

Intrinsic rotation in tokamaks

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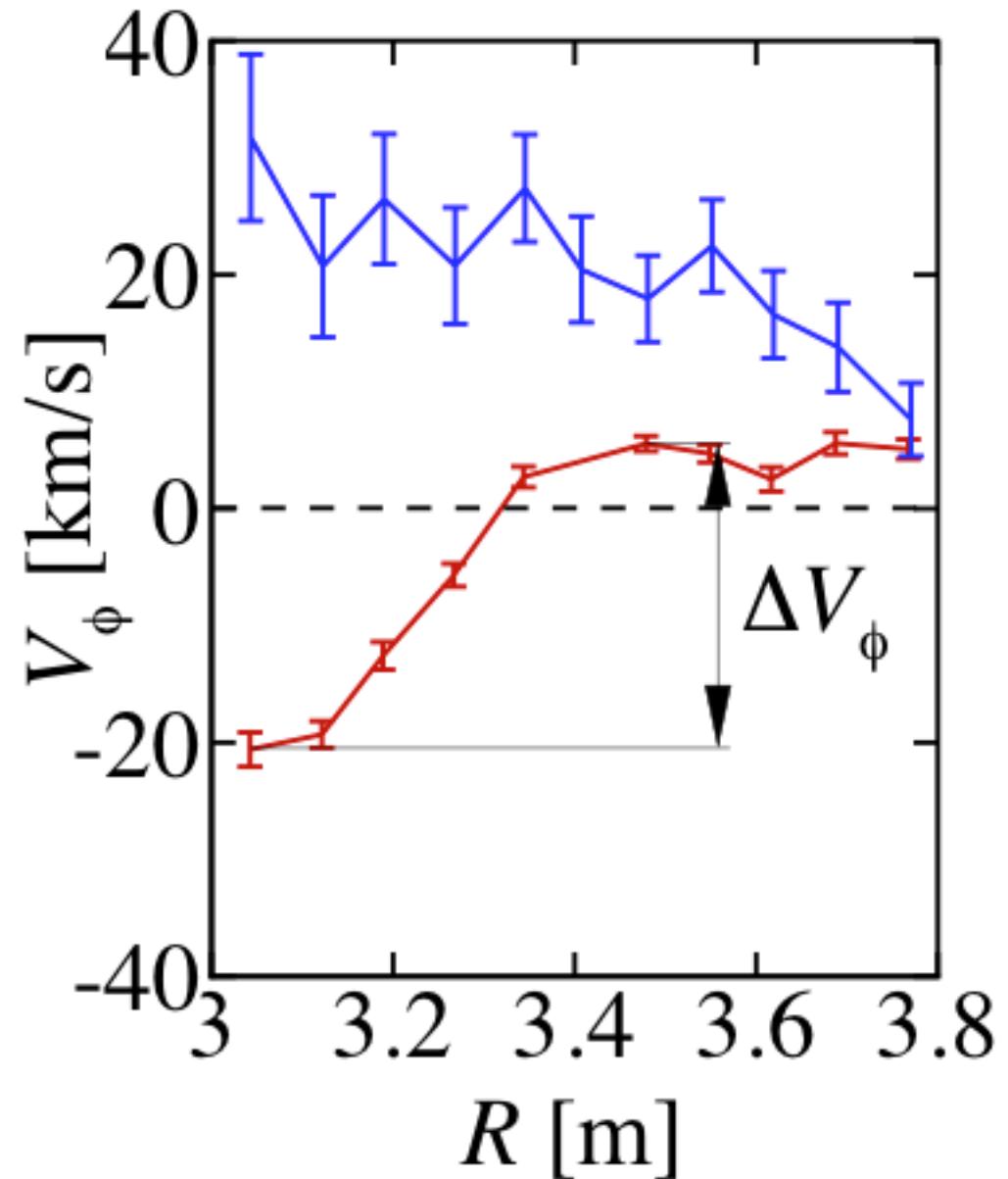
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Can we get large rotational shear for free?

- Recent observations of significant rotation (\sim Mach 0.3) without external momentum injection
- Important because difficult to force rotation in large, dense plasmas (i.e. ITER)
- Complicated dependence on experimental parameters



What sets intrinsic rotation?

- For small rotation and rotation gradient:

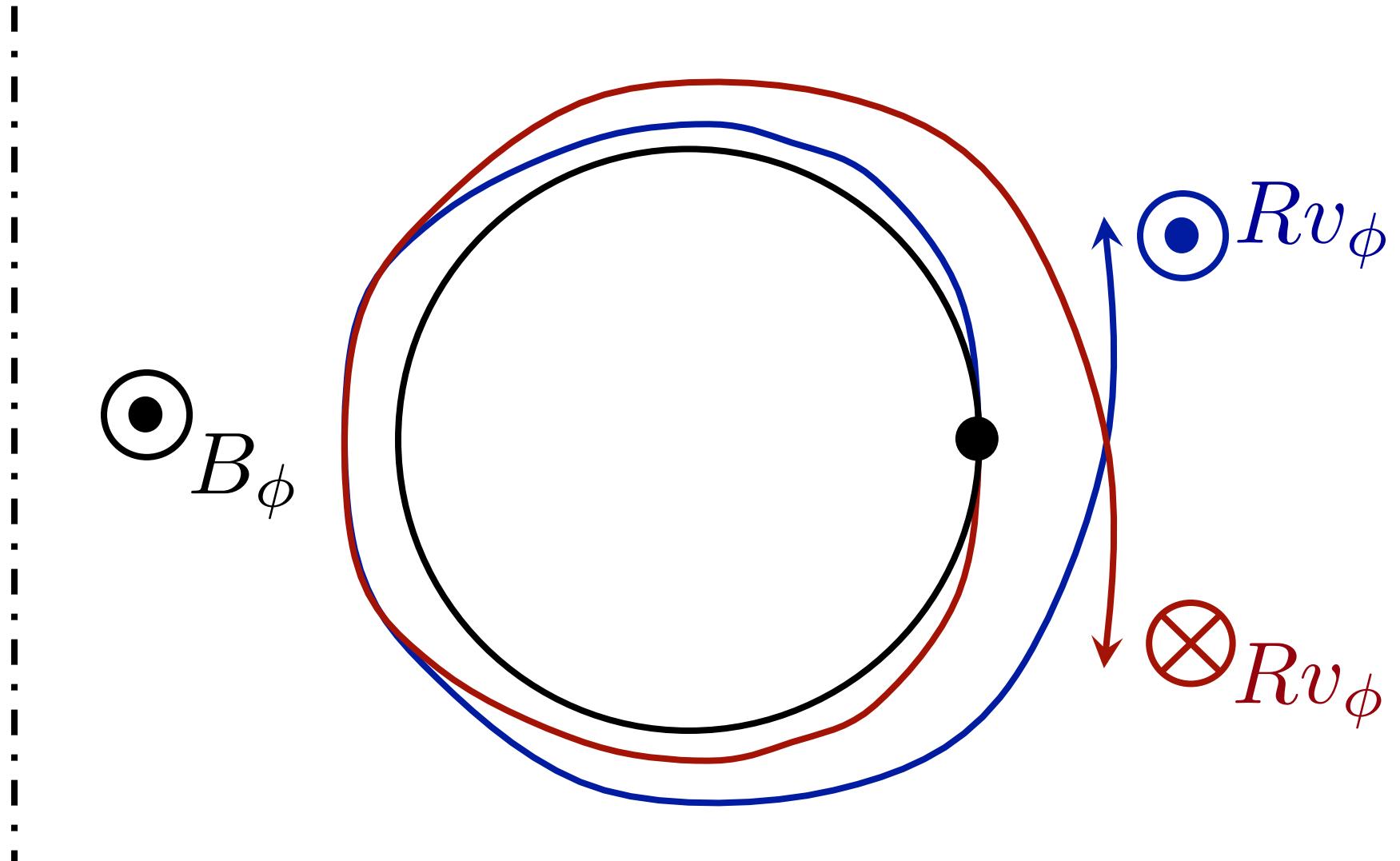
$$\Pi = -C\Omega_\zeta - \nu\Omega'_\zeta$$

