



# *Ion vs. Electron Heating by Plasma Turbulence*

*(an accretion-disc problem that opened the “plasmagates”)*



←**Yohei Kawazura**, Michael Barnes→

&

**Alex Schekochihin**

*(Oxford)*



with thanks to S. Cowley, W. Dorland, E. Quataert (who started this),

G. Howes (who turned it into an astro-useable model),

S. Balbus, F. Parra (who were here to help us),

B. Chandran, M. Kunz, N. Loureiro, A. Mallet, R. Meyrand (who were there to discuss)

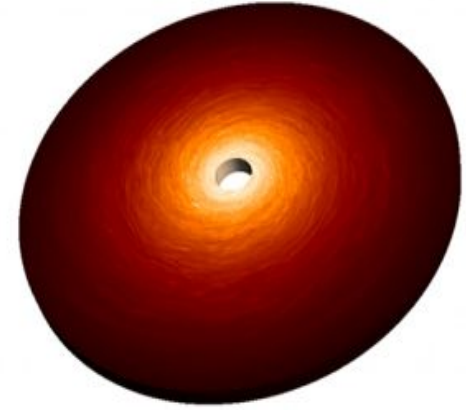
[arXiv:1807.07702]

# An Astrophysics Problem

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Matter in discs **accretes** onto central black hole.



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[Rees, Begelman & Blandford 1982; Narayan & Yi 1995; Quataert & Gruzinov 1999]

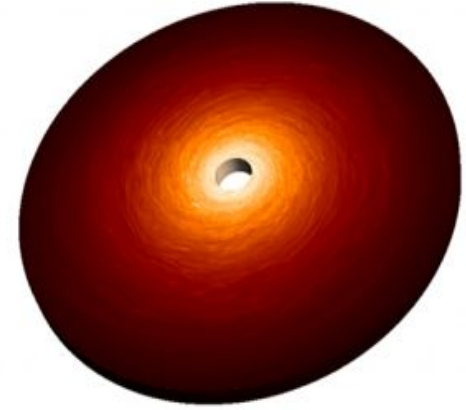
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In order for this **accretion** to happen,  
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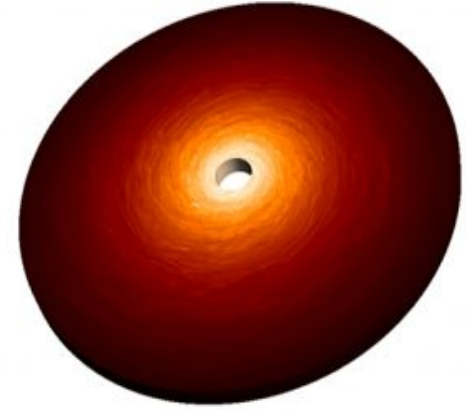


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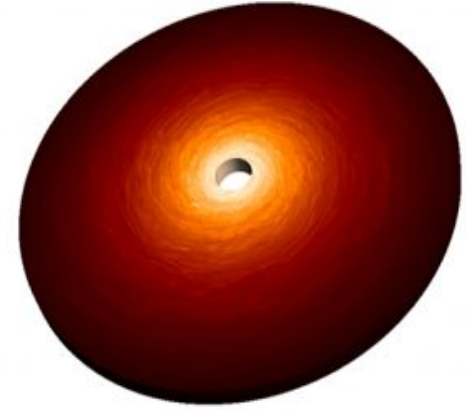
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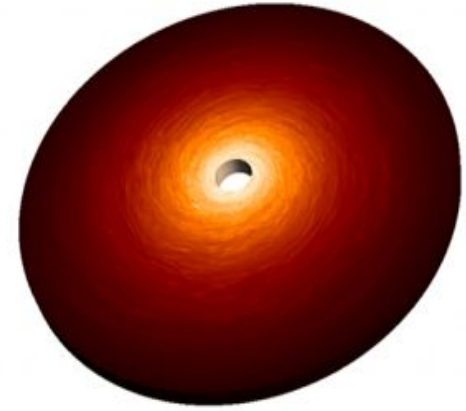
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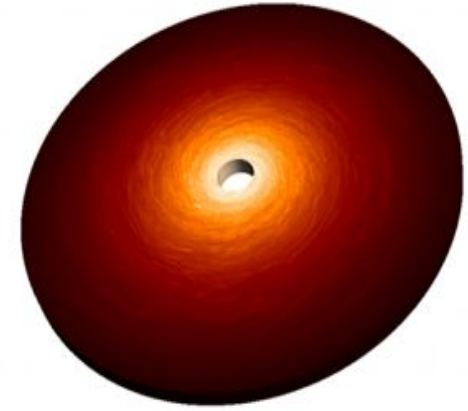
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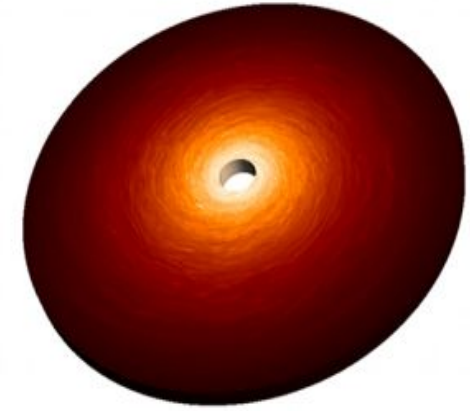
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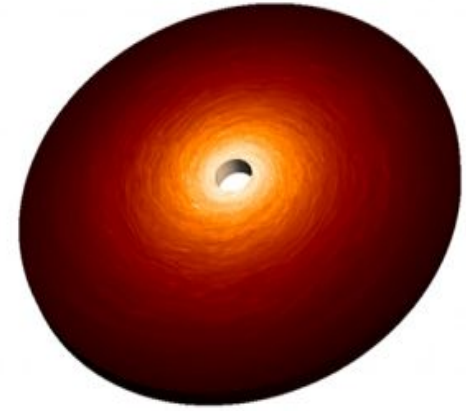
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This question is meaningful in a **weakly collisional plasma**,  
where Coulomb equilibration between species is slow.



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# A Physics Problem

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This problem can be cast in **fundamental physics** terms:

A state with different  $T_i$  and  $T_e$  is out of equilibrium (has free energy). However, we do not know of any linear instabilities that feed off that. The only equilibration mechanism we know is collisions: slow!

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I.e., is turbulence **redistributive**:  $T_i > T_e \rightarrow Q_i < Q_e$  and vice versa,  
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This is a **plasma physics problem**  
because in MHD the two species move together.

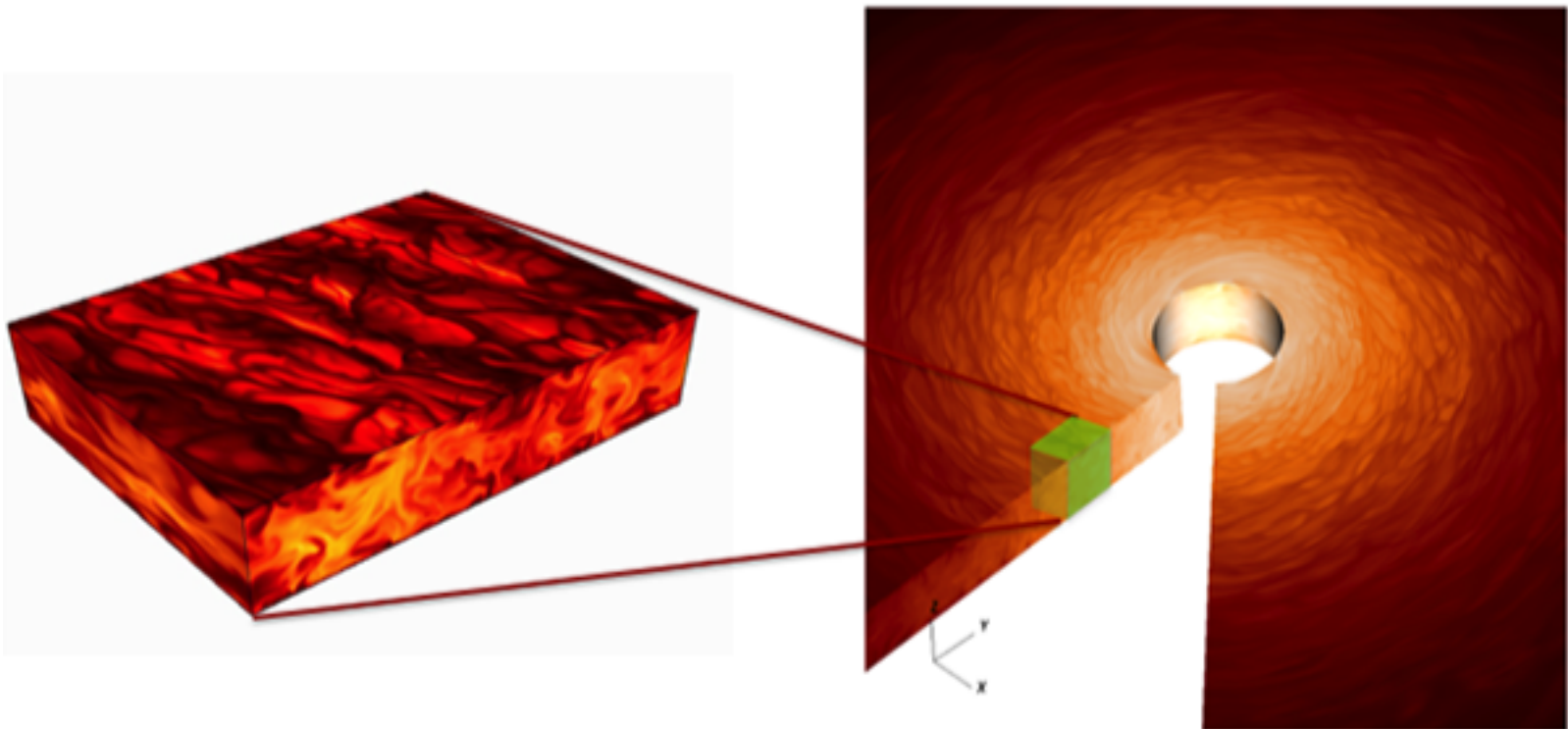
# Global Zoo to Local Universality



General philosophy is that, whatever the global specifics of a particular system, they all happen at MHD scales, where ions and electrons move together, so energy partition between is as yet undecided.

At sufficiently small (but still MHD) scales, turbulence becomes universal, viz., anisotropic ( $k_{\perp} \gg k_{\parallel}$ ) MHD turbulence in a strong mean field.

So our problem can be solved in a homogeneous box, into which energy is (artificially) injected at a given rate.



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It can be shown rigorously that cascades of Alfvénic ( $\mathbf{u}_{\perp}, \delta \mathbf{B}_{\perp}$ ) and “compressive” ( $\delta n, u_{\parallel}, \delta B_{\parallel}, \langle \delta f \rangle_{\theta}$ ) perturbations energetically decouple at the outer scale and cannot exchange energy in the MHD inertial range.

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[AAS et al. 2009, *ApJS* **182**, 310]

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In the solar wind, observationally, most of the energy is in the Alfvénic cascade; we do not know whether it is so elsewhere in Nature.

In our simulations, we only injected Alfvénic perturbations.



