

Preventing impurity accumulation

H-mode turbulence reduction & I-mode impurity removal

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Motivation

Impurity accumulation

In-out asymmetries

Poloidal variation

Diamagnetic effects

Impurity flow effects

Conservation equations

Momentum \rightarrow Pol. n var.

E_r poloidal variation

Energy \rightarrow Poloidal T var.

Poloidal flow

Pedestal profile alignment

Radial flux

Radial flux evaluation

Impurity confinement

I-mode explanation

Summary

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1) Introduction and motivation

2) New physical phenomena capturing pedestal poloidal variation measurements

3) Radial impurity flux evaluation: tokamak operation and I-mode explanation

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Energy losses due to impurity absorption into the plasma

Introduction and motivation

Motivation

- 1 Impurity accumulation
In-out asymmetries

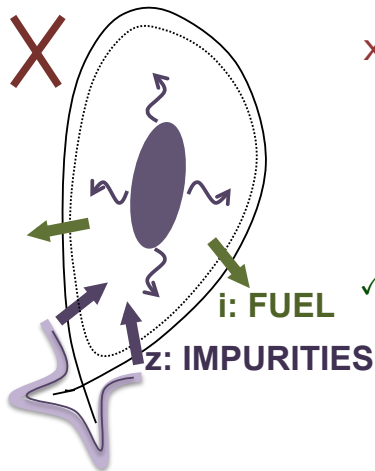
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Diamagnetic effects
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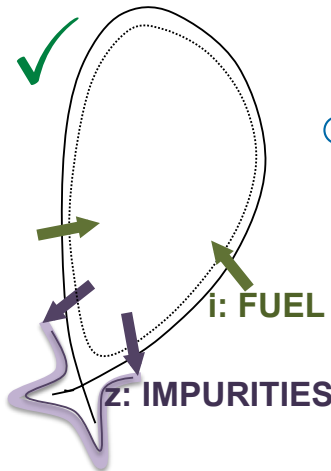
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✗ Tokamaks with high-z divertors (e.g. JET and Alcator C-Mod) can experience large energy losses due to impurity accumulation.

✓ Measuring pedestal radial flux of non-trace impurities could suggest optimal tokamak operation.



\Rightarrow Pedestal impurity radial flow provides insight on impurity confinement.

Pedestal poloidal asymmetries in boron temperature and density

Introduction and motivation

Impurity accumulation \leftrightarrow Pedestal impurity radial flux \propto Parallel friction \leftrightarrow Pedestal impurity poloidal variation

Toroidal mom. Helander 1998

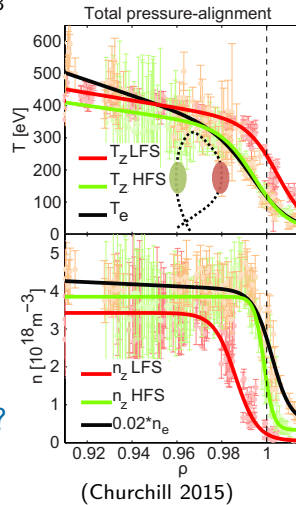
$\mathbf{E} \times \mathbf{B}$ shear stabilization of turbulence:

- Heat transport (high order) \rightarrow turbulence
- H-mode flows (low order) \rightarrow neoclassical theory

Pedestal poloidal asymmetries:

- Boron temperature larger on outboard (LFS) side compared to inboard (HFS).
- HFS accumulation of boron density up to six fold.

Can neoclassical theory predict H-mode pedestal flows?
Pedestal radial flux measuring method?



Motivation

Impurity accumulation

2

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Pedestal profile alignment

Radial flux

Radial flux evaluation

Impurity confinement

I-mode explanation

Summary

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Motivation

Impurity accumulation

In-out asymmetries

3 Poloidal variation

Diamagnetic effects

Impurity flow effects

Conservation equations

Momentum \rightarrow Pol. n var.

E_r poloidal variation

Energy \rightarrow Poloidal T var.

Poloidal flow

Pedestal profile alignment

Radial flux

Radial flux evaluation

Impurity confinement

I-mode explanation

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Main novel physics self-consistently allowed in theory developed

Explaining pedestal in-out asymmetries



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Species: (i) Banana Maxwell-Boltzmann bulk ions
(z) Collisional highly charged non-trace impurities

Orderings keep diamagnetic effects:

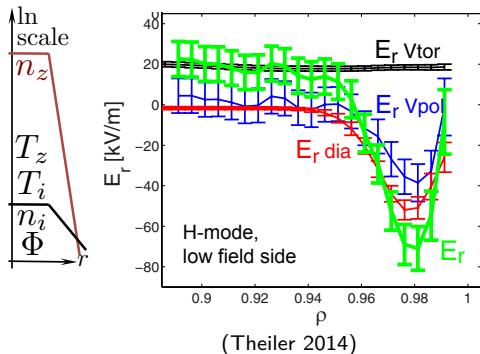
◦ Radial variation:

$$\mathbf{E}_r = \frac{1}{z_z e n_z} \frac{\partial p_z}{\partial r} + V_{zt} B_p - V_{zp} B_t$$

$$\frac{\nabla_{\perp} n_z}{n_z} \sim \frac{\frac{z_z}{z_i} \frac{\nabla_{\perp} \Phi}{\frac{T_i}{z_i e}}}{1} \ll \frac{1}{\rho_{pz}}$$

◦ Poloidal variation: $\underbrace{\frac{\partial \ln B}{\partial \theta}}_{\sim \epsilon} \lesssim \frac{\partial \ln n_z}{\partial \theta}$

⇒ Strong radial and poloidal impurity density variation.



Motivation

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3

Diamagnetic effects

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Poloidal flow
Pedestal profile alignment

Radial flux

Radial flux evaluation
Impurity confinement
I-mode explanation

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Need to retain 2D radial flow effects for self-consistency

Explaining pedestal in-out asymmetries



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○ \perp Momentum:

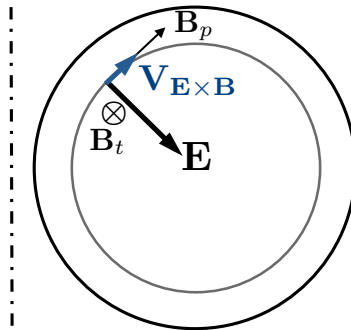
$$\mathbf{V}_{z\perp} = \frac{c}{B^2} \mathbf{B} \times \left[\nabla \Phi + \frac{1}{z_z e n_z} \nabla p_z \right]$$

○ Particles:

$$\nabla \cdot [\mathbf{V}_z n_z] = \underbrace{\nabla \cdot [\mathbf{V}_{z\perp} n_z]}_{\text{Also radial flow!}} + \nabla \cdot [\mathbf{V}_{z\parallel} n_z] = 0$$



$$V_{z\parallel} = V_{z\parallel}^{1D} + V_{z\parallel}^{\text{diamagnetic}} + V_{z\parallel}^{\text{radial}}$$



\Rightarrow RADIAL FLOW affects PARALLEL FLOW due to the strong radial variation.

Motivation

Impurity accumulation

In-out asymmetries

Poloidal variation

Diamagnetic effects

Impurity flow effects

Conservation equations

Momentum \rightarrow Pol. n var.

E_r poloidal variation

Energy \rightarrow Poloidal T var.

Poloidal flow

Pedestal profile alignment

Radial flux

Radial flux evaluation

Impurity confinement

I-mode explanation

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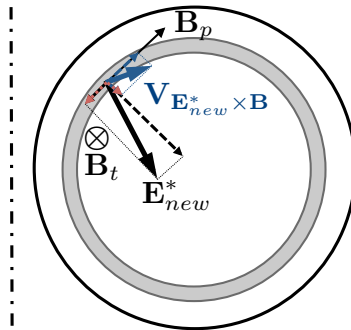
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Preventing
impurity
accumulation

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Motivation

Impurity accumulation

In-out asymmetries

Poloidal variation

Diamagnetic effects

Impurity flow effects

Conservation equations

Momentum → Pol. n var.

E_r poloidal variation

Energy → Poloidal T var.

Poloidal flow

Pedestal profile alignment

Radial flux

Radial flux evaluation

Impurity confinement

I-mode explanation

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Self-consistent set of conservation equations for impurities

Explaining pedestal in-out asymmetries



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Self-consistent set of conservation equations for impurities:

○ || Momentum:

$$\underbrace{m_z n_z \mathbf{V}_z \cdot \nabla \mathbf{V}_z \cdot \frac{\mathbf{B}}{B}}_{\text{Inertial term}} + \underbrace{\frac{\mathbf{B}}{B} \cdot (\nabla \cdot \pi_z)}_{\text{Viscosity}} + \underbrace{\nabla_{\parallel} p_z}_{\text{Press.grad.}} + \underbrace{n_z z e \nabla_{\parallel} \Phi}_{\text{Pot.grad.}} = \underbrace{R_{zi}}_{\text{Frict.}}$$

⇒ The impurity parallel flow modifies the **friction** with the background ions.