- Steady-state with no momentum input ($\Pi = 0$):

$$\Omega_\zeta \propto \exp \left(- \int_0^\psi d\psi' \frac{C(\psi')}{\nu(\psi')} \right)$$

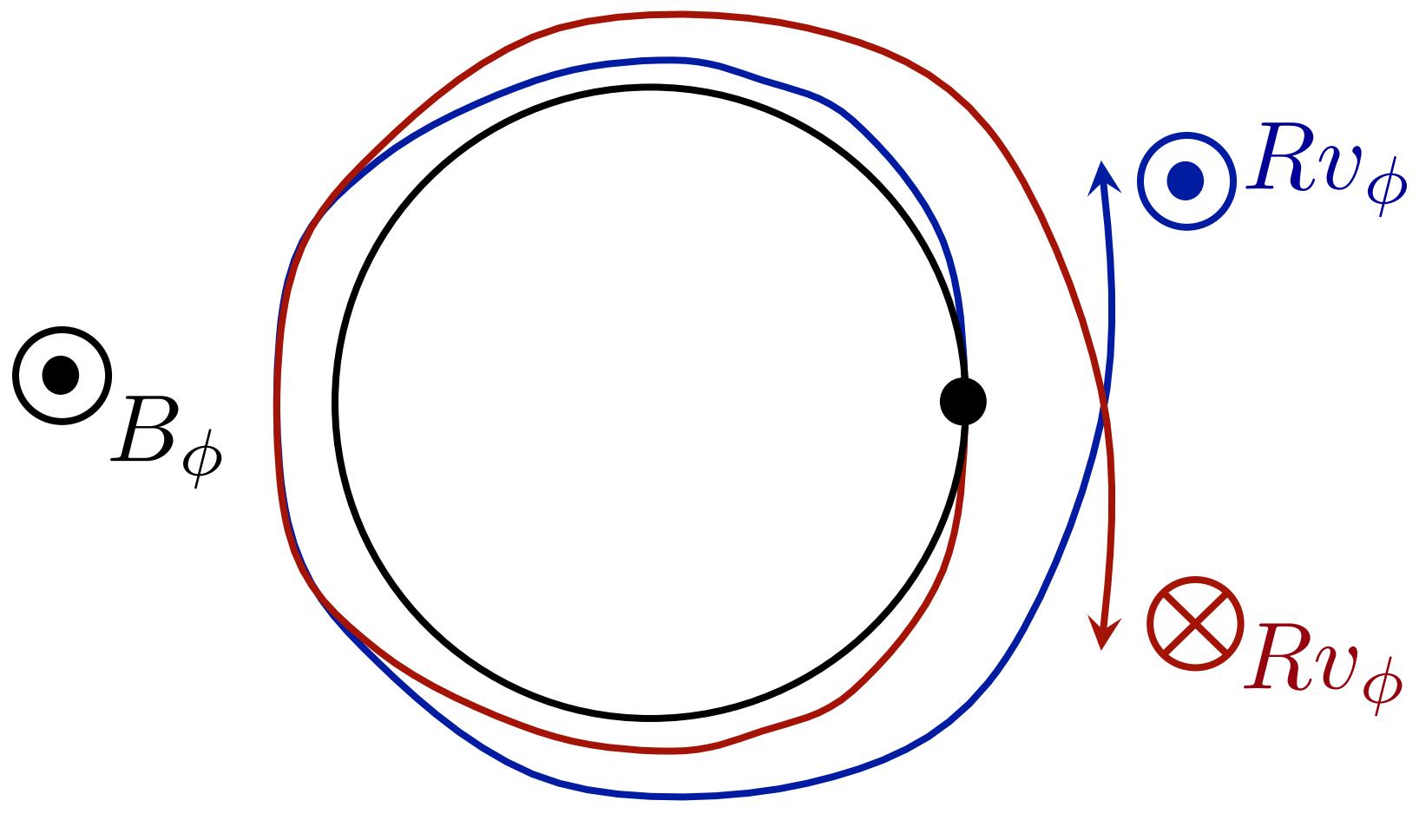
- No rotation sign reversal possible, so can't explain many experimental observations
- Must consider additional physics (not just diffusion + pinch)

Symmetry property



Symmetry property

No momentum transport from local turbulence in up-down symmetric system!



Symmetry of gyrokinetic system

- Lowest-order GK system invariant under up-down reflection about equatorial plane, reversal of rotation and rotation gradient, and

$$v_{\parallel} \rightarrow -v_{\parallel}, \quad \theta \rightarrow -\theta, \quad \partial_{\psi} \rightarrow -\partial_{\psi}$$

$$\delta f \rightarrow -\delta f, \quad \Phi \rightarrow -\Phi$$

- Consequently, momentum flux must vanish for zero rotation and rotation gradient (relevant for intrinsic rotation):

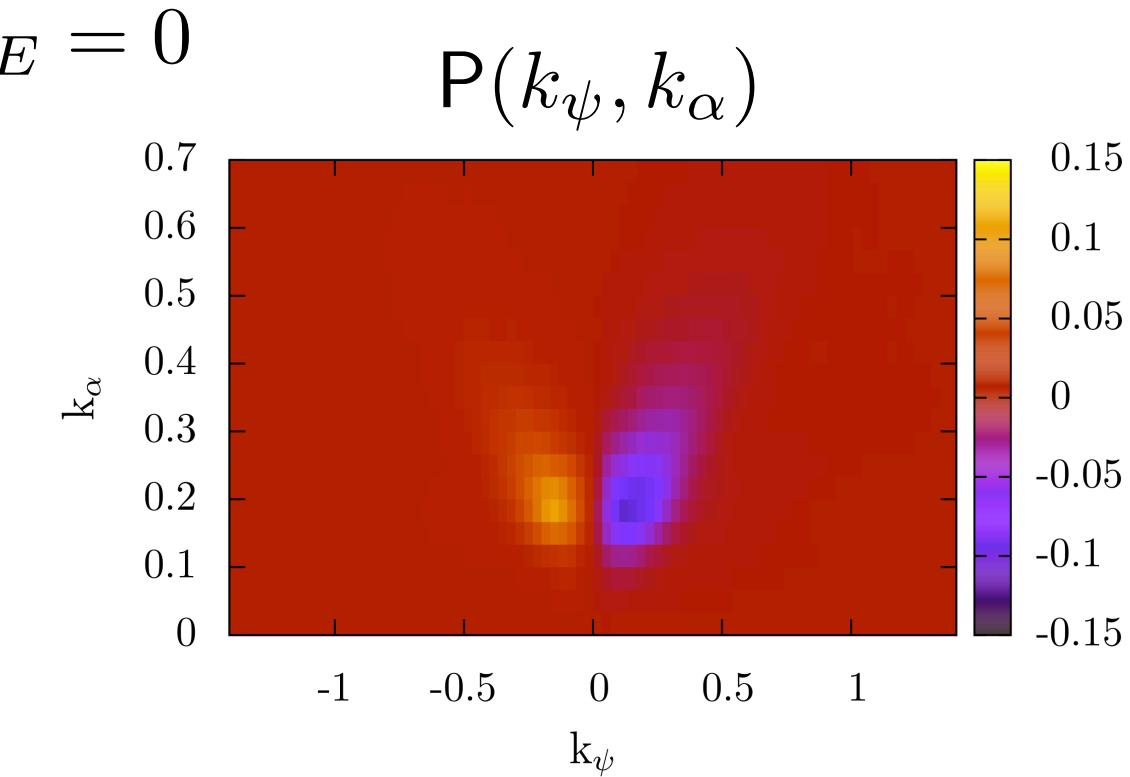
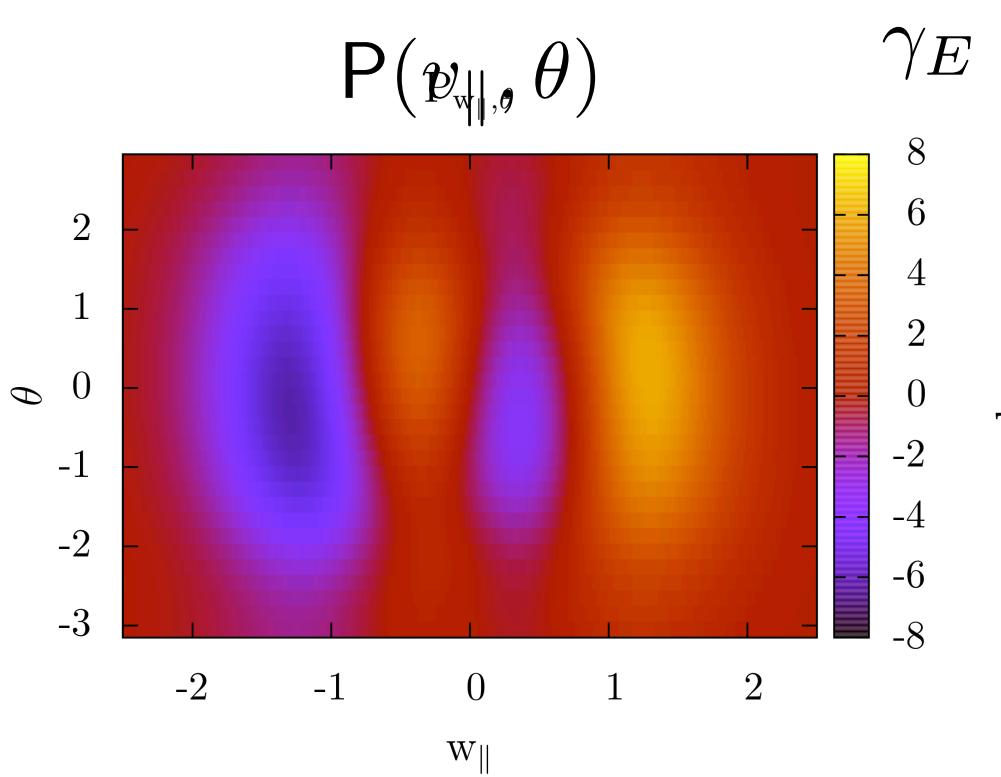
$$\Pi(\Omega_{\zeta}, \Omega'_{\zeta}) = -\Pi(-\Omega_{\zeta}, -\Omega'_{\zeta}) \Rightarrow \Pi(0, 0) = 0$$