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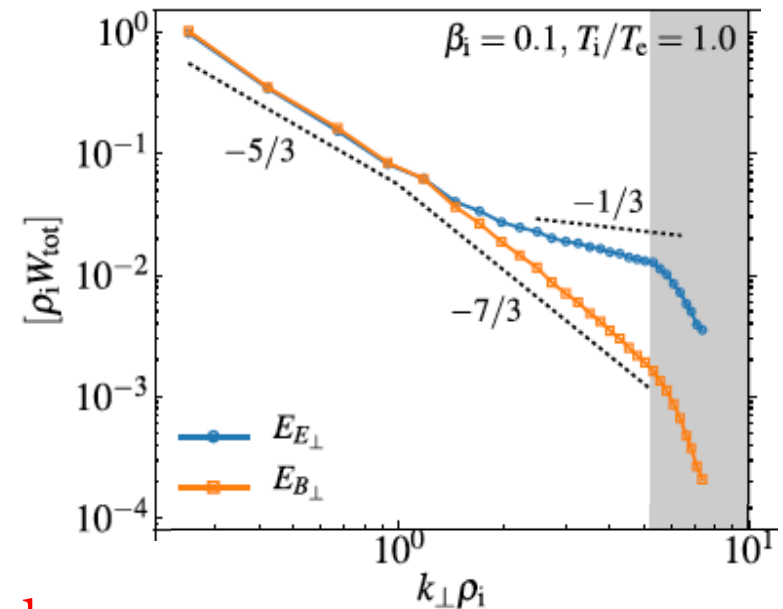
**This changes the nature of turbulence:**

from cascade of Alfvén waves ( $\omega = k_{\parallel} v_A$ ,  $E_{\perp} \sim u_{\perp} \sim \delta B_{\perp}$ )  
+ compressive perturbations

to “kinetic Alfvén waves” (KAW,  $\omega \propto k_{\parallel} v_A k_{\perp} \rho_i$ ,  $E_{\perp} \sim k_{\perp} \delta B_{\perp}$ )  
↳ **electron heating  $\mathcal{Q}_e$**

+ phase-space cascade of ion entropy (linear & nonlinear phase mixing)  
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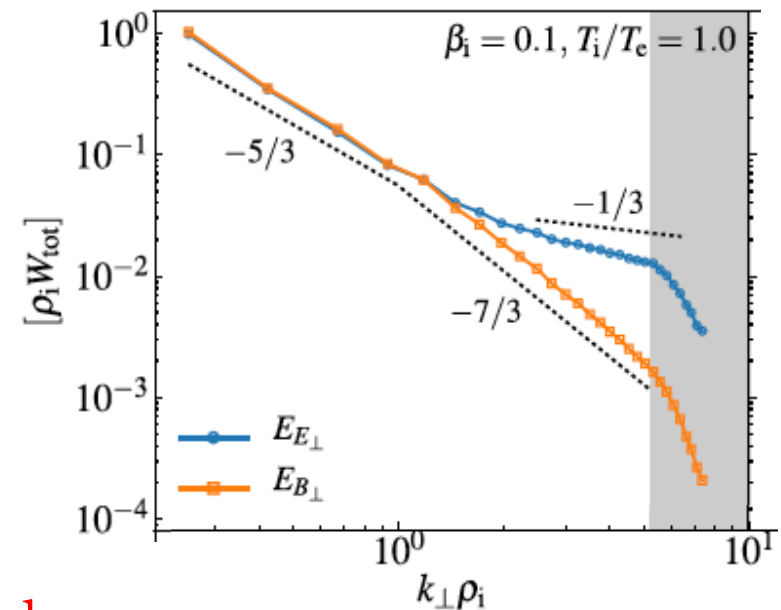
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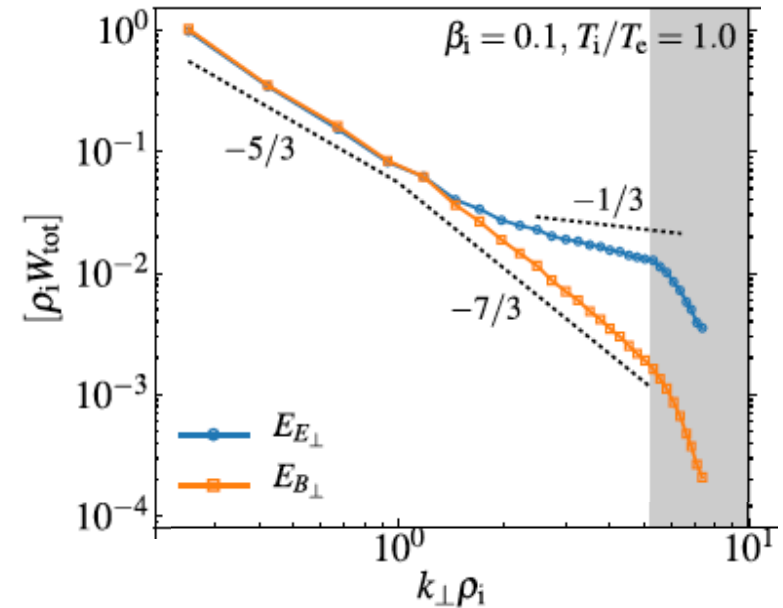
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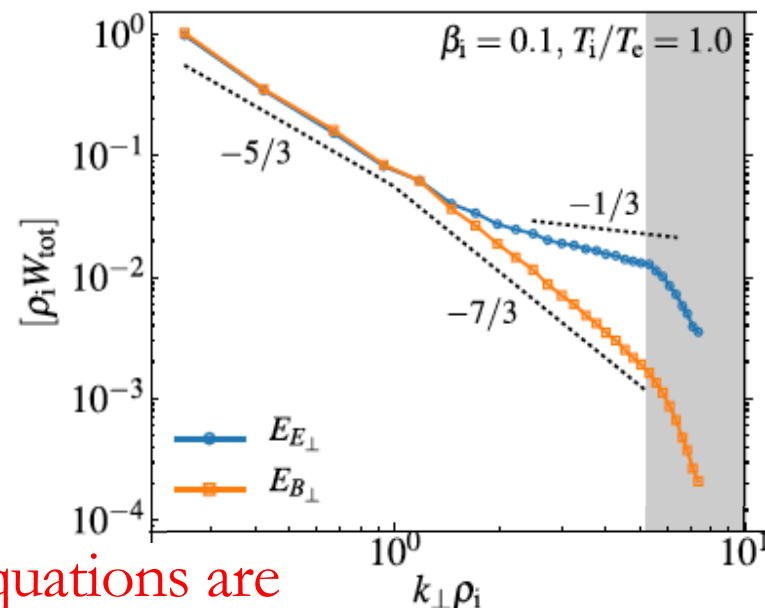
Therefore, all one needs to do is solve for (gyro)kinetic ions + fluid (isothermal) electrons.



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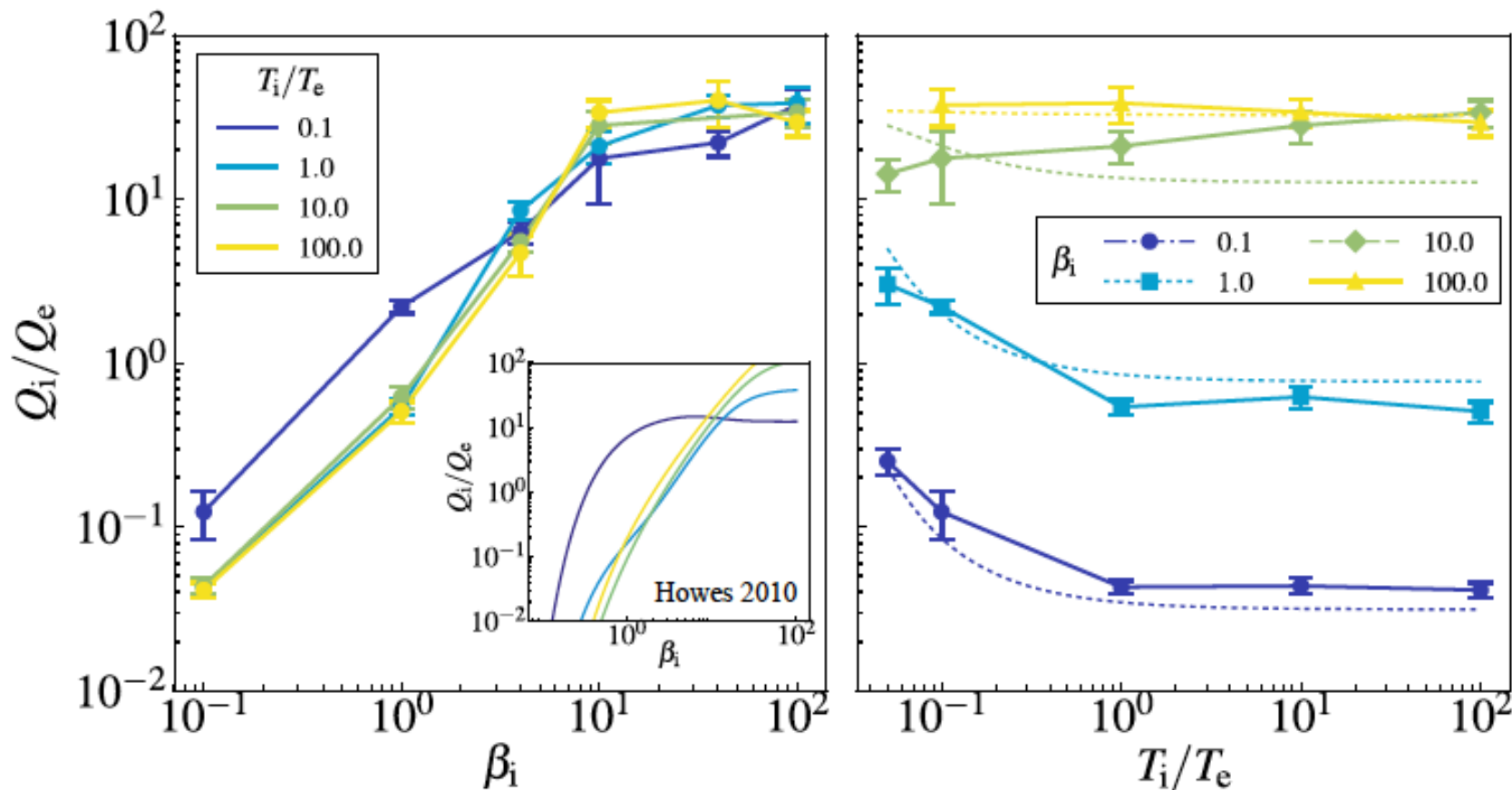


Therefore, all one needs to do is solve for **(gyro)kinetic ions** + **fluid (isothermal) electrons**. The equations are