○ Energy:

$$\underbrace{\frac{3}{2} n_z \mathbf{V}_z \cdot \nabla T_z}_{\text{Convection}} + \underbrace{p_z \nabla \cdot \mathbf{V}_z}_{\text{Comp.heating}} + \underbrace{\nabla \cdot \mathbf{q}_z}_{\text{Heat flux}} + \underbrace{\pi_z : \nabla \mathbf{V}_z}_{\text{Viscous}} = \underbrace{\frac{3}{2} n_z \nu_{zi} (T_i - T_z)}_{\text{Equilibration}}$$

⇒ **Compressional heating** drives **impurity temperature poloidal variation**.

Its importance grows with the size of the flows.

Motivation

Impurity accumulation

In-out asymmetries

Poloidal variation

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5

Conservation equations

Momentum → Pol. n var.

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Poloidal flow

Pedestal profile alignment

Radial flux

Radial flux evaluation

Impurity confinement

I-mode explanation

Summary

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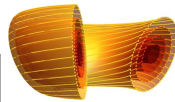
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Momentum: Diamagnetic effects \rightarrow Poloidal density variation

Explaining pedestal in-out asymmetries

Non-linear \parallel momentum: $\nabla_{\parallel} p_z + n_z z e \nabla_{\parallel} \Phi = R_{zi} \parallel \Rightarrow$
drives

$$(1 + \alpha n) \frac{\partial n}{\partial \vartheta} = g (n - b^2) + U (n - 1) - D \left[(1 - b^2) - \alpha (n - 1) \right]$$



(Ball 2014)

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accumulation

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Motivation

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In-out asymmetries

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Impurity flow effects

Conservation equations

Momentum \rightarrow Pol. n var.

E_r poloidal variation

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Poloidal flow

Pedestal profile alignment

Radial flux

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Impurity confinement

I-mode explanation

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Non-dimensionalization:

Poloidal
variation:

$$[n] = \frac{n_z}{\langle n_z \rangle}$$

$$b^2 = \frac{B^2}{\langle B^2 \rangle}$$

$$[T] = \frac{T_z}{T_i}$$

Amplification factors
(flux functions):

$$g = -\xi \left\langle \frac{\partial \ln p_i}{\partial \psi} - \frac{3}{2} \frac{\partial \ln T_i}{\partial \psi} \right\rangle$$

$$U = \xi \gamma \int d^3 v_i \frac{h_i}{B} \frac{v_{i\parallel}}{v_i^3}$$

$$D = -\xi \frac{\langle T_z \rangle}{T_i} \frac{z_i}{z_z} \frac{\partial \ln \langle p_z \rangle}{\partial \psi}$$

$$\alpha = \frac{\frac{z_z^2 \langle n_z \rangle}{z_i^2 \langle n_i \rangle} \frac{T_i}{\langle T_z \rangle}}{1 + \frac{\langle n_e \rangle}{z_i \langle n_i \rangle} \frac{T_i}{z_i T_e}} \sim 1$$

Radial derivatives of
poloidal variation \Rightarrow As 1D with 2D effects
cancel

Known

Unknown

Magnetic field: b^2

Radial variation: g, U, D

Poloidal variation: n, T

$$n_z = \underbrace{\langle n_z \rangle}_{\text{known}} \left(1 + \frac{n_z - \langle n_z \rangle}{\underbrace{\langle n_z \rangle}_{\text{unknown}}} \right)$$

Momentum: Diamagnetic effects \rightarrow Poloidal density variation

Explaining pedestal in-out asymmetries



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accumulation

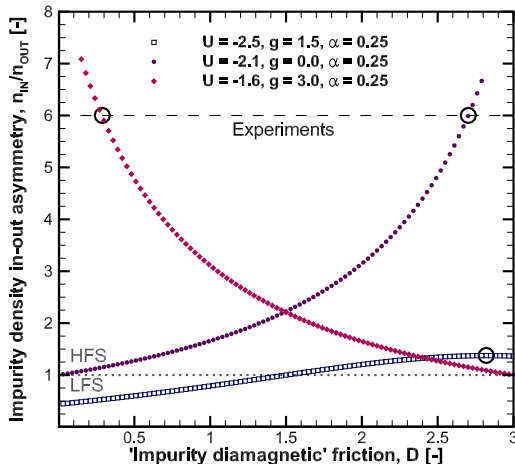
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$$\text{Linear parallel momentum: } (1 + \alpha) \frac{\partial n}{\partial \vartheta} = (g - D) (1 - b^2) + (g + U + \alpha D) (n - 1)$$

$$\text{E.g. } \left\| \begin{array}{l} b^2 = 1 - 2\epsilon \cos \vartheta \\ n = 1 + C \cos \vartheta + S \sin \vartheta \\ \text{with } S^2 + C^2 \leq 1 \ (n \geq 0) \end{array} \right.$$

The \bigcirc corresponds to the 'impurity diamagnetic' friction D with the closest in-out asymmetry to the experiments.

