

Gyrokinetic Microtearing Studies

C M Roach

summarising work involving many collaborators:

D J Applegate⁰, JW Connor, S C Cowley, D Dickinson¹, W Dorland²,
R J Hastie, S Saarelma, A A Schekochihin³ and H R Wilson¹

Euratom/CCFE Fusion Association, Culham Science Centre, UK

⁰ SERCO

¹ University of York, UK

² University of Maryland, US

³ University of Oxford, UK

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Outline of the Talk

Summary of mostly old gyrokinetic simulations of microtearing modes in STs, using GS2.

- (1) Tearing Parity Modes and Simulation Literature
- (2) Microtearing Mode in MAST
- (3) Contact with Analytic Theory
- (4) Nonlinear Simulations
- (5) Key Questions

Eigen-Mode Parity along Equilibrium Magnetic Field is Even or Odd

Local ballooning space represents physical quantities as twisting slices:

$$F(x, y, \theta) = e^{ik_y(y+s(\theta-\theta_0)x)} \sum_{p=-\infty}^{\infty} \hat{F}(\theta - \theta_0 - 2\pi p) e^{inq(x)2\pi p}$$

fast \perp variation *slow \parallel variation*

x is equ'm flux surface label, $x=0$ at $q(x)=m/n$

y equ'm field line label, \perp to \mathbf{b} , lying in the flux surface

θ is \parallel to \mathbf{b}

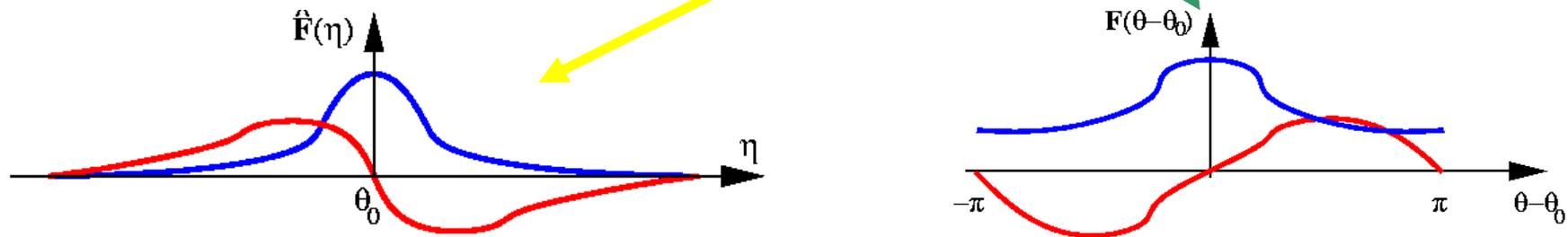
\hat{F} is defined on infinite domain in the ballooning angle η ,
 θ_0 is the ballooning parameter.

$$\hat{F}(\eta) \rightarrow 0 \quad \text{as } \eta \rightarrow \pm\infty$$

\hat{F} eigenfunctions are either even or odd in η , about $\eta = \theta_0$

Tearing Parity Modes

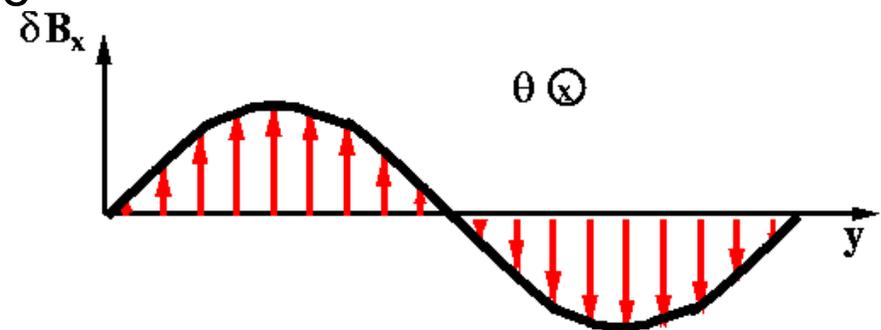
At $x=0$, the parity of $\hat{F}(\eta)$ about $\eta = \theta_0$ in ballooning space determines the symmetry of F along the field line in real space



Perturbed magnetic field comes from $\delta\mathbf{B} = \nabla \times \delta\mathbf{A}$
 \Rightarrow radial component: $\delta B_x = \partial A_{\parallel} / \partial y = ik_y A_{\parallel}$

A_{\parallel} even, conclude for $x=0$ that

- $\Rightarrow \delta B_x$ same sign along equ'm field line
- $\Rightarrow \delta B_x$ sinusoidal in y at fixed θ
- \Rightarrow equilibrium field lines are torn!



Even A_{\parallel} implies tearing of magnetic flux surface $x=0$

Some Gyrokinetic Microtearing Mode Simulations in the Literature

Microtearing found in study high β and high performance plasmas:

- M Kotschenreuther *et al*, Nuclear Fusion **40**, 677 (2000) GS2

Often dominant instabilities for $k_y \rho_i < 1$ at mid-radius in MAST plasmas:

- D J Applegate *et al*, Phys Plasmas **11**, 5085 (2004) GS2
- C M Roach *et al*, PPCF **47**, B323 (2005)

Microtearing found to dominate ST Power Plant equilibrium:

- H R Wilson *et al*, Nuclear Fusion **44**, 917 (2004) GS2

Detailed numerical study of microtearing, ST reference, includes scan in R/a:

- D J Applegate *et al*, PPCF **49**, 1113 (2007) GS2

Nonlinear analytic theory of μ -tearing may explain electron transport in NSTX

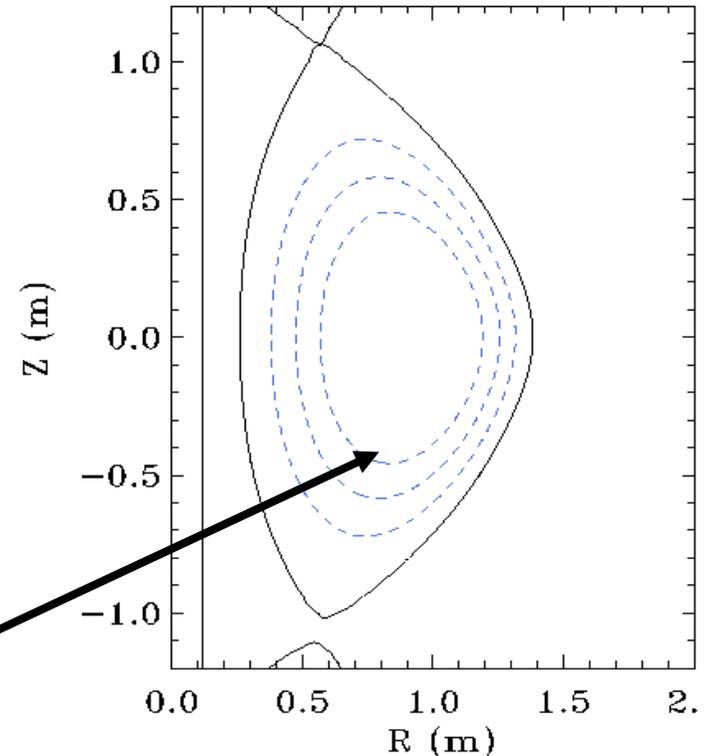
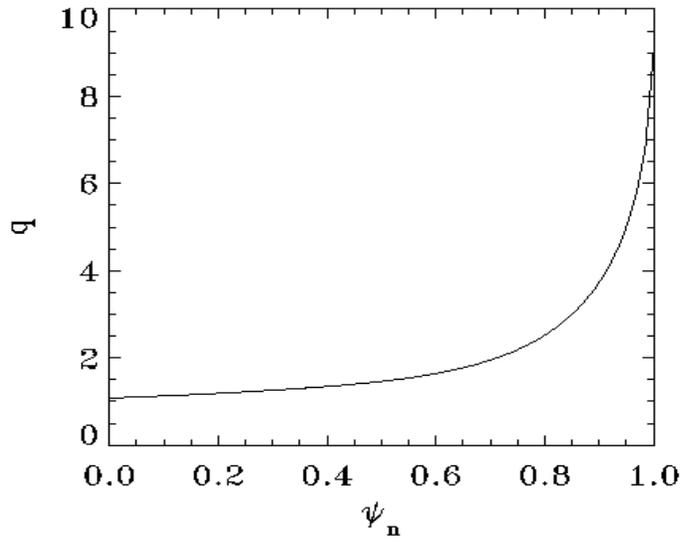
- K L Wong *et al*, Phys. Rev. Lett. **99**, 135003 (2007)

Edge plasmas in ASDEX-Upgrade have μ -tearing modes

- D Told *et al*, Phys. Plasmas **15**, 102306 (2008)

Linear Microstability Analysis at Mid-Radius in MAST

MAST equilibrium from ELMy H-Mode #6252



At mid-radius surface $\Psi_n=0.4$,
 $\beta_e=0.05$, $q \sim 1.35$ $T_i \sim T_e$, $a \sim 0.3$ m, $R \sim 0.9$ m $\Rightarrow R/a \sim 3$

See Applegate *et al*, Physics of Plasmas (2004)

Tearing Parity Modes at ρ_i scale

Fastest growing modes in STs often found to have tearing parity:

- MAST [1], and NSTX [2]
- conceptual burning STs [3,4]

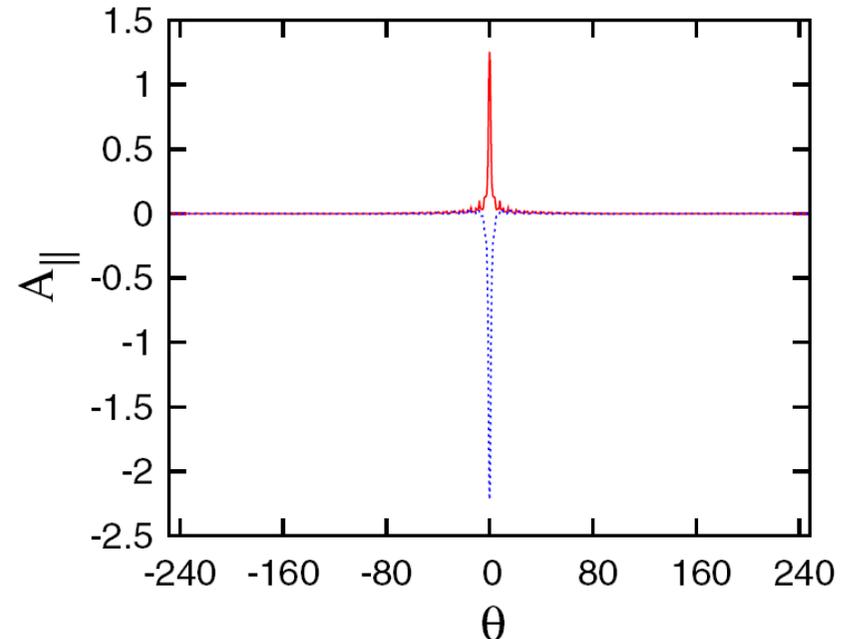