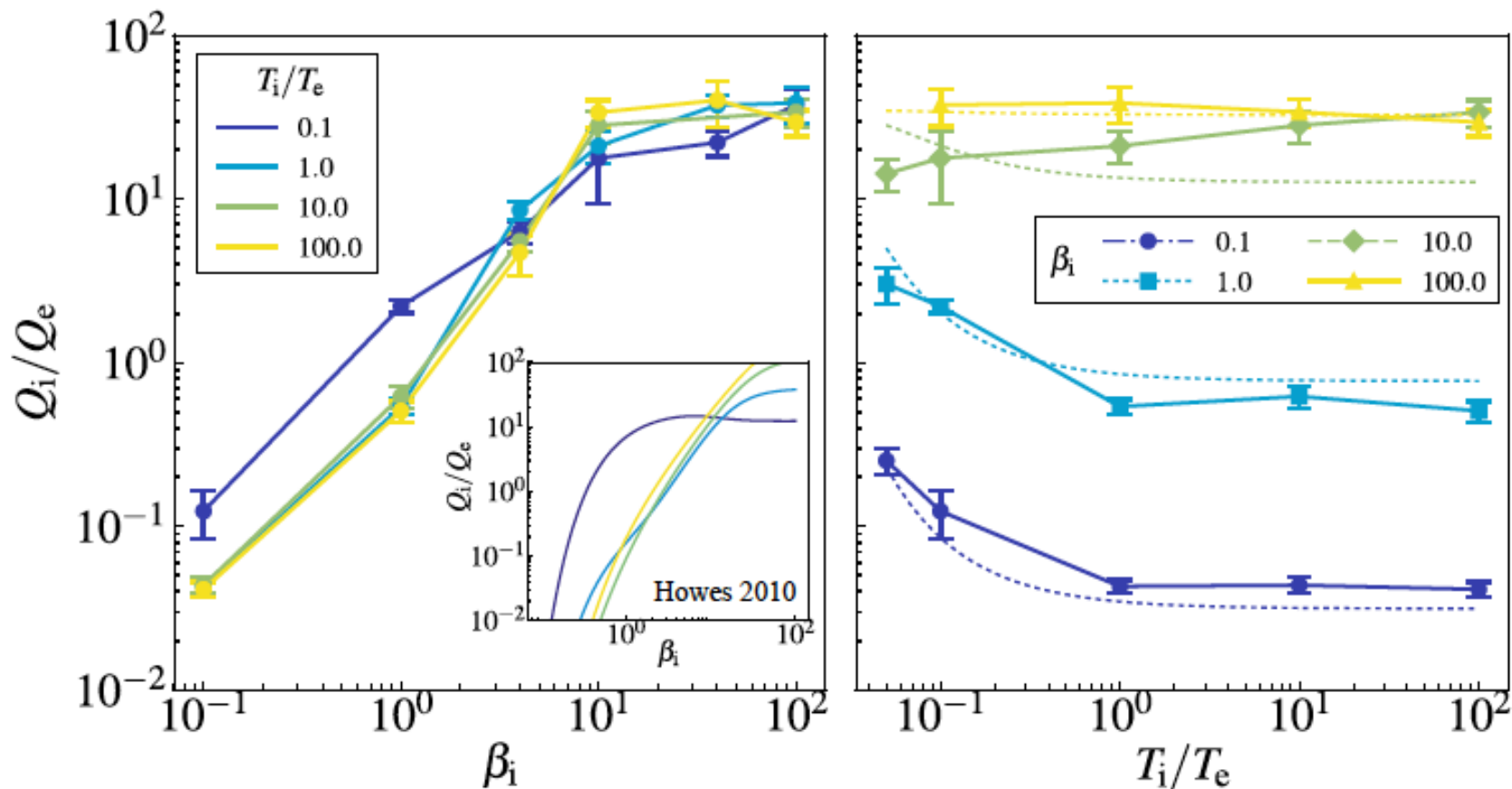
$$\begin{aligned}
 f &= F_0 + \delta f, \quad \delta f = -\varphi(r)F_0 + h(\mathbf{R}), \quad \mathbf{R} = \mathbf{r} + \boldsymbol{\rho}, \quad \boldsymbol{\rho} = \frac{\mathbf{v}_\perp \times \hat{\mathbf{z}}}{\Omega} \\
 \frac{\partial h}{\partial t} + v_\parallel \frac{\partial h}{\partial z} + \frac{\rho_i v_{th}}{2} \{ \langle \chi \rangle_{\mathbf{R}}, h \} &= \frac{\partial \langle \chi \rangle_{\mathbf{R}}}{\partial t} F_0 + C[h] \quad \langle \chi \rangle_{\mathbf{R}} = \hat{J}_0 \varphi - 2 \hat{v}_\parallel \hat{J}_0 \mathcal{A} + \hat{v}_\perp^2 \hat{J}_1 \frac{\delta B}{B} \\
 \frac{\partial \mathcal{A}}{\partial t} + \frac{v_{th}}{2} \nabla_\parallel \varphi &= \frac{v_{th}}{2} \nabla_\parallel \frac{Z}{\tau} \frac{\delta n}{n} + \eta \nabla_\perp^2 \mathcal{A}, \quad \varphi = \frac{Ze\phi}{T_i} \quad \mathcal{A} = \frac{A_\parallel}{\rho_i B_0} \\
 \frac{d}{dt} \left( \frac{\delta n}{n} - \frac{\delta B}{B} \right) + \nabla_\parallel u_{\parallel e} &= -\frac{\rho_i v_{th}}{2} \left\{ \frac{Z}{\tau} \frac{\delta n}{n}, \frac{\delta B}{B} \right\} \\
 \frac{\delta n}{n} = -\varphi + \overline{\hat{J}_0 h}, \quad \frac{u_{\parallel e}}{v_{th}} &= \frac{1}{\beta_i} \hat{\nabla}_\perp^2 \mathcal{A} + \hat{v}_\parallel \hat{J}_0 h + \mathcal{J}_{ext}, \quad \frac{2}{\beta_i} \frac{\delta B}{B} = \left( 1 + \frac{Z}{\tau} \right) \varphi - \frac{Z}{\tau} \overline{\hat{J}_0 h} - \overline{\hat{v}_\perp^2 \hat{J}_1 h}
 \end{aligned}$$

New code: Kawazura & Barnes 2018, *JCP* **360**, 57

[AAS et al. 2009, *ApJS* **182**, 310]

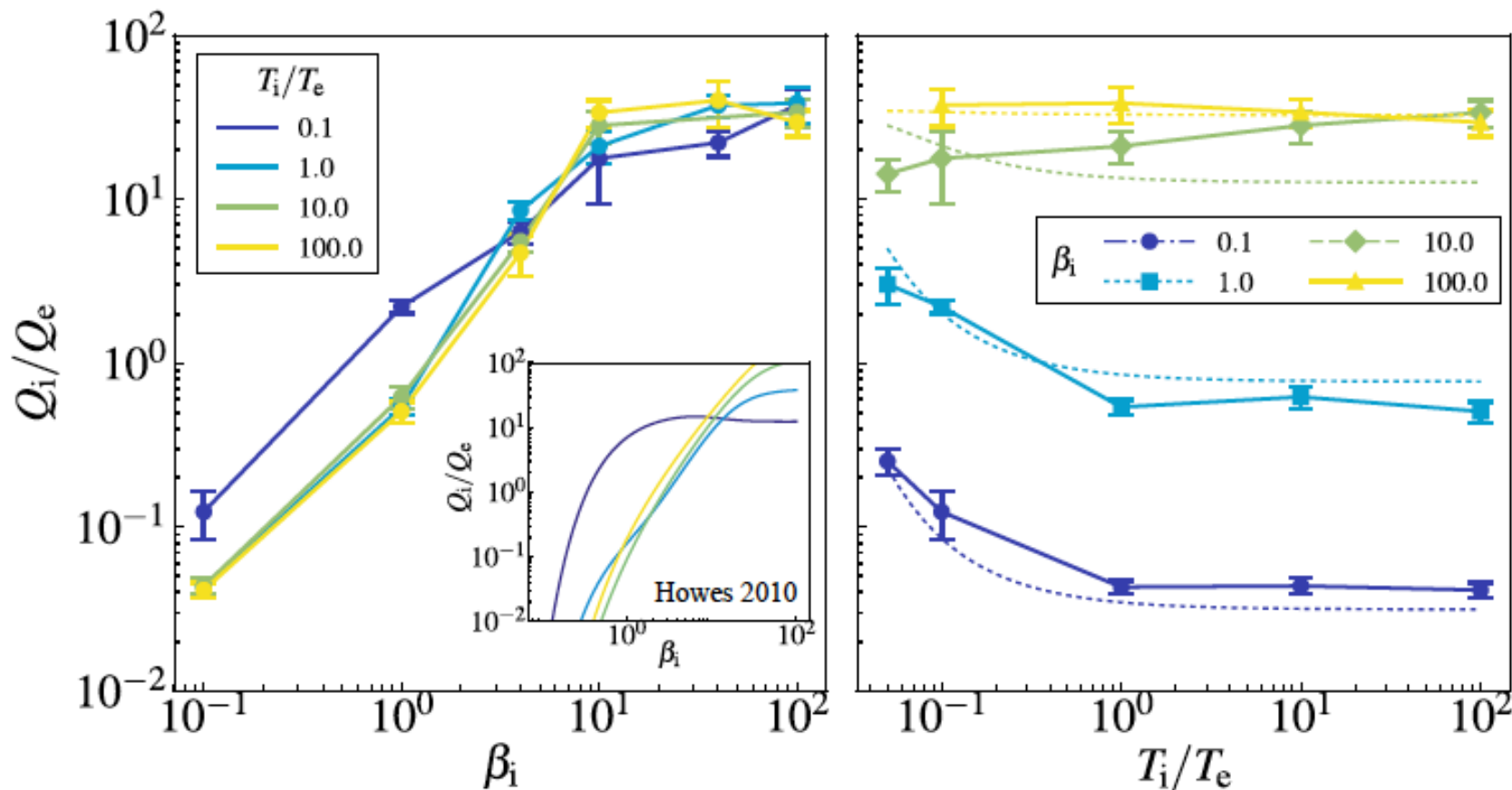


previous, full-GK calculations by Howes et al. 2008, 2011;  
Told et al. 2015, Bañón Navarro et al. 2016 could only afford  
to do one point:  $\beta_i = 1$ ,  $T_i/T_e = 1$



Turbulence is indifferent  
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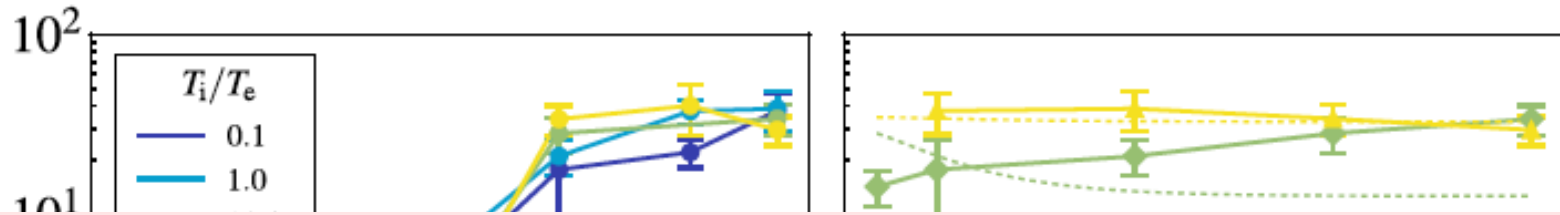




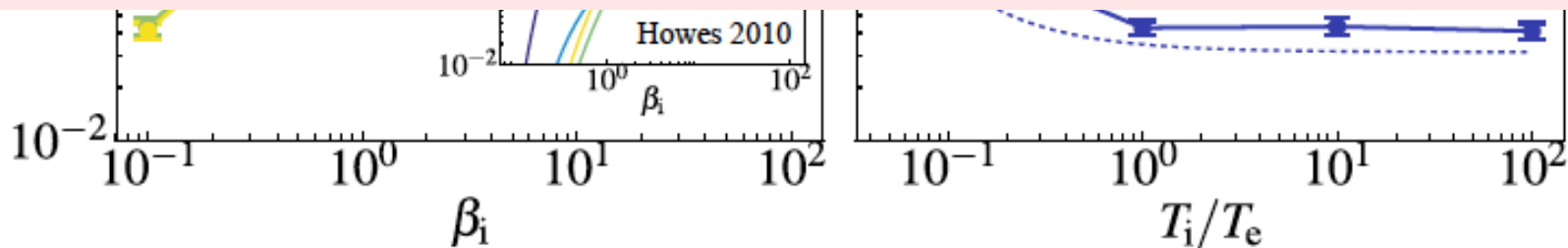
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 at high  $\beta_i$ , ions get hotter  
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# Prescription for Modellers