\Rightarrow Physical diamagnetic and radial effects allows to robustly capture much stronger in-out asymmetries.



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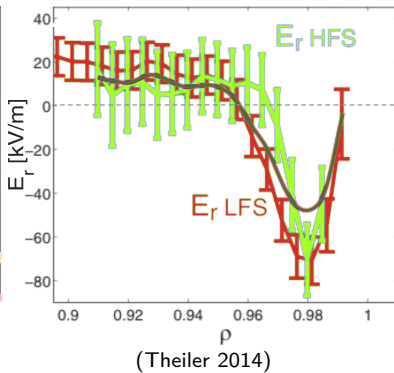
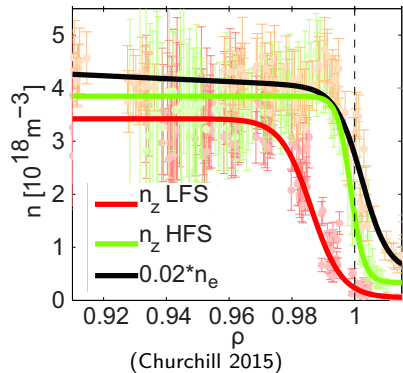
Quasineutrality \rightarrow Radial electric field poloidal variation

Explaining pedestal in-out asymmetries

From quasineutrality and Maxwell-Boltzmann electron and main ions:

$$\underbrace{\frac{z_i}{z_z} \frac{\nabla_{\perp} (n_z - \langle n_z \rangle)}{n_z}}_{\text{More } \ominus n_z \text{ slope on HFS}}$$

$$\sim \frac{\nabla_{\perp} (\Phi - \langle \Phi \rangle)}{\frac{T_i}{z_i e}} \sim \boxed{-} \underbrace{\frac{E_r - \langle E_r \rangle}{\frac{T_i}{z_i e}}}_{E_r \text{ less } \ominus \text{ on HFS}}$$



Strong poloidal
impurity **density**
variation

\downarrow
Poloidal **radial**
electric field
variation in
agreement with
experiments.

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Pedestal profile alignment

Radial flux

Radial flux evaluation

Impurity confinement

I-mode explanation

Summary

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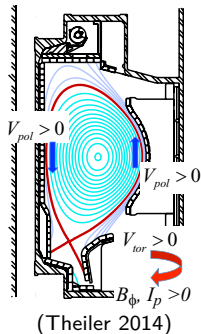
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Energy: Compressional heating → Poloidal temperature variation

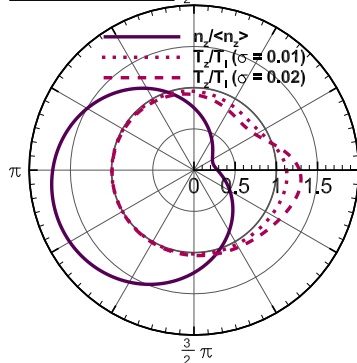
Explaining pedestal in-out asymmetries

Energy conservation equation for impurities:

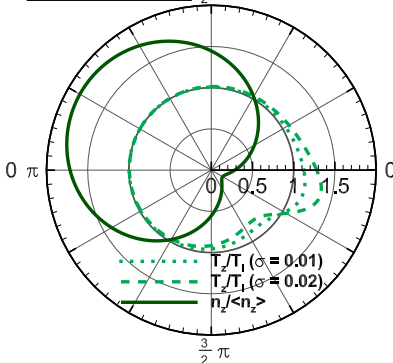
$$\underbrace{p_z \nabla \cdot \mathbf{V}_z}_{\text{Comp. heating}} = \underbrace{\frac{3}{2} n_z \nu_{zi} (T_i - T_z)}_{\text{Equilibration}} \Rightarrow \frac{T_z - T_i}{T_z} = \underbrace{\sigma(\psi)}_{\geq 0} (g + U + \alpha D) \frac{1}{n^2} \frac{\partial n}{\partial \vartheta}$$



$g + U + \alpha D < 0: \frac{1}{2} \pi$



$g + U + \alpha D > 0: \frac{1}{2} \pi$



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Conservation equations

Momentum → Pol. n var.

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I-mode explanation

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Impurity up-down asymmetry ⇒ Impurity temperature in-out asymmetry.