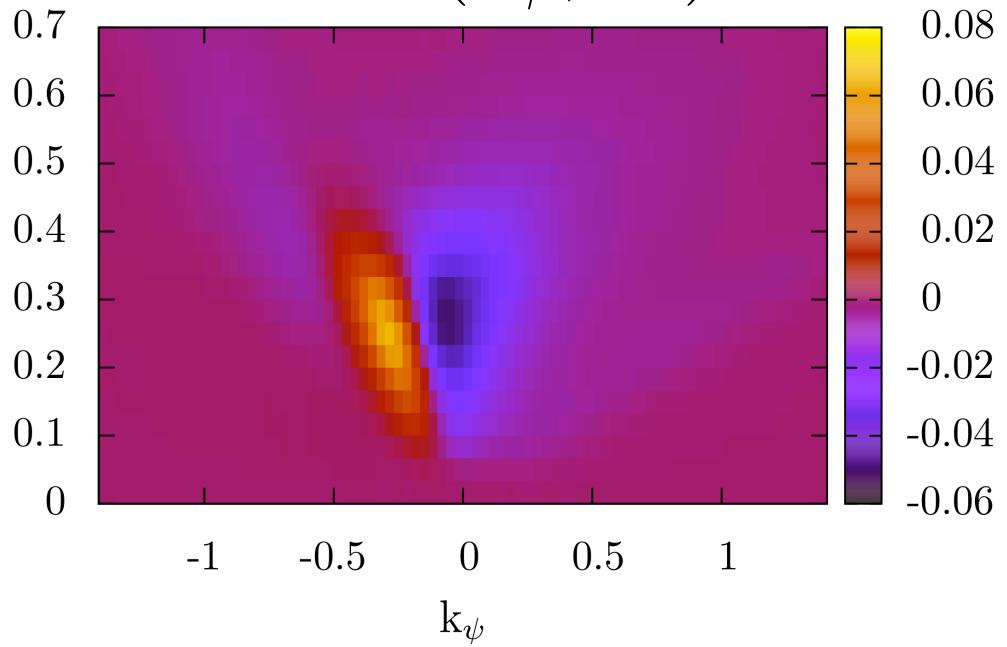
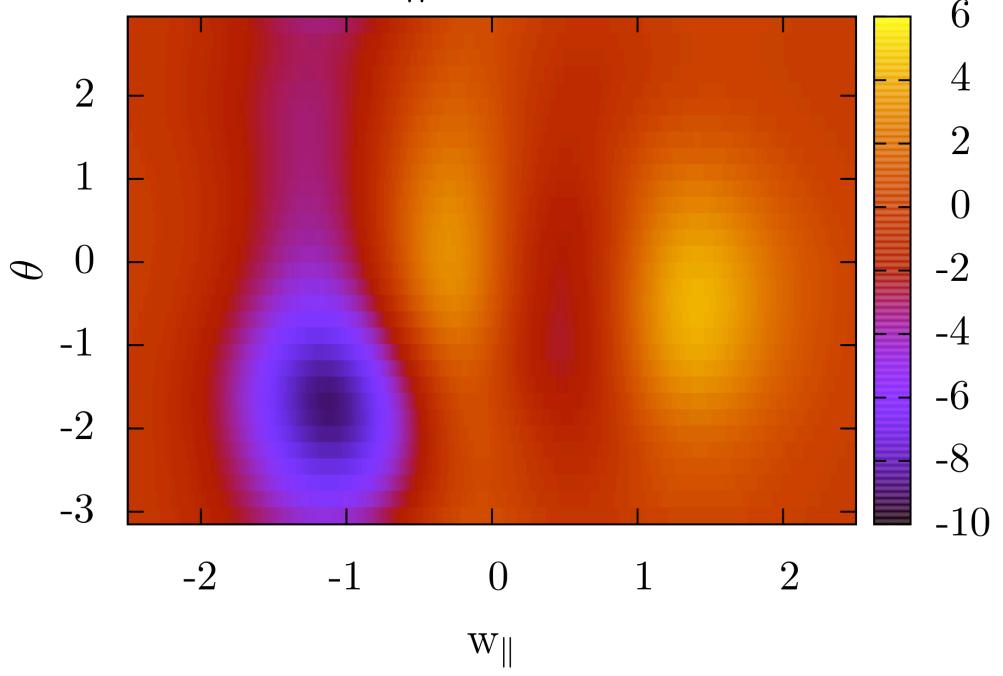
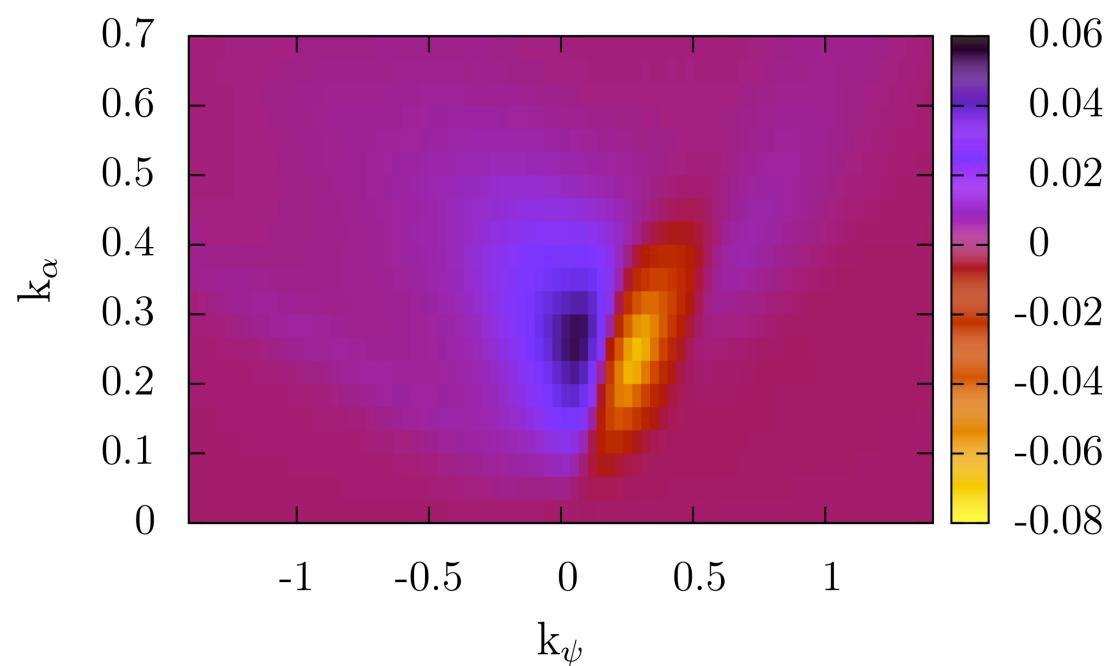
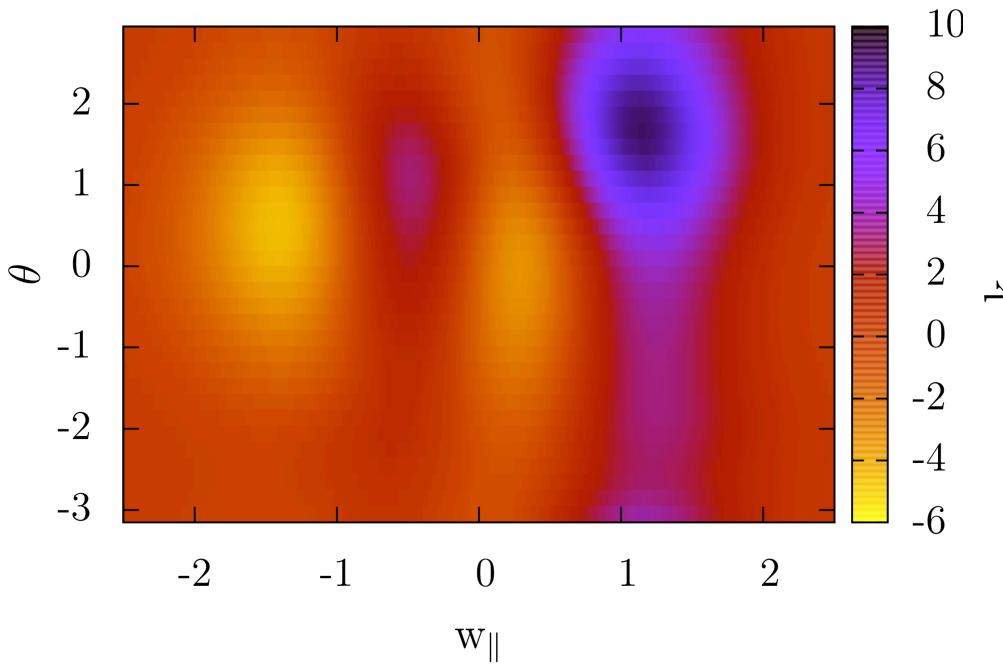
Symmetry in GS2 simulations