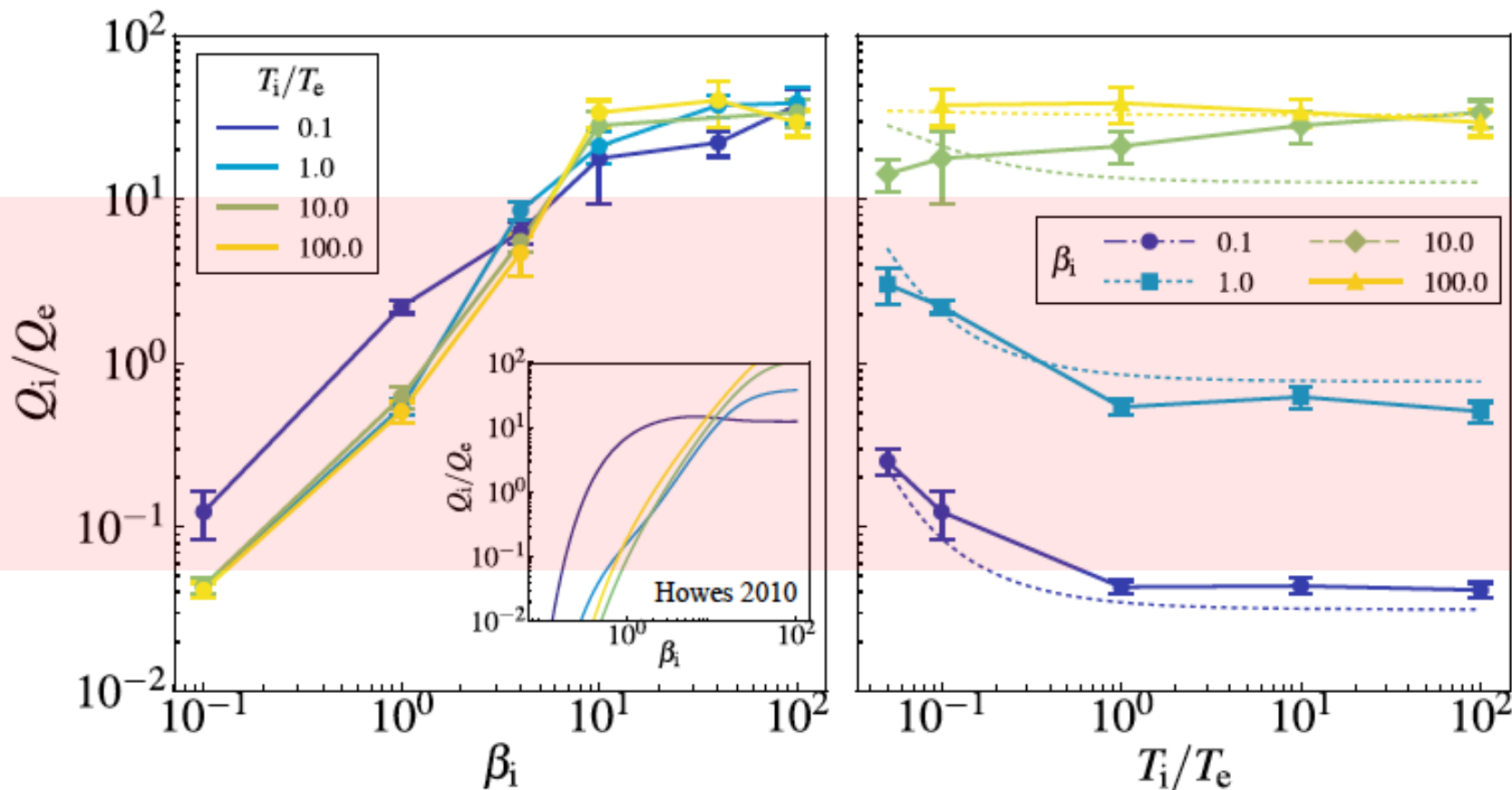
$$\frac{Q_i}{Q_e} = \frac{35}{1 + (\beta_i/15)^{-1.4} e^{-0.1 T_e/T_i}}$$



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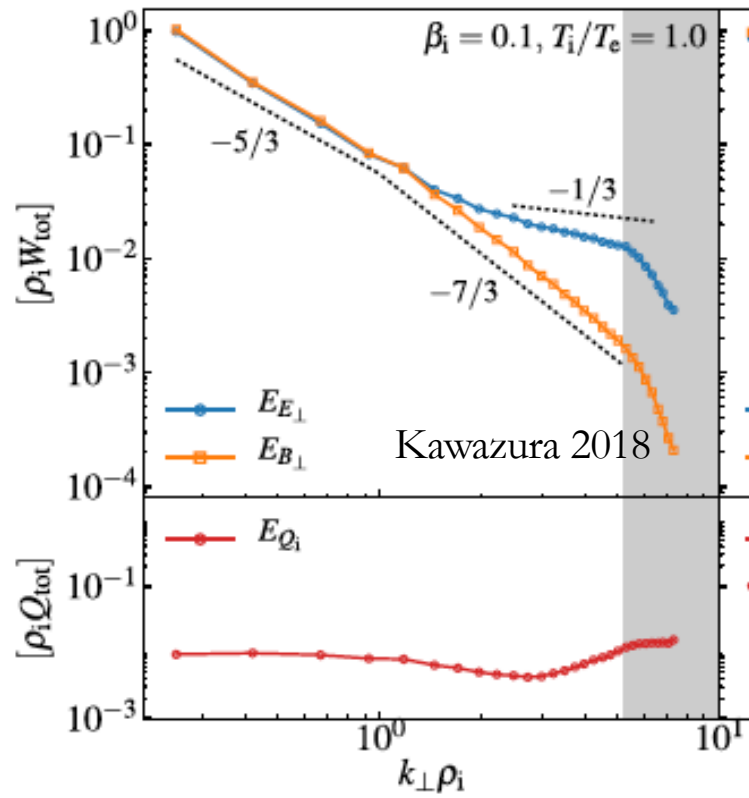
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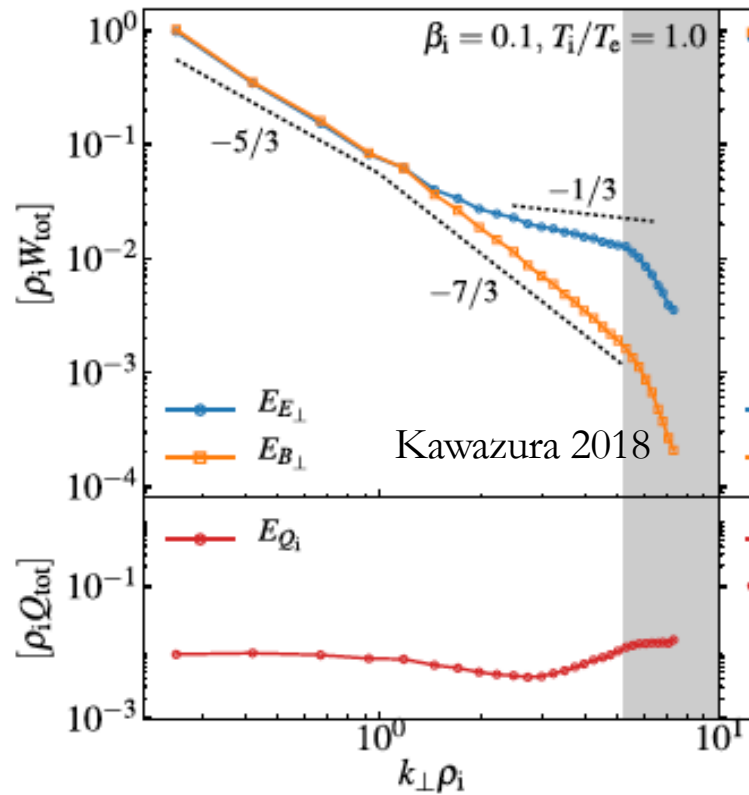
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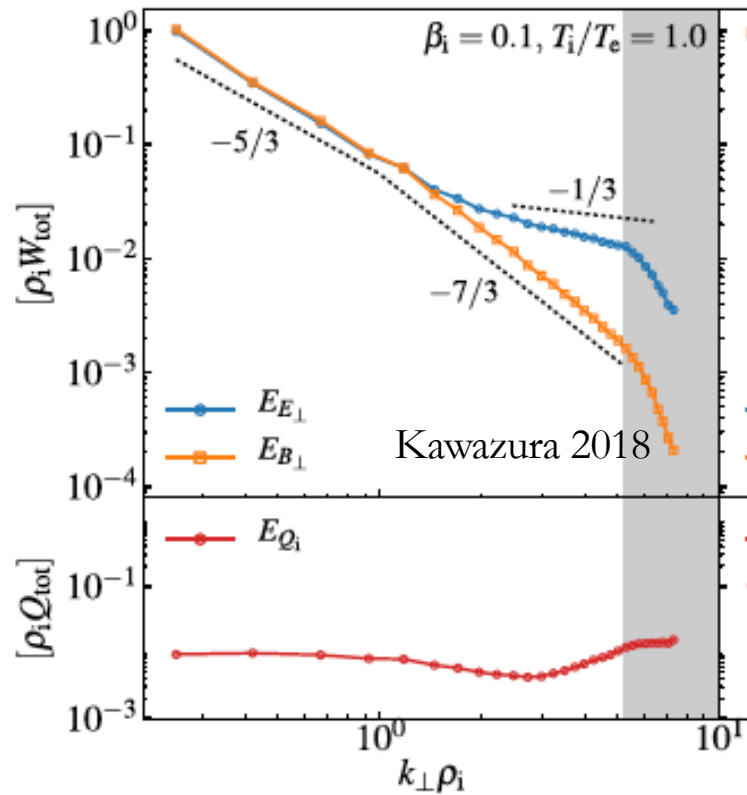
# Low Beta



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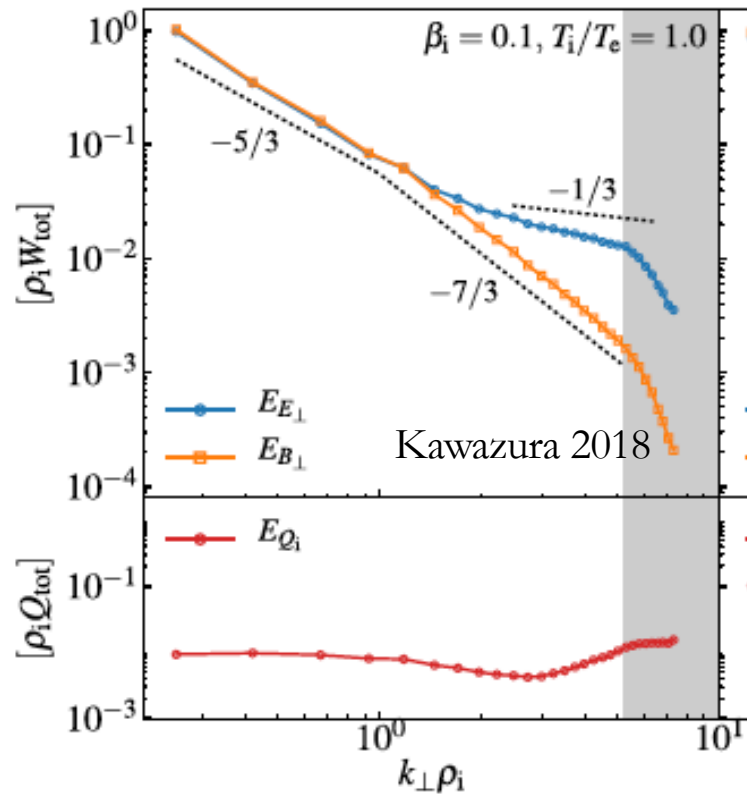


One can prove analytically that  $Q_i/Q_e \rightarrow 0$  as  $\beta_i \rightarrow 0$  because ions are slower than Alfvén waves:  
 $v_{\text{th}i} = v_A \beta_i^{1/2} \ll v_A$



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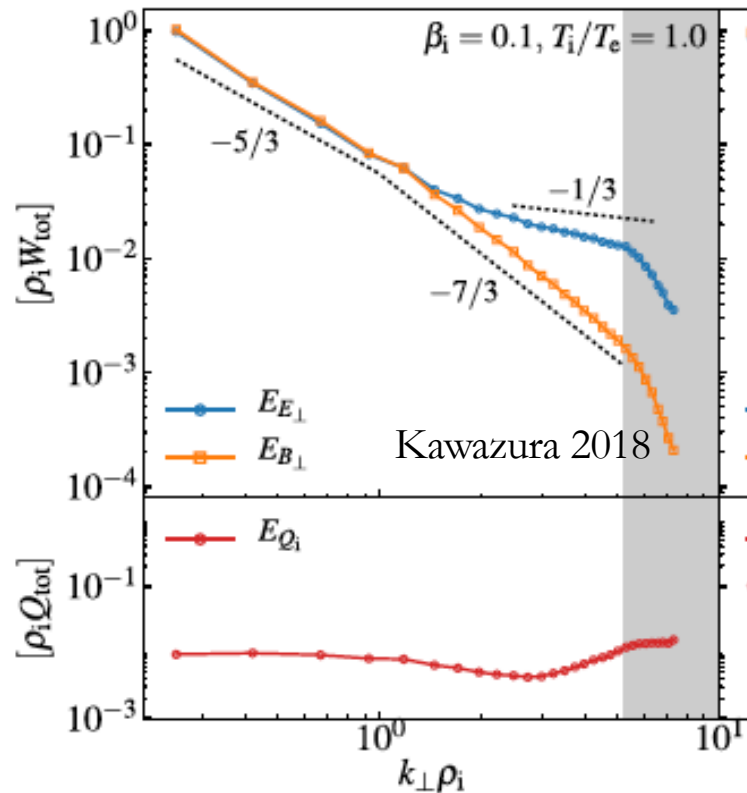
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## CAVEATS:

- GK does not have stochastic ion heating

[Chandran 2010]

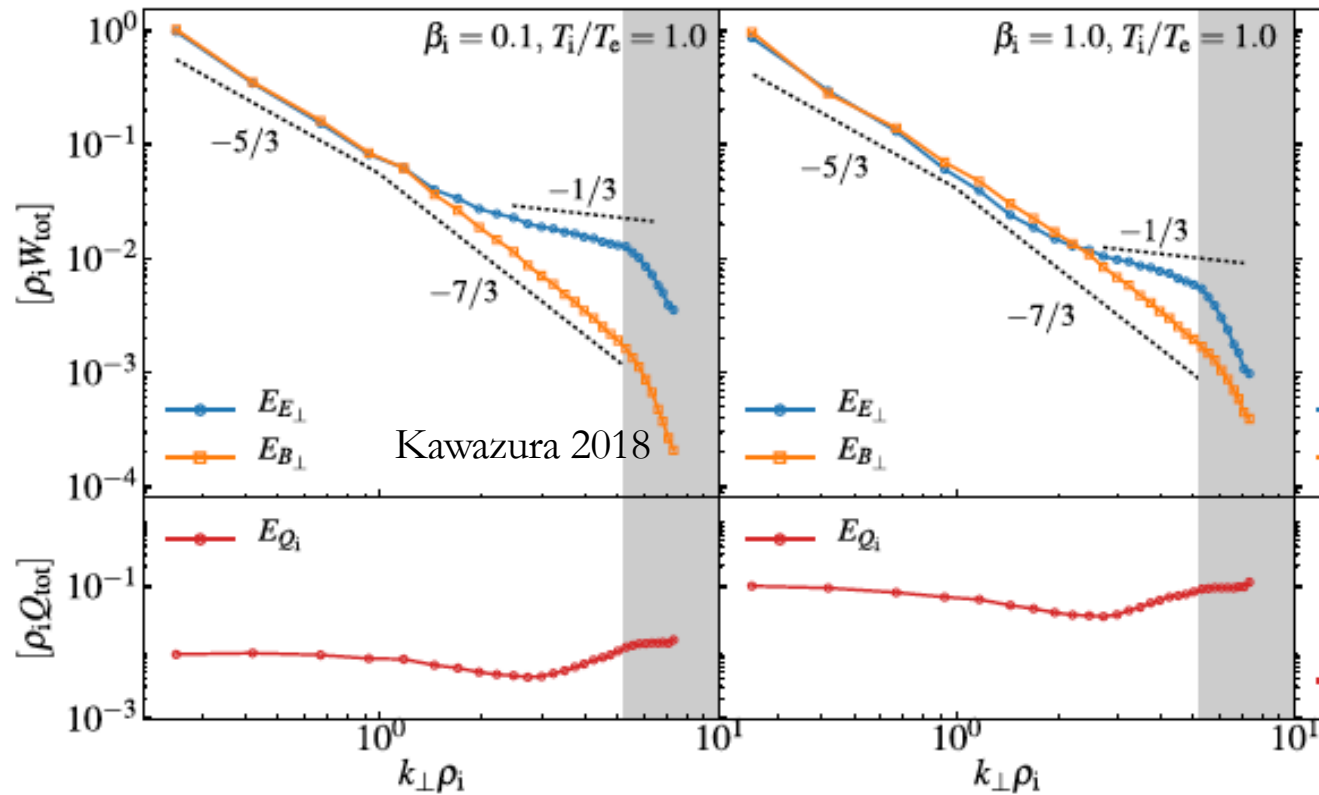
- We might not be resolving multiscale reconnection heating

[cf. Rowan, Sironi, Narayan 2017]

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# Beta = 1

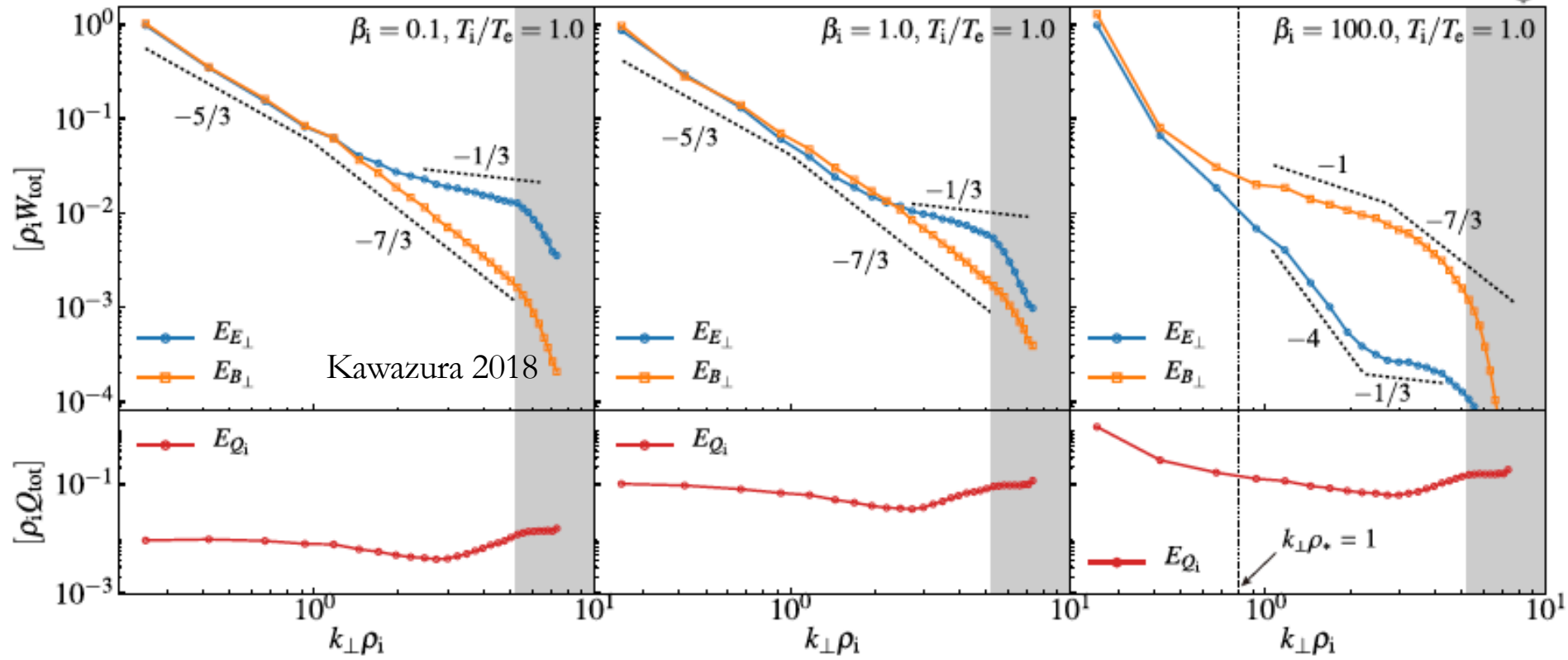


$$Q_i/Q_e \cong 0.5$$

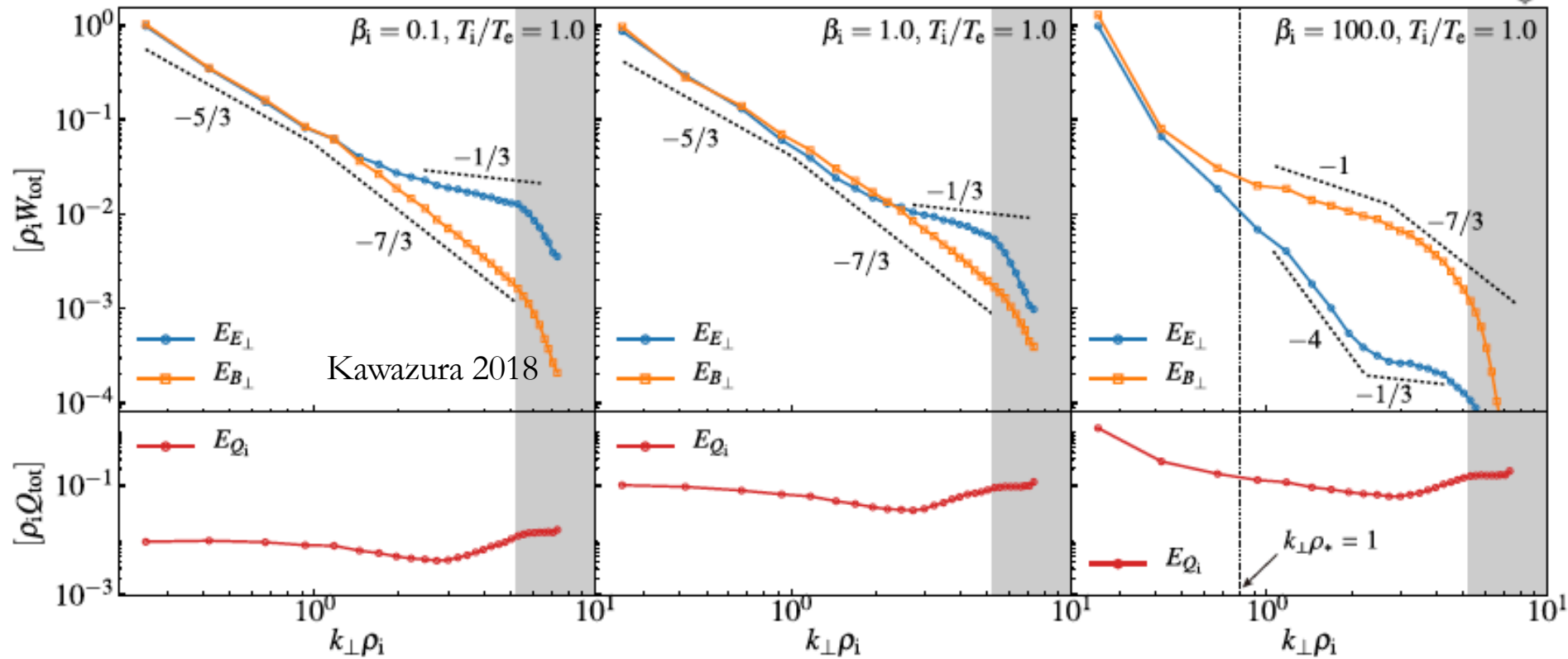
[same result found by Told et al. 2015 in full two-species GK]

Non-asymptotic case: a bit of this, a bit of that...

# High Beta

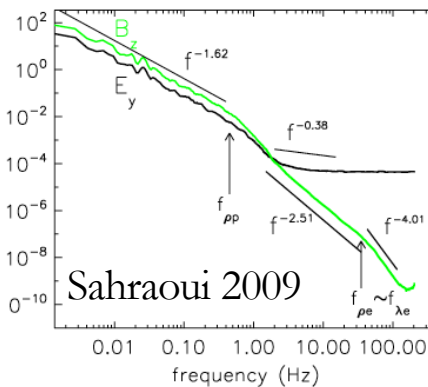
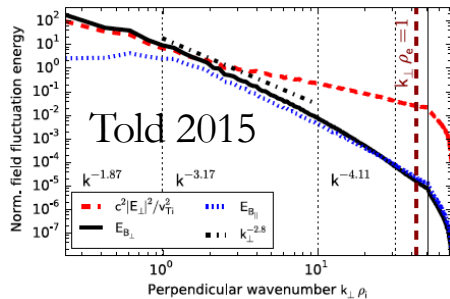


# High Beta



These are familiar from simulations  
and solar wind...