Pedestal impurity poloidal flow affects impurity accumulation

Explaining pedestal in-out asymmetries



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accumulation

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Motivation

Impurity accumulation
In-out asymmetries

Poloidal variation

Diamagnetic effects
Impurity flow effects
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10

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Pedestal profile alignment

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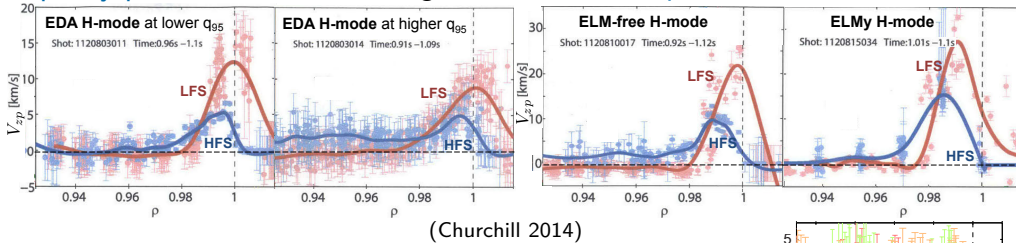
Radial flux evaluation
Impurity confinement
I-mode explanation

Summary

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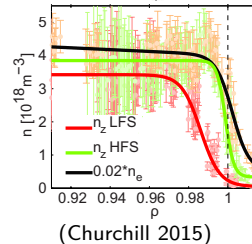
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Impurity poloidal flow: Much larger on the LFS and positive.



Without diamagnetic effects:
$$\frac{\mathbf{V}_z \cdot \nabla \theta}{\mathbf{B} \cdot \nabla \theta} = \overbrace{\chi_1(\psi)}^{\geq 0} \frac{g + U}{n}$$

↓
larger on LFS



\Rightarrow The impurity poloidal flow affects the radial impurity flux via $g + U$.

Pedestal impurity poloidal flow affects impurity accumulation

Explaining pedestal in-out asymmetries



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accumulation

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Motivation

Impurity accumulation
In-out asymmetries

Poloidal variation

Diamagnetic effects
Impurity flow effects
Conservation equations
Momentum \rightarrow Pol. n var.
 E_r poloidal variation
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10

Poloidal flow

Pedestal profile alignment

Radial flux

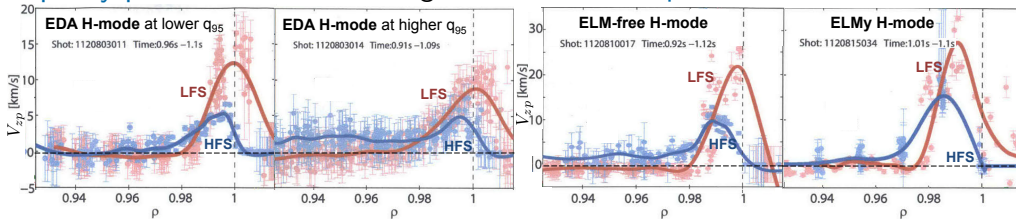
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I-mode explanation

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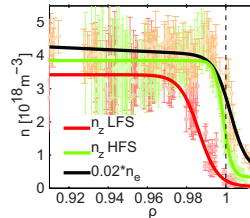


(Churchill 2014)

$$\frac{\mathbf{V}_z \cdot \nabla \theta}{\mathbf{B} \cdot \nabla \theta} = \underbrace{\chi_1(\psi)}_{\geq 0} \frac{g + U + \underbrace{\alpha D}_{\geq 0}}{n} + \underbrace{\chi_2(\psi)}_{\geq 0} \frac{\partial \ln n_z}{\partial \psi} (1 + \alpha n)$$

Even larger on LFS

Larger on LFS
(more – on HFS)



(Churchill 2015)

\Rightarrow Stronger poloidal variation of the impurity flow.

Pedestal impurity poloidal flow affects impurity accumulation

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accumulation

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Motivation

Impurity accumulation
In-out asymmetries

Poloidal variation

Diamagnetic effects
Impurity flow effects
Conservation equations
Momentum \rightarrow Pol. n var.
 E_r poloidal variation
Energy \rightarrow Poloidal T var.

10

Poloidal flow

Pedestal profile alignment

Radial flux

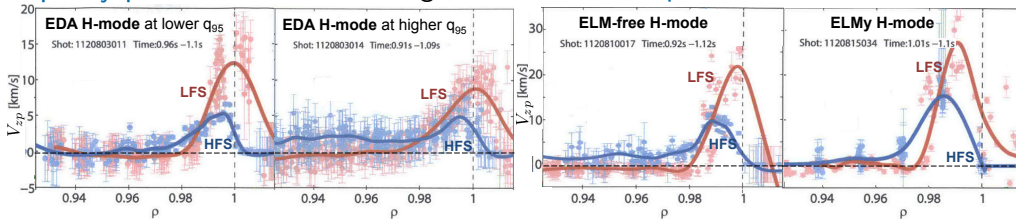
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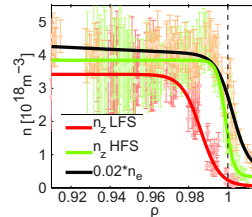