$P(\theta, k_\psi, k_\alpha, v_{\parallel}, \mu)$ is the time-averaged momentum flux integrand

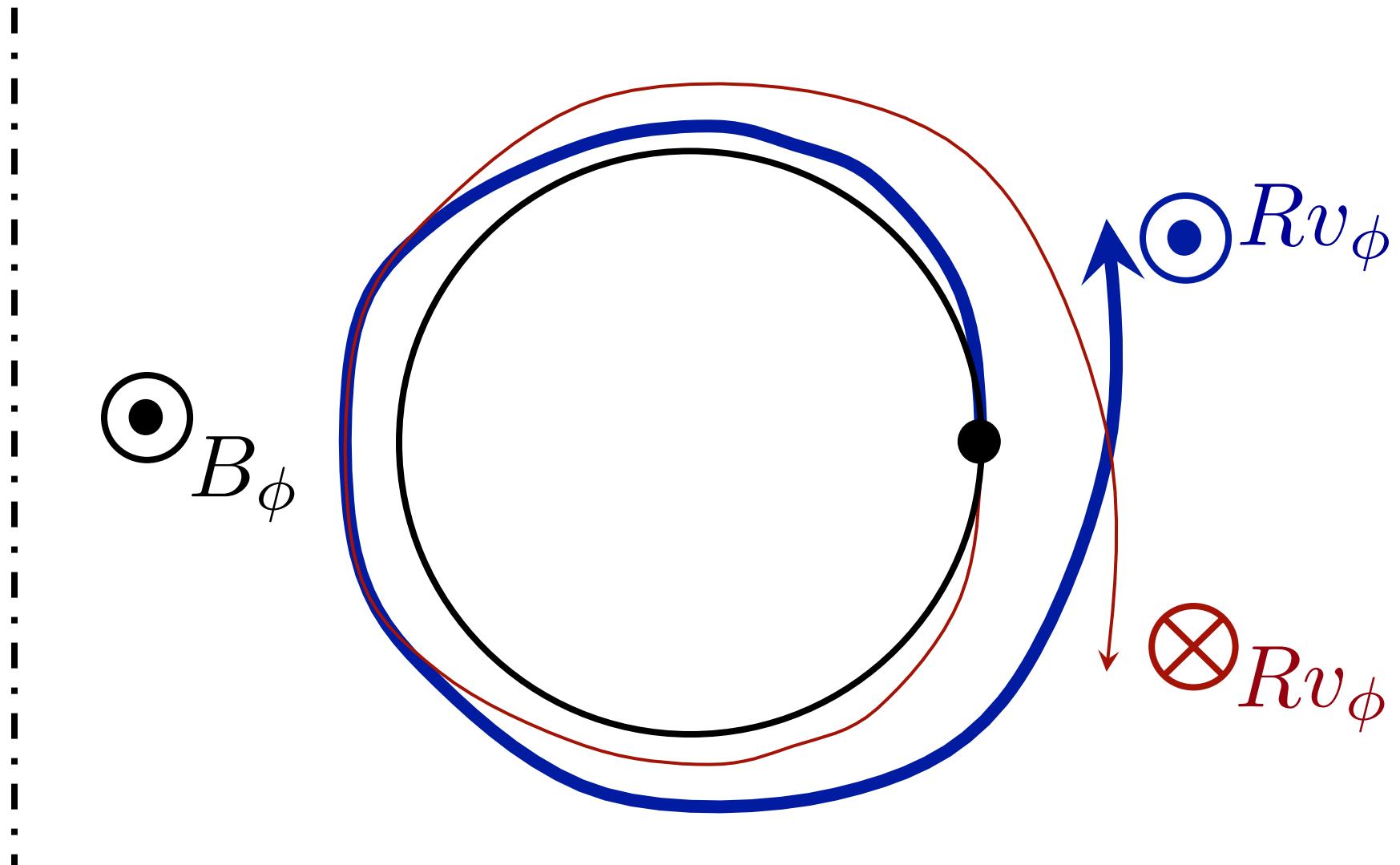
Symmetry constraints:

$$P(v_{\parallel}, \theta) = -P(-v_{\parallel}, -\theta) \quad P(k_\psi, k_\alpha) = -P(-k_\psi, k_\alpha)$$