↑  
...but this is a **new regime!**

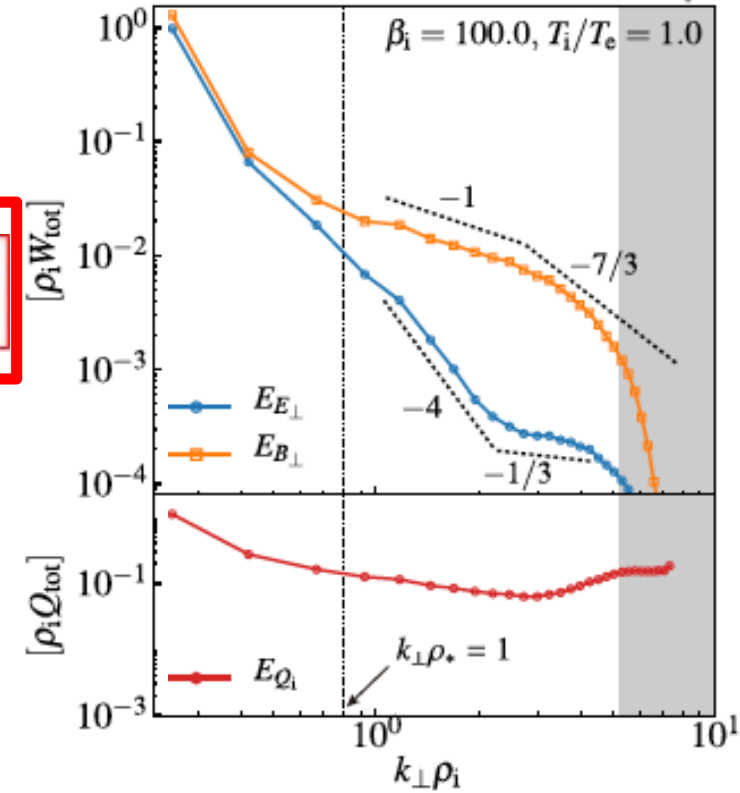


# High Beta



Alfvén waves at high  $\beta_i$  are heavily damped and stop propagating around  $k_{\perp}\rho_* = 1$ ,  $\rho_* \sim \rho_i\beta_i^{-1/4}$ :

$$\omega = |k_{\parallel}|v_A \left[ \pm \sqrt{1 - (k_{\perp}\rho_*)^4} - i(k_{\perp}\rho_*)^2 \right]$$



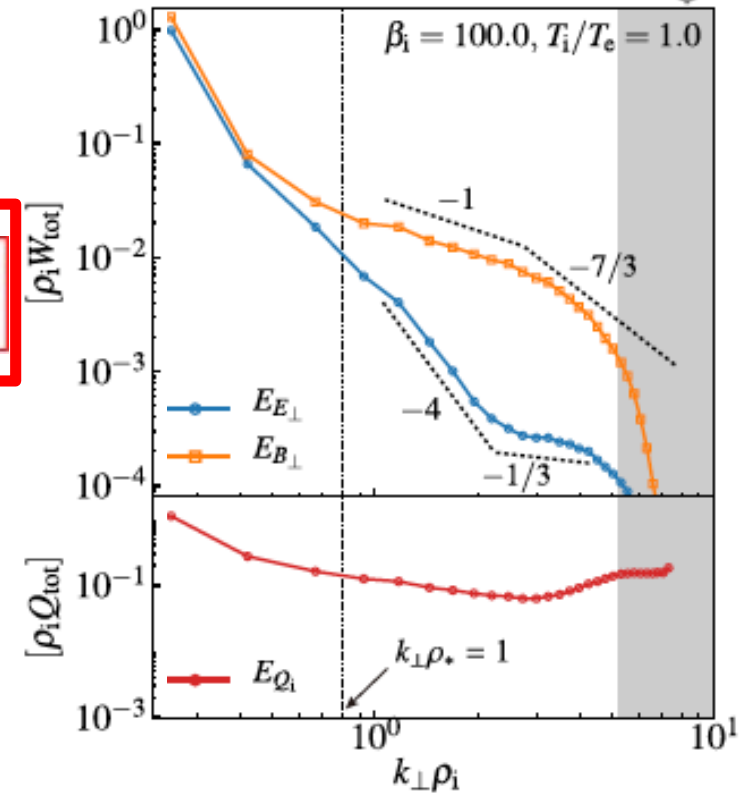
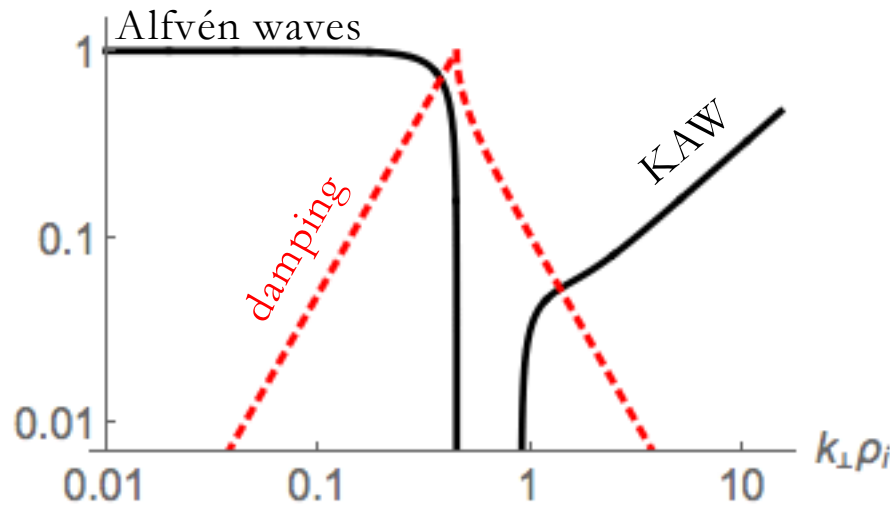
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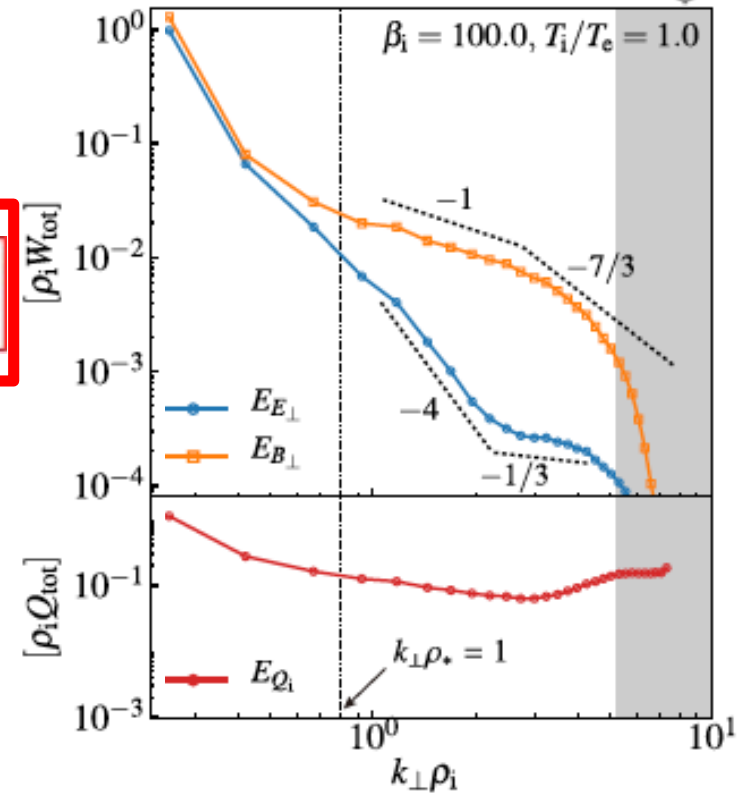
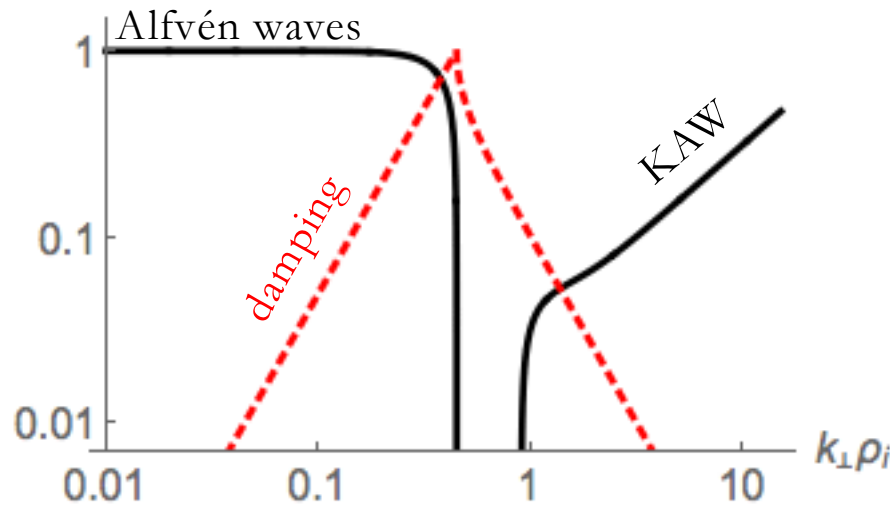
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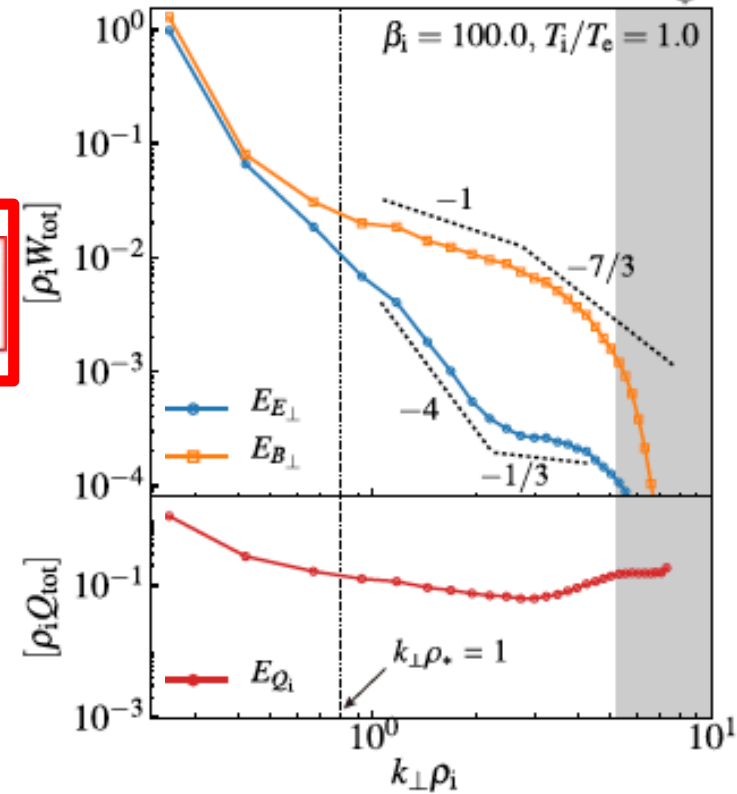
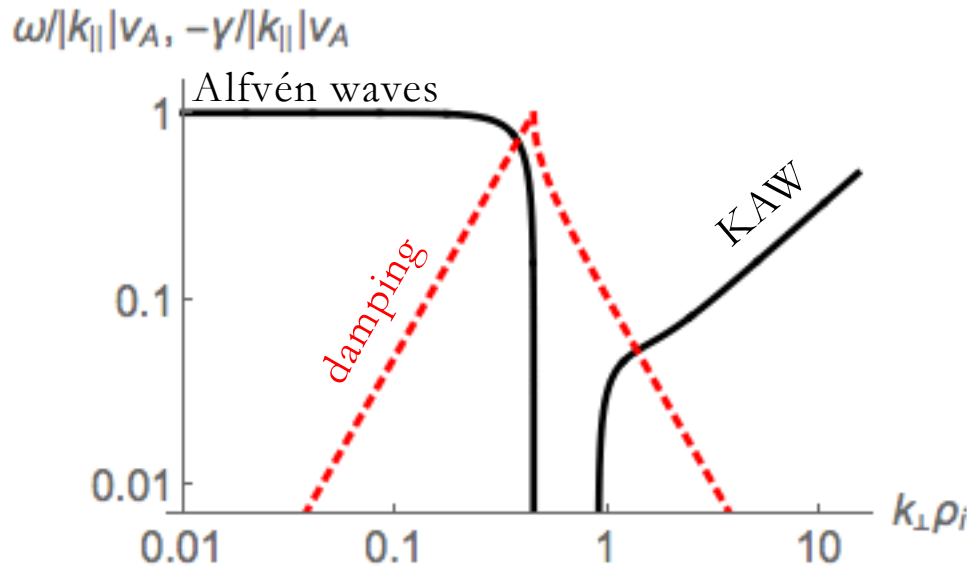
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**magnetic fields** (displacements) **not damped**  
 velocities heavily damped