(Churchill 2014)

$$\frac{\overbrace{\mathbf{V}_z \cdot \nabla \theta}^{+}}{\mathbf{B} \cdot \nabla \theta} = \underbrace{\chi_1(\psi)}_{\geq 0} \frac{g + \underbrace{U + \alpha D}_n}{n} + \underbrace{\chi_2(\psi)}_{\geq 0} \frac{\partial \ln n_z}{\partial \psi} \underbrace{(1 + \alpha n)}_{-}$$

Even larger on LFS
Larger on LFS (more – on HFS)

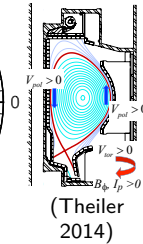
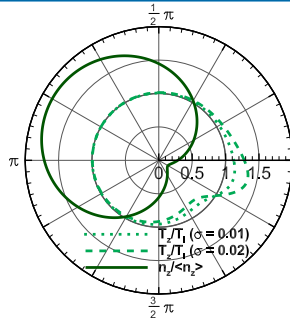
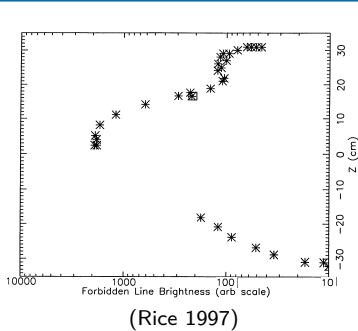
\Rightarrow For positive poloidal flow, $g + U + \alpha D \geq 0$.



(Churchill 2015)

Model predictions in agreement with experimental observations

Explaining pedestal in-out asymmetries



⇒ Upper impurity accumulation in agreement with the experiments.

Experimental physics captured	Us
Strong poloidal imp. density variation	✓
Weak poloidal imp. temperature variation	✓
Weak poloidal radial electric field variation	✓

- ✓ The measured impurity density and temperature **in-out asymmetry** can be **successfully captured without invoking anomalous transport**.
- ✓ Self-consistent '2D' **radial** and **impurity diamagnetic flow** effects!

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Impurity accumulation
In-out asymmetries

Poloidal variation

Diamagnetic effects
Impurity flow effects
Conservation equations
Momentum → Pol. n var.
 E_r poloidal variation
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11 Poloidal flow

Pedestal profile alignment

Radial flux

Radial flux evaluation
Impurity confinement
I-mode explanation

Summary

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Pedestal profile alignment: Total pressure with HFS temperature

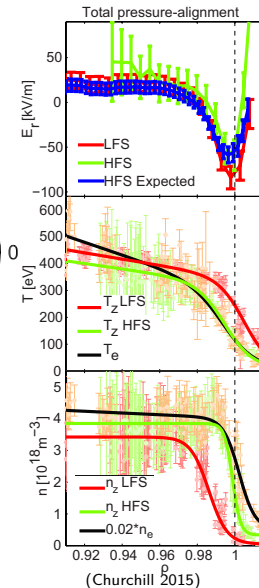
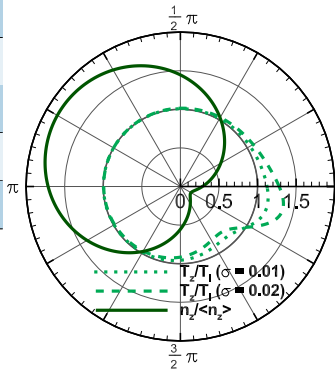
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Poloidal variation	Variables
Strong	n_z
Weak	$\cancel{T_z}, \cancel{E_r}$
Very weak	Φ, n_i, n_e
Flux functions	T_i, T_e

$$p_{tot} = n_e T_e + n_i T_i + \underbrace{n_z \cancel{T_z}}_{\substack{\downarrow \\ T_{z,HFS} \\ \sim \frac{z_i^2}{z_z} n_i T_i}}$$

⇒ Sharp prediction of the pedestal profile alignment: total pressure with inboard impurity temperature.



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Motivation

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In-out asymmetries

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Diamagnetic effects
Impurity flow effects
Conservation equations
Momentum → Pol. n var.
 E_r poloidal variation
Energy → Poloidal T var.
Poloidal flow

12

Pedestal profile alignment

Radial flux

Radial flux evaluation
Impurity confinement
I-mode explanation

Summary

Silvia
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16

Motivation

Impurity accumulation

In-out asymmetries

Poloidal variation

Diamagnetic effects

Impurity flow effects

Conservation equations

Momentum \rightarrow Pol. n var.

E_r poloidal variation

Energy \rightarrow Poloidal T var.