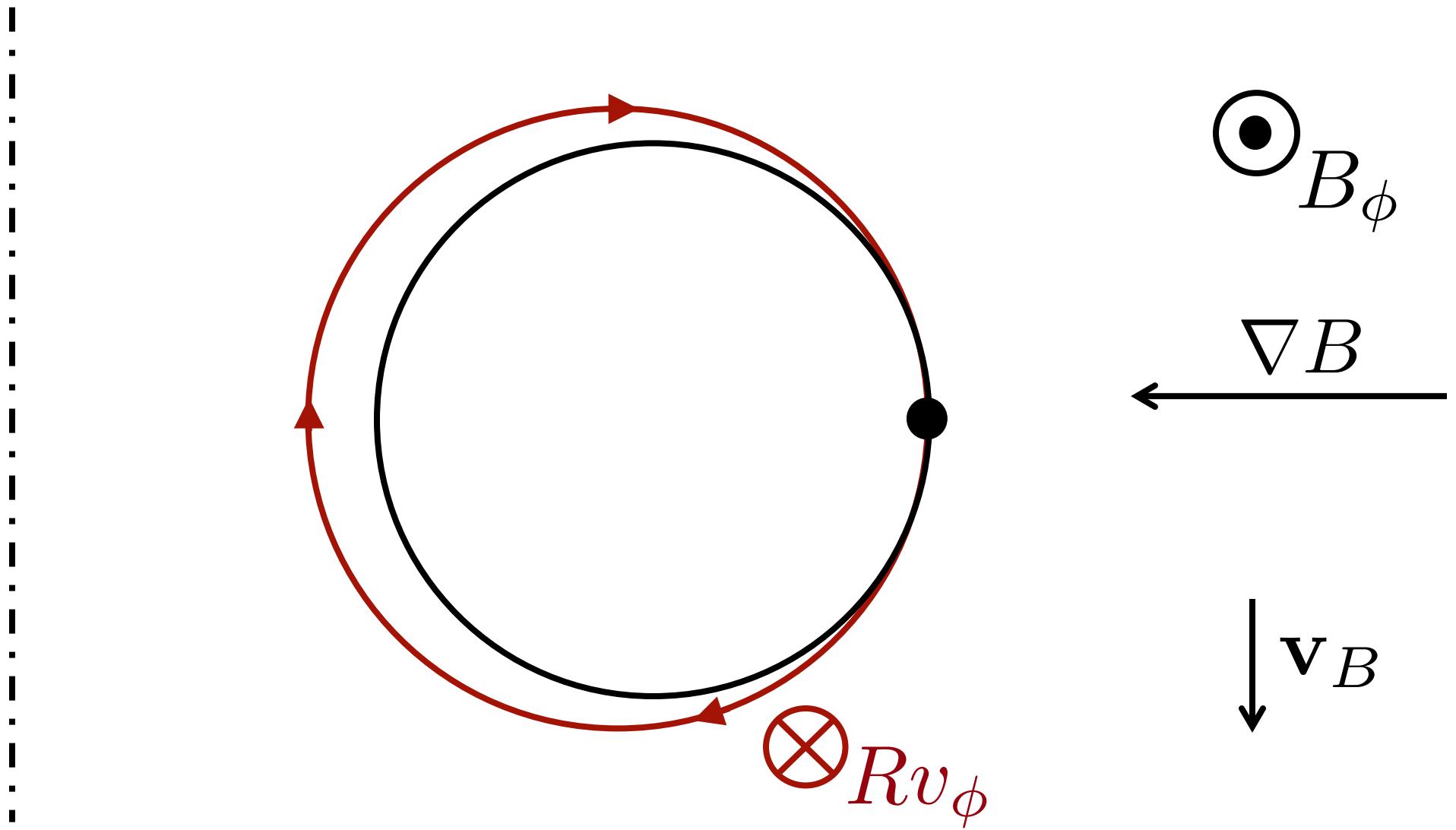


$P(v_{\parallel}, \theta)$ $\gamma_E = 0.2(v_{\text{th}}/R)$ $P(k_{\psi}, k_{\alpha})$  $\gamma_E = -0.2(v_{\text{th}}/R)$ 

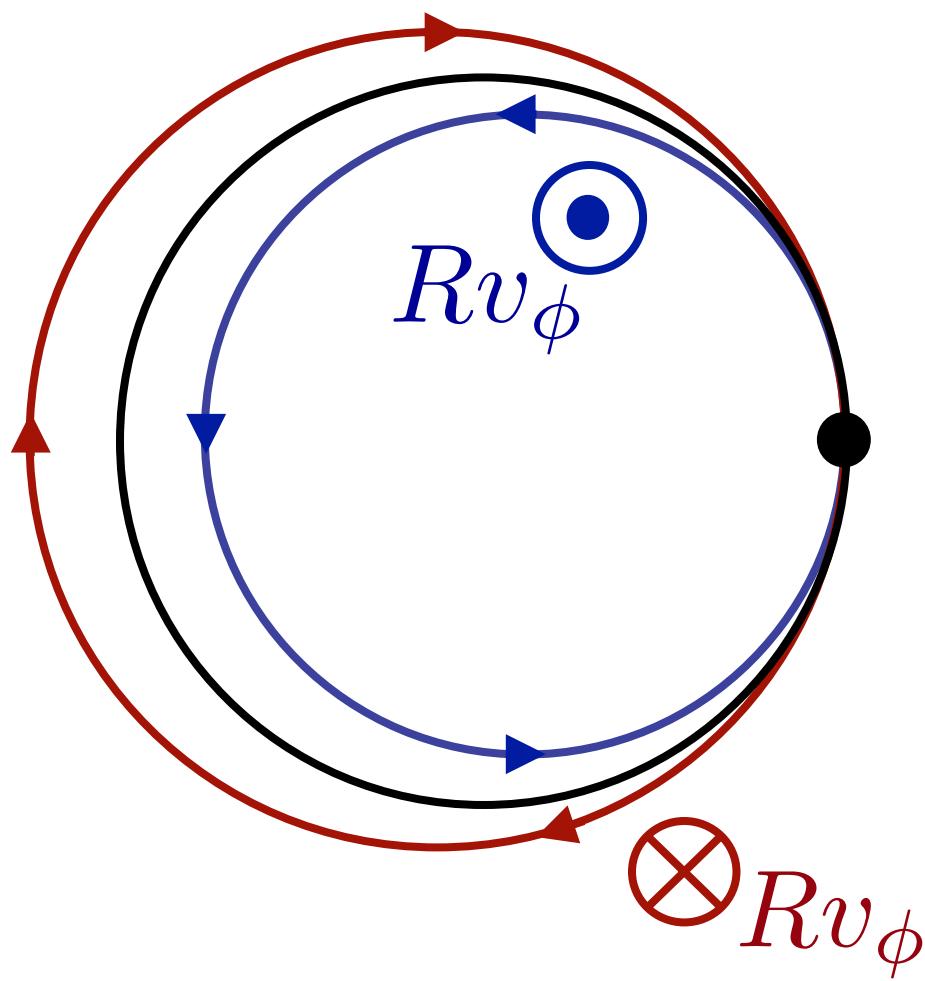
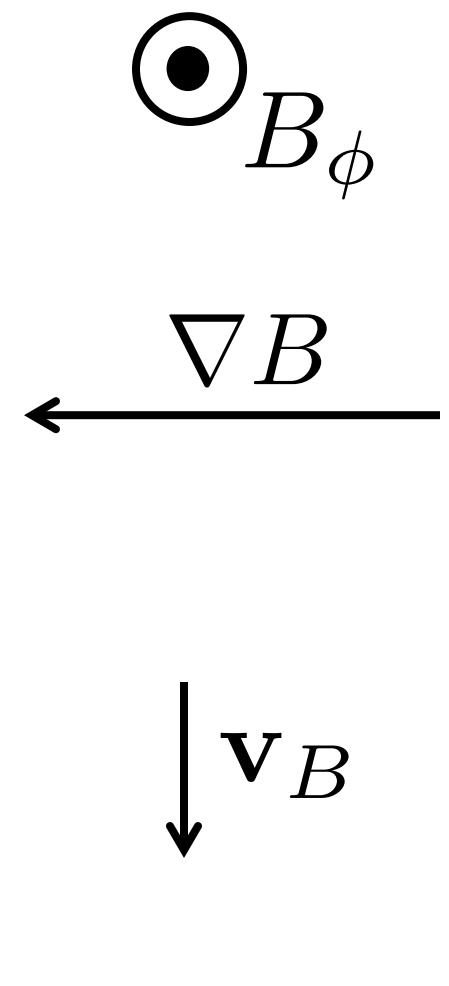
Symmetry breaking: mean flow



Mean flow generation

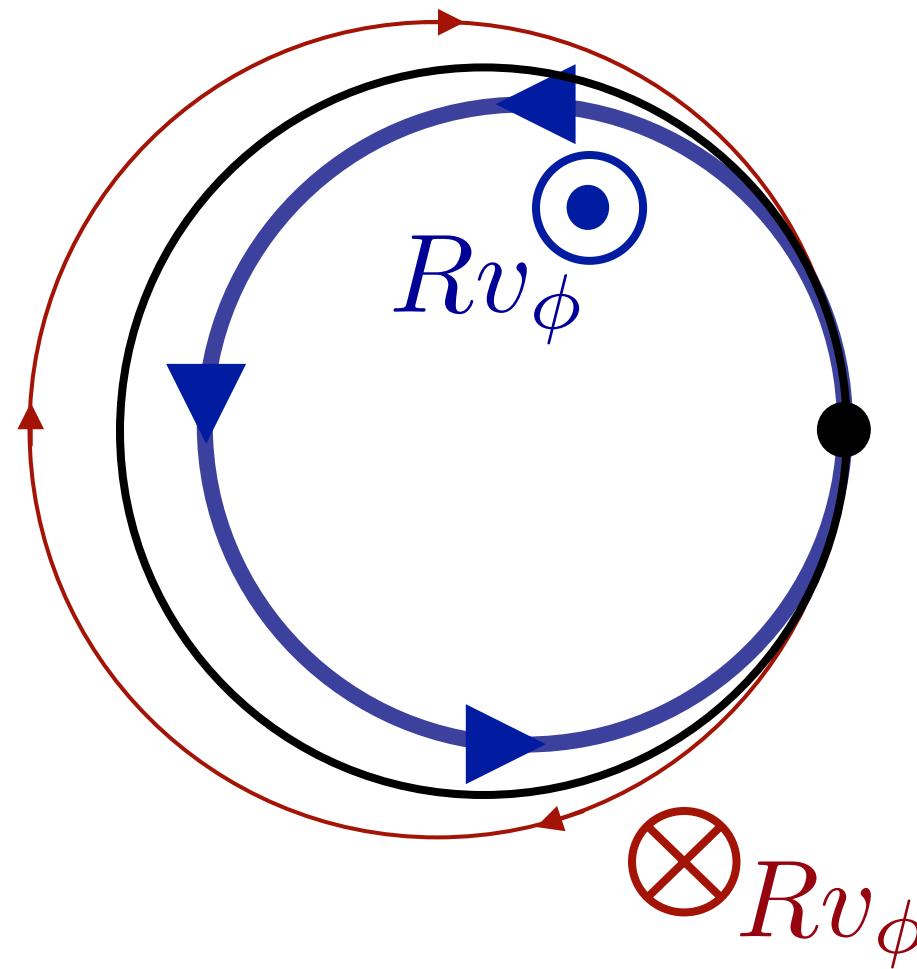


Mean flow generation



Mean flow generation

$$u \propto \Delta r \frac{d \ln p}{dr} v_t \sim \frac{\rho_\theta}{L_p} v_t$$



How big is the effect?

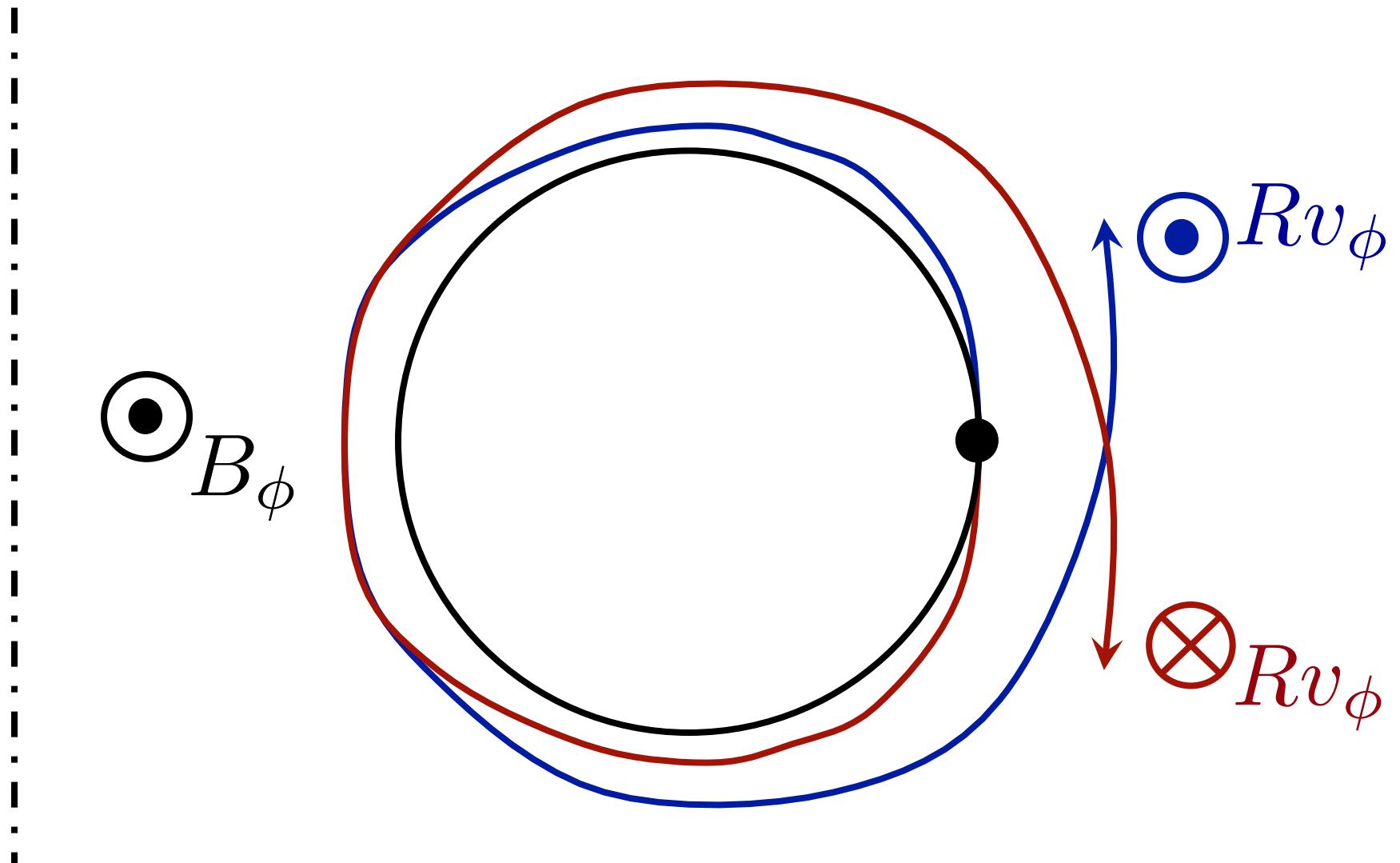
$$u \propto \Delta r \frac{d \ln p}{dr} v_t \sim \frac{\rho_\theta}{L_p} v_t$$

$$\Pi = -mRn\nu\frac{du}{dr}, \quad Q = -n\chi\frac{dT}{dr}$$

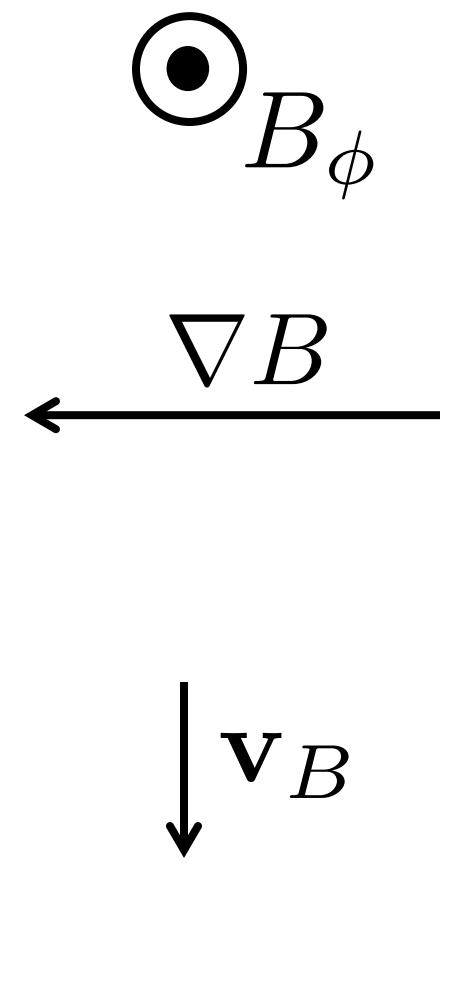
$$\nu \sim \chi \sim qR\frac{\rho_\theta^2}{v_t}$$

$$\frac{\Pi}{Q}\frac{Q_{GB}}{\Pi_{GB}} \sim mv_t\frac{du}{dr}\left(\frac{dT}{dr}\right)^{-1} \sim \rho_i\left(\frac{dT}{dr}\right)^{-1}\frac{d}{dr}\left(\frac{q}{\epsilon}\frac{dT}{dr}\right)$$

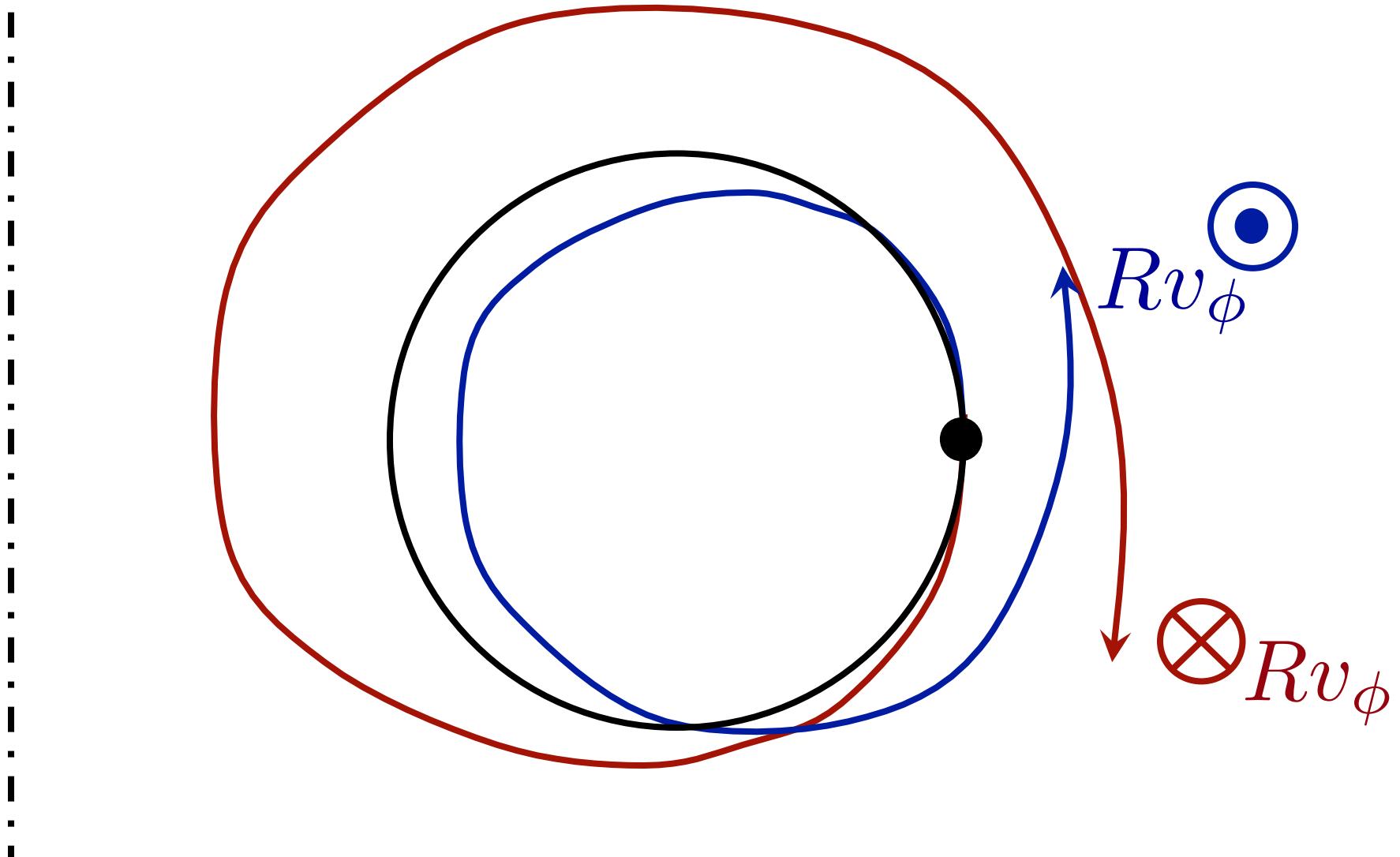
Symmetry breaking: up-down asymmetry



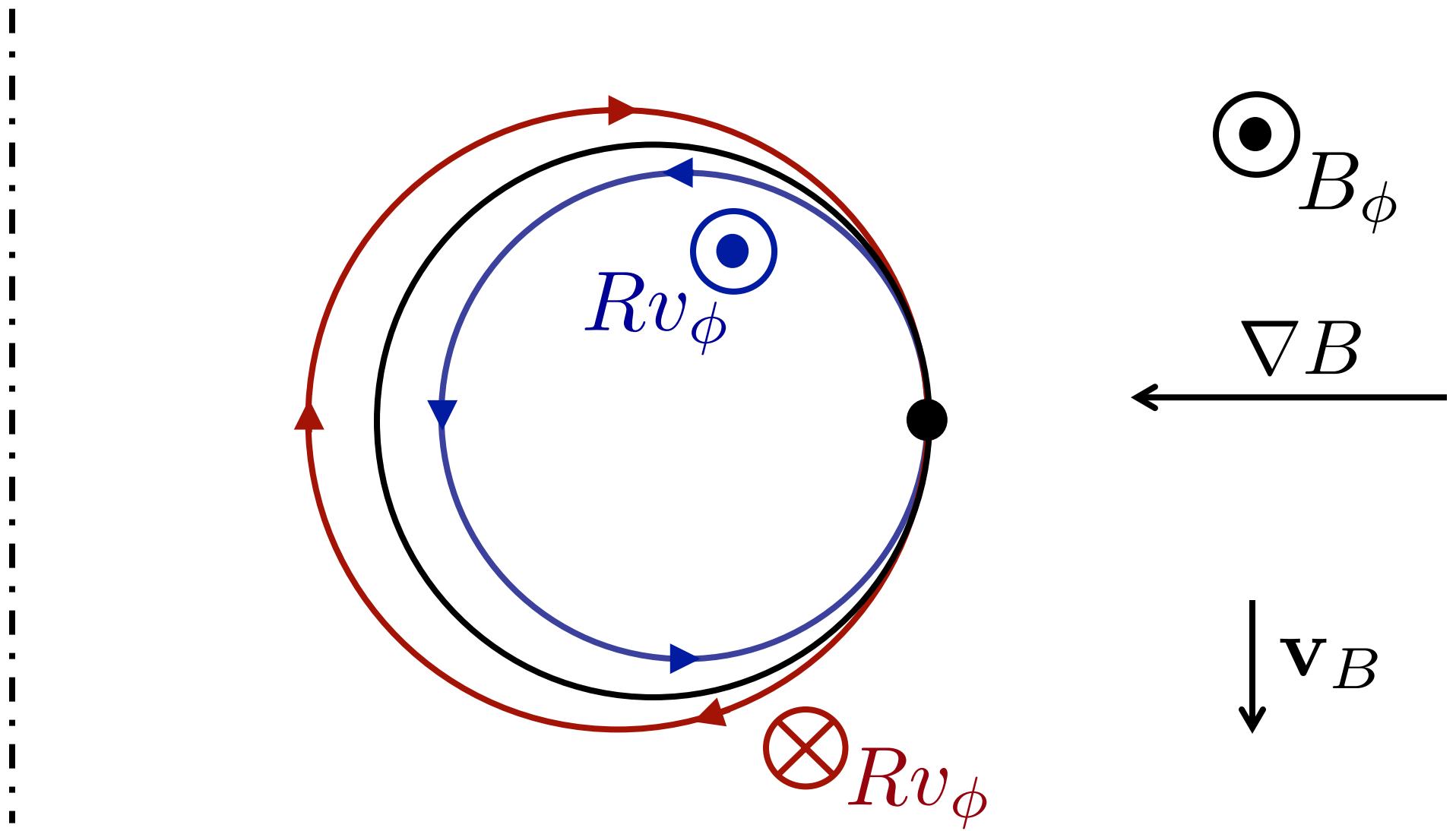
Symmetry breaking: orbit length



Symmetry breaking: orbit length



Symmetry breaking: radial profile variation



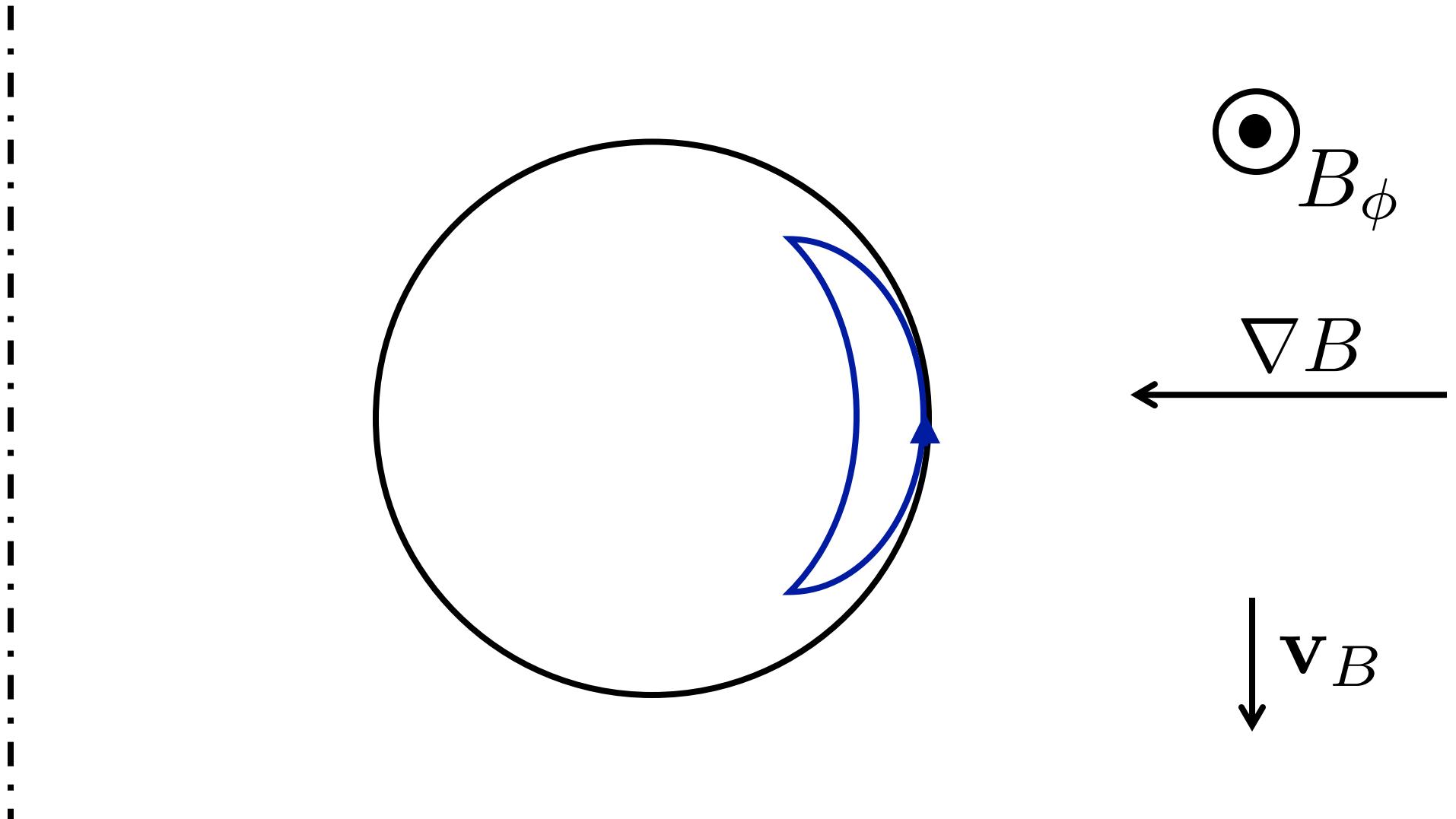
Higher-order GK equation (B_θ/B small)

(R,E, μ) variables

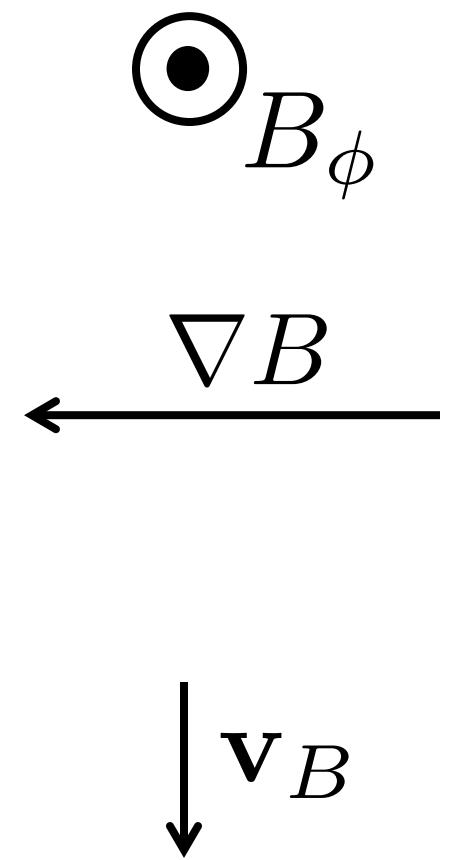
Parra, Barnes, and Catto, Nucl. Fusion (2011).

$$\begin{aligned}
 \frac{dg_s}{dt} + \mathbf{v}_\parallel \cdot \nabla \left(g_s - Z_s e \langle \Phi \rangle \frac{\partial F_{0s}}{\partial E} \right) + \langle \mathbf{v}_E^\perp \rangle \cdot \nabla F_{0s} \\
 + (\mathbf{v}_{Cs} + \mathbf{v}_{Ms} + \langle \mathbf{v}_E^\perp \rangle) \cdot \nabla_\perp \left(g_s - Z_s e \langle \Phi \rangle \frac{\partial F_{0s}}{\partial E} \right) \\
 = - \mathbf{v}_{Ms} \cdot \nabla \theta \frac{\partial}{\partial \theta} \left(g_s - Z_s e \langle \Phi \rangle \frac{\partial F_{0s}}{\partial E} \right) - \langle \mathbf{v}_E^\parallel \rangle \cdot \nabla_\perp g_s \\
 - \langle \mathbf{v}_E^\perp \rangle \cdot \nabla \theta \frac{\partial g_s}{\partial \theta} - \langle \mathbf{v}_E^\parallel \rangle \cdot \nabla F_{0s} - \langle \mathbf{v}_E^\perp \rangle \cdot \nabla F_{1s} \\
 + Z_s e \left(\mathbf{v}_\parallel \cdot \nabla \langle \Phi \rangle + \mathbf{v}_{Ms} \cdot \nabla_\perp \langle \Phi \rangle \right) \left(\frac{\partial g_s}{\partial E} + \frac{\partial F_{1s}}{\partial E} \right) \\
 - \mathbf{v}_E^{nc} \cdot \nabla_\perp g_s + Z_s e \mathbf{v}_\parallel \cdot \nabla \Phi^{nc} \frac{\partial g_s}{\partial E} + \psi\text{-profile variation}
 \end{aligned}$$

Symmetry breaking



Symmetry breaking



Symmetry breaking