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**Magnetic-only cascade  
(fields advected  
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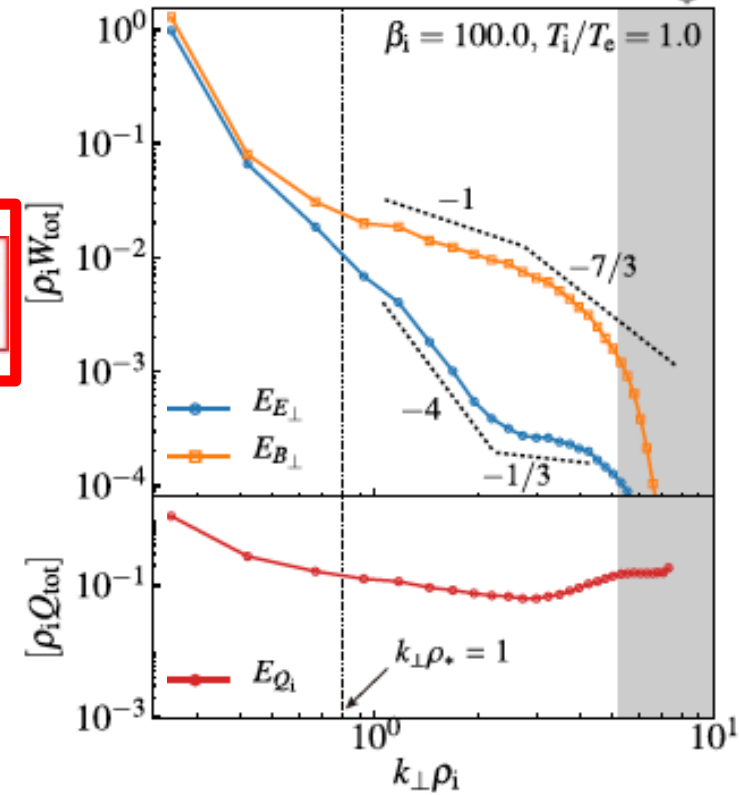
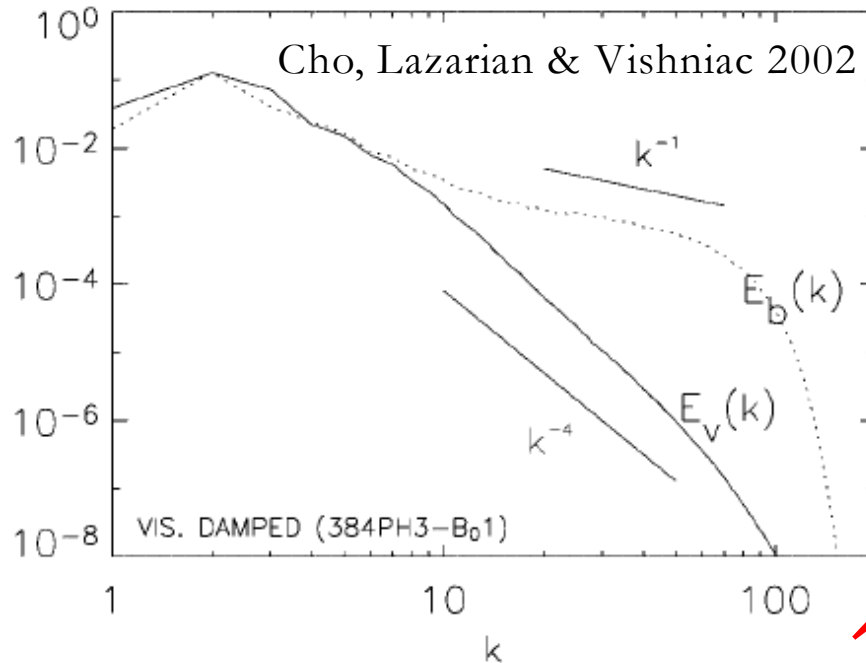
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Reminiscent of high-Pm MHD turbulence at subviscous scales





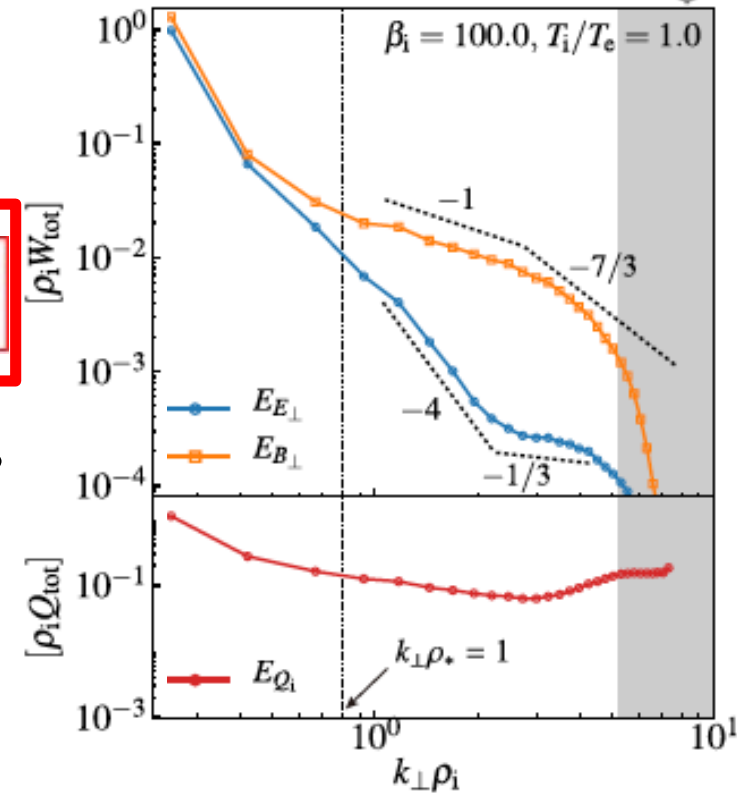
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**an order-unity fraction of cascaded energy is converted into ion heat**



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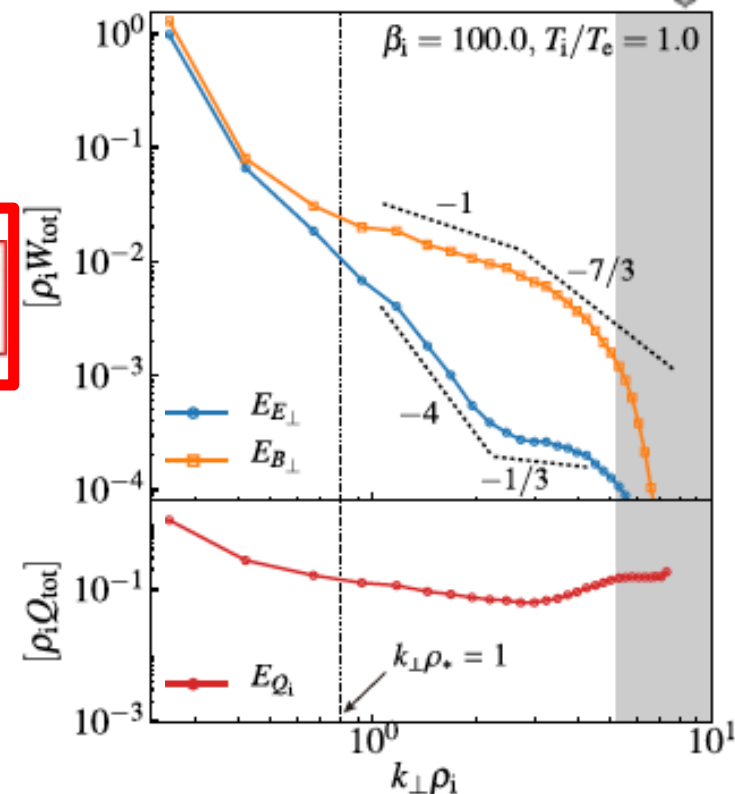


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What fraction is what numerics tell us, viz.,  
 **$Q_i/Q_e \sim 30$**



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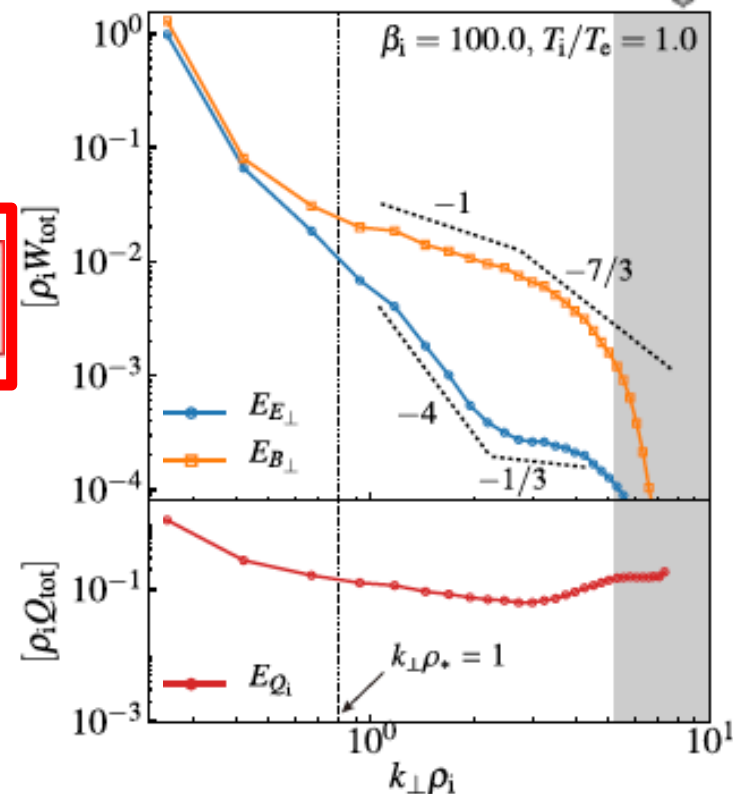
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Why this, exactly, and why it saturates is to do with

- how efficient Landau damping is in a turbulent environment [cf. AAS et al. 2016, *JPP* 82, 905820212: echo effect]
- how efficiently energy is channeled from magnetic to KAW cascade

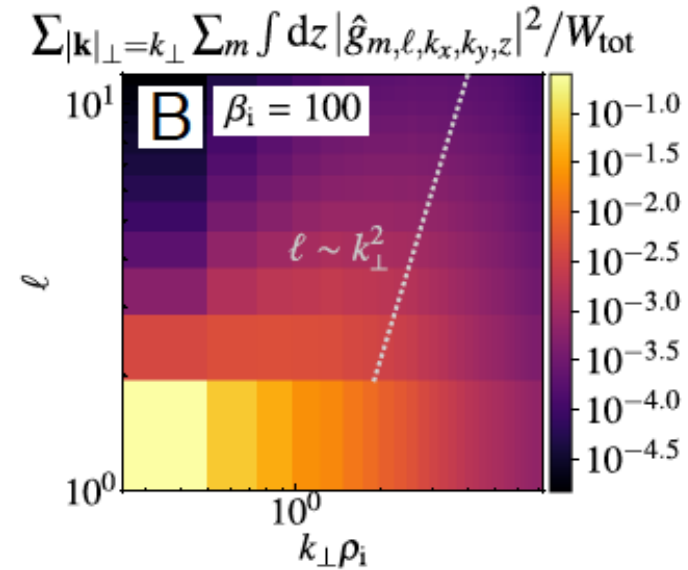
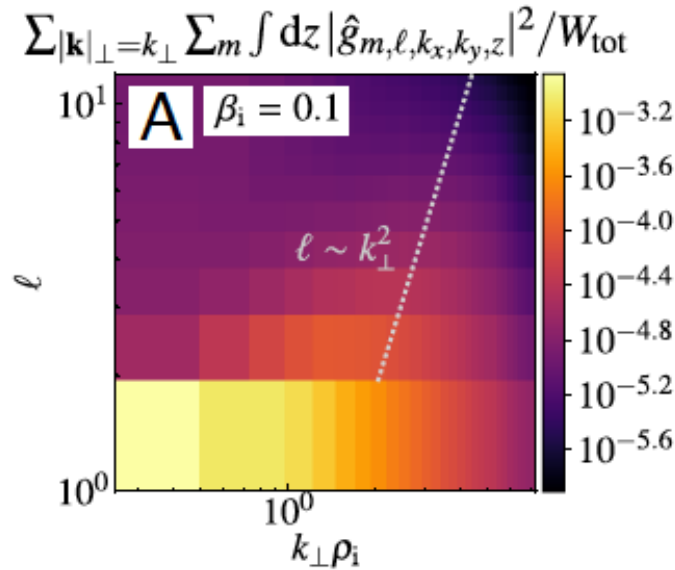