Poloidal flow

Pedestal profile alignment

13 Radial flux

Radial flux evaluation

Impurity confinement

I-mode explanation

Summary

Silvia
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Novel insight: Radial impurity flux from existing measurements

Radial flux measurement to avoid impurity accumulation

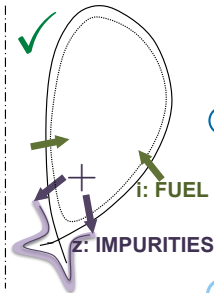
1. Large aspect ratio (without diamagnetic effects) \rightarrow *Espinosa & Catto, POP 2017*

$$\text{Radial impurity flux} \propto - \left\langle \frac{BR_{zi\parallel}}{1 + (b^2 - 1)} \right\rangle \stackrel{\substack{\text{Solubility:} \\ \langle BR_{zi\parallel} \rangle = 0}}{\downarrow} \underbrace{\left\langle BR_{zi\parallel} (b^2 - 1) \right\rangle}_{\text{Available measurements}} [1 + O(\epsilon)]$$

$$\text{Radial impurity flux} \propto - \left\langle \left(1 - b^2\right)^2 \right\rangle g + \left\langle (n - 1) (b^2 - 1) \right\rangle (g + U)$$

\uparrow \uparrow
 Radial profiles Computationally demanding
 $\propto \left(\frac{1}{2} \frac{\partial \ln T_i}{\partial \psi} - \frac{\partial \ln n_i}{\partial \psi} \right)$ kinetic calculation of full bulk ion response

\downarrow $2\epsilon^2$ \downarrow Imp. density
 $\epsilon \frac{n_{HFS} - n_{LFS}}{n_{HFS} + n_{LFS}}$



Motivation

Impurity accumulation
In-out asymmetries

Poloidal variation

Diamagnetic effects
Impurity flow effects
Conservation equations
Momentum \rightarrow Pol. n var.
 E_r poloidal variation
Energy \rightarrow Poloidal T var.
Poloidal flow
Pedestal profile alignment

Radial flux

13 Radial flux evaluation
Impurity confinement
I-mode explanation

Summary

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New realization: Radial impurity flux from existing measurements

Radial flux measurement to avoid impurity accumulation



Preventing
impurity
accumulation

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$$\begin{aligned}
 &\text{Radial impurity flux} \propto - \left\langle \left(1 - b^2\right)^2 \right\rangle g + \left\langle (n-1) \left(b^2 - 1\right) \right\rangle (g + U) \\
 &\quad \uparrow \text{Thomson scattering} \\
 &\quad \propto \left(\frac{1}{2} \frac{\partial \ln T_e}{\partial \psi} - \frac{\partial \ln n_e}{\partial \psi} \right)
 \end{aligned}$$

$2\epsilon^2$
 \downarrow
 $\epsilon \frac{n_{HFS} - n_{LFS}}{n_{HFS} + n_{LFS}}$ Imp. density
 $\propto \frac{n_z \mathbf{V}_z \cdot \nabla \theta}{\mathbf{B} \cdot \nabla \theta}$ Imp. pol. flow
 \downarrow

- ✓ Electron temperature profile twice as steep as the electron density or more.
- ✓ HFS impurity accumulation with poloidal flow in the magnetic field direction
OR LFS accumulation with poloidal flow in the opposite direction.

\Rightarrow Novel insight: The impurity radial flux can be obtained from measurements currently available, bypassing the computationally demanding kinetic calculation.

Techniques for actively preventing impurity accumulation

Radial flux measurement to avoid impurity accumulation



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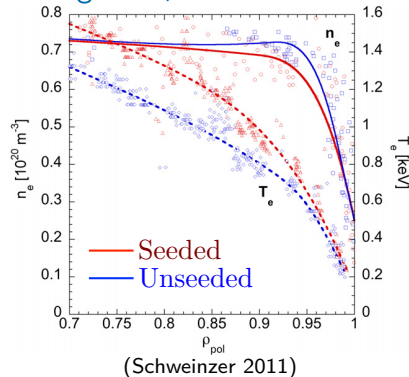
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2. General geometry with inertia and plasma heating \rightarrow Espinosa&Catto,PPCF 2017

- Outboard \rightarrow Inertia
- Inboard \rightarrow Plasma heating (ICRH,NBI)
- $\uparrow \frac{\partial \ln T_e}{\partial \ln n_e} \rightarrow$ Seeding

$$\left\langle \frac{BR_{zi}}{n_z} \right\rangle = 0 \quad \rightsquigarrow \text{Relates} \left\{ \begin{array}{ll} \text{fluid } i \text{ (} g \text{)} & \checkmark \\ \text{kinetic } i \text{ (} U \text{)} & \\ \text{poloidal flow } z & \checkmark \end{array} \right.$$



\Rightarrow Solve the solubility condition for the kinetic effects, which cannot be measured, to express the radial impurity flux as a function of available diagnostics.

