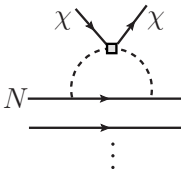
- Only leading diagram for $\bar{q}\gamma_5 q$
- Leading diagram for $\bar{q}\gamma^\mu\gamma_5 q$

Chiral power counting – beyond LO

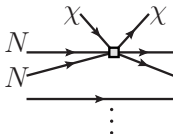
[cf. Cirigliano, Graesser, Ovanesyan 1205.2695]



- For $\bar{q}q$ scales as $\nu = \nu_{\text{LO}} + 1$



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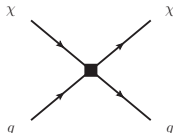
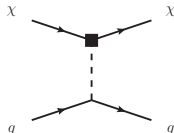
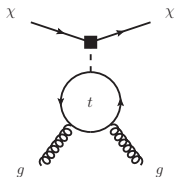


- Always scales as $\nu = \nu_{\text{LO}} + 2$

Nonrelativistic limit and nuclear matrix elements

- At $\mu \ll \Lambda_{\text{QCD}}$ transition to pionless EFT
 - Effectively introduce form factor $\propto 1/(m_\pi^2 - q^2)$
- Construct nonrelativistic, Galilean-invariant EFT for nuclear responses
[Fitzpatrick et al. 1203.3542]
- Calculation of nuclear matrix elements for all nuclear response functions (available for F, Na, Ge, I, Xe)
[Fitzpatrick et al. 1203.3542]
- Finally, convolution with velocity distribution and experimental efficiencies allows to calculate scattering rate for different experiments

Illustrative Example



$$\frac{C_{3,4}^{(5)}}{\Lambda} \xrightarrow{\mu \sim v_{EW}} \frac{C_{3,4}^{(5)}}{\Lambda v_{EW}^2} \xrightarrow{\mu \lesssim m_c} \frac{C_{3,4}^{(5)}}{\Lambda v_{EW}^2} \times \left\{ \frac{2m_G}{27} \alpha_s, m_q \right\}$$

$$\sigma \propto \left(\frac{1}{\Lambda v_{EW}^2} C_{3,4}^{(5)} \right)^2 \left(\sum_{q_\ell = u, d, s} m_{q_\ell} + \sum_{q_h = c, b, t} \frac{2m_G}{27} \alpha_s \right)^2 A^2$$

Summary and Outlook

- Complete EFT framework is **important** for **consistent interpretation** of direct detection data
- Our goal:
 - General setup that **covers most models**
 - Provide **public code** for automatic running from UV to nuclear scale
- Many future directions:
 - **Several multiplets and Higgs interactions**
 - Scalar and vector DM
 - Dimension-seven operators in the UV
 - Heavy DM