**Magnetic-only cascade  
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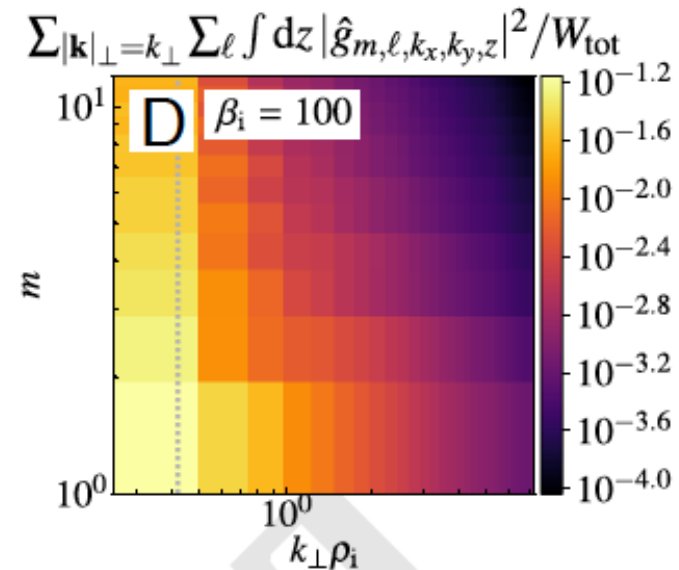
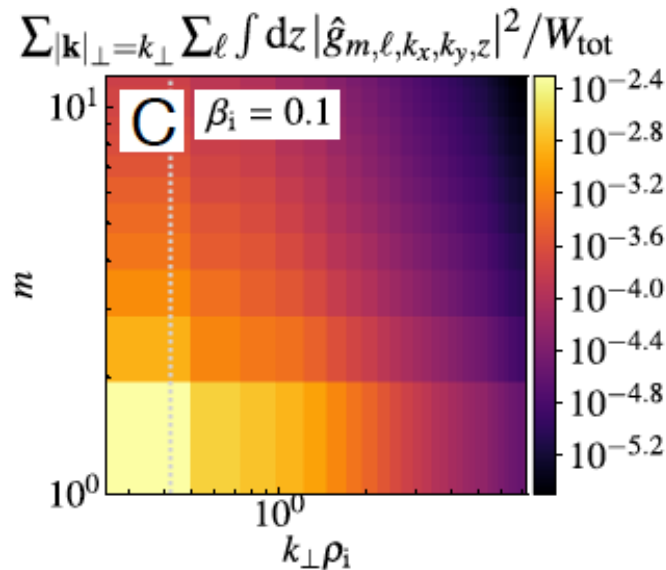
# Phase-Space Cascades



Laguerre  
(dual to  $v_{\perp}$ )



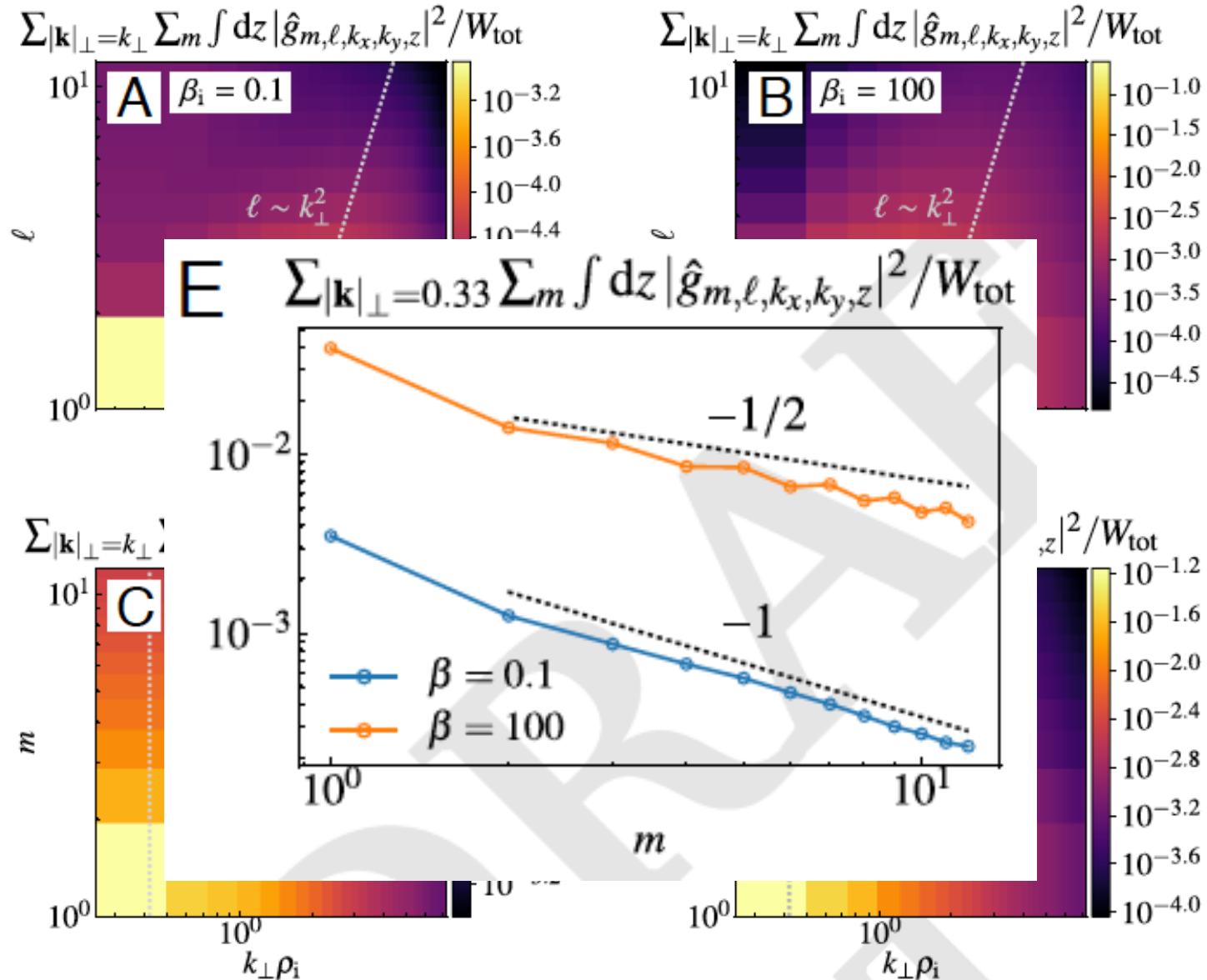
Hermite  
(dual to  $v_{\parallel}$ )



# Phase-Space Cascades



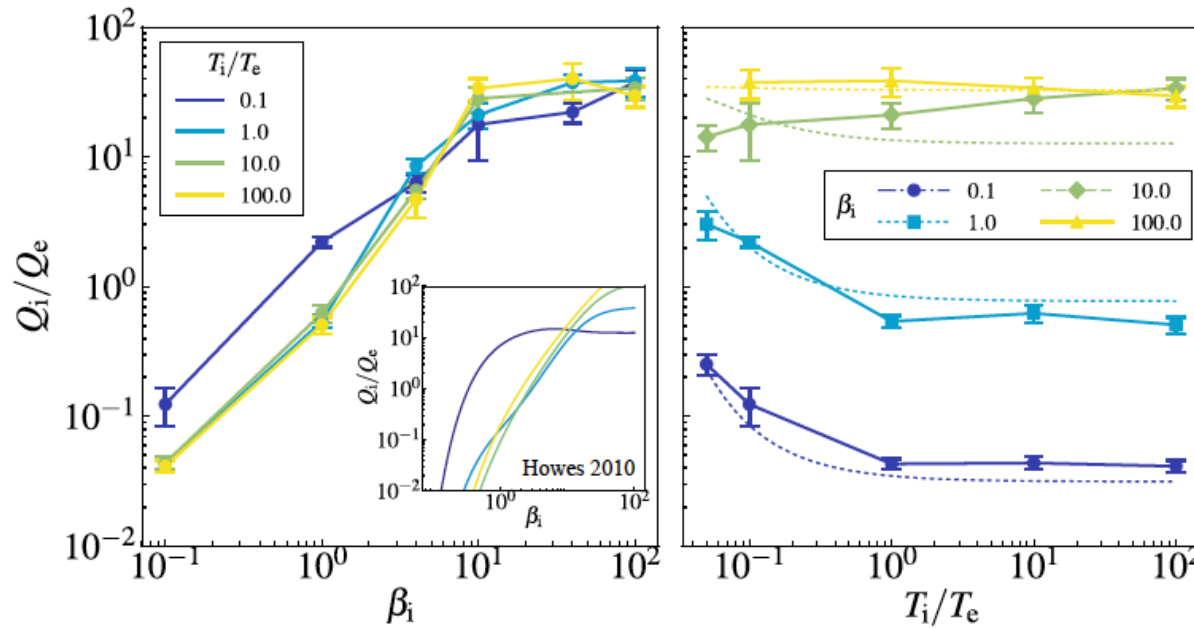
Laguerre  
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# Conclusions



- At **low beta**, i-e energy partition happens at MHD (outer) scale:  
 $Q_i/Q_e = \text{compressive/Alfvénic}$
  - At **high beta**, i-e energy partition happens just above ion Larmor scale;  
 for an Alfvénic cascade,  $Q_i/Q_e \rightarrow 30$
- There is a **new regime of turbulence**, resembling high-Pm MHD

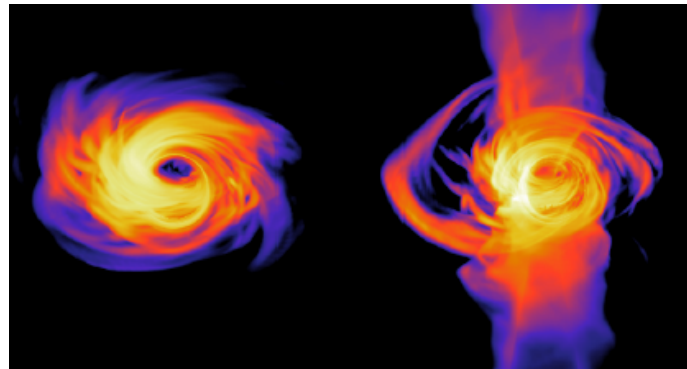


$$\frac{Q_i}{Q_e} = \frac{35}{1 + (\beta_i/15)^{-1.4} e^{-0.1 T_e/T_i}}$$

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- within that, the very low electron heating at low beta turns out to be crucial for **the jet showing up in emission**



more  $Q_e$

less  $Q_e$

from  
Chael, Rowan,  
Narayan et al.  
arXiv:1804.06416

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to explain low luminosity of Sgr A\* without assuming low accretion  
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to be crucial for **the jet showing up in emission**
- A take-away for those interested in fundamental plasma physics:  
**turbulence is indifferent to species inequality**  
(heating is independent of  $T_i/T_e$ )  
and indeed promotes **disequilibrium of species**  
(hotter ions at high  $\beta_i$  and hotter electrons at low  $\beta_i$ )