Theoretical explanation of impurity removal on I-mode

Radial flux measurement to avoid impurity accumulation



E.g. I-mode:

Radial impurity flux

$$\propto - \overbrace{\left\langle (1 - b^2)^2 \right\rangle}^{\text{Outward}} g + \overbrace{\left\langle (n - 1) (b^2 - 1) \right\rangle}^{\text{Outward (close to separatrix)}} (g + U)$$

Thomson scattering: -

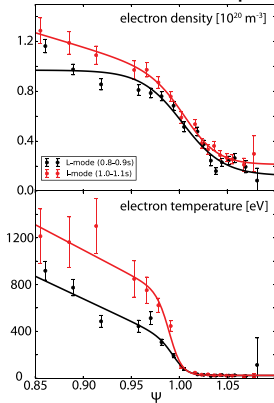
$$\propto \left(\frac{1}{2} \frac{\partial \ln T_e}{\partial \psi} - \frac{\partial \ln n_e}{\partial \psi} \right)$$

Imp.density: -

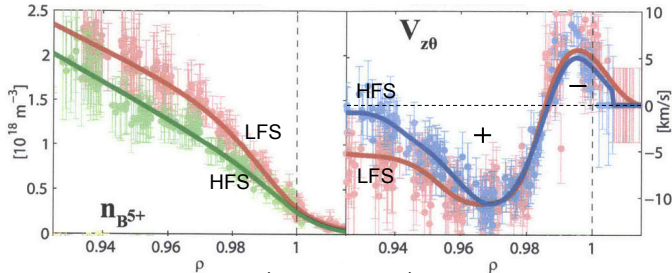
$$\propto \frac{n_{HFS} - n_{LFS}}{n_{HFS} + n_{LFS}}$$

Imp.pol.flow: +/-

$$\propto \frac{n_z \mathbf{V}_z \cdot \nabla \theta}{\mathbf{B} \cdot \nabla \theta}$$



(Walk 2014)



(Churchill 2014)

⇒ I-mode regime is favourable to avoid impurity accumulation.

Preventing impurity accumulation
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15

16

Theoretical explanation of impurity removal on I-mode

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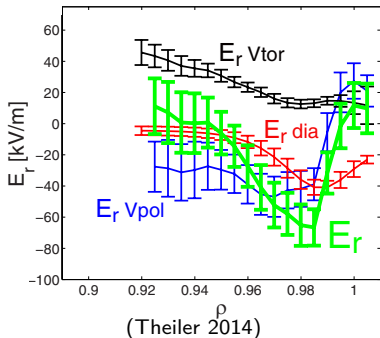
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E.g. I-mode:

Radial impurity flux



$$\propto - \overbrace{\left\langle (1 - b^2)^2 \right\rangle}^{\text{Outward}} g + \overbrace{\left\langle (n - 1) (b^2 - 1) \right\rangle}^{\text{Outward (close to separatrix)}} (g + U)$$

Thomson scattering: -

$$\propto \left(\frac{1}{2} \frac{\partial \ln T_e}{\partial \psi} - \frac{\partial \ln n_e}{\partial \psi} \right)$$

Imp.density: -

$$\propto \frac{n_{HFS} - n_{LFS}}{n_{HFS} + n_{LFS}}$$

Imp.pol.flow: +/-

$$\propto \frac{n_z \mathbf{V}_z \cdot \nabla \theta}{\mathbf{B} \cdot \nabla \theta}$$

\Rightarrow I-mode regime is favourable to avoid impurity accumulation, without invoking anomalous transport due to weakly coherent mode.

15

16

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- ✓ Self-consistent model with '2D' radial and impurity diamagnetic flow effects.
- ✓ Experimental values of impurity density, temperature and radial electric field in-out asymmetries successfully explained neoclassically.

2D diamagnetic \rightarrow Espinosa & Catto 2017, prep.

Density asymmetry \rightarrow "

Temperature asymmetry \rightarrow "

- ✓ First method of measuring the radial impurity flux from available diagnostics, without the need of a computationally demanding kinetic calculation.

- ✓ Outward neoclassical impurity flux and inward fueling found for I-mode.

Large aspect ratio \rightarrow Espinosa & Catto 2017, POP

General geometry \rightarrow Espinosa & Catto 2017, PPCF

I-mode \rightarrow Espinosa & Catto 2017, PRL sub.

16 Summary

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Preventing impurity accumulation

H-mode turbulence reduction & I-mode impurity removal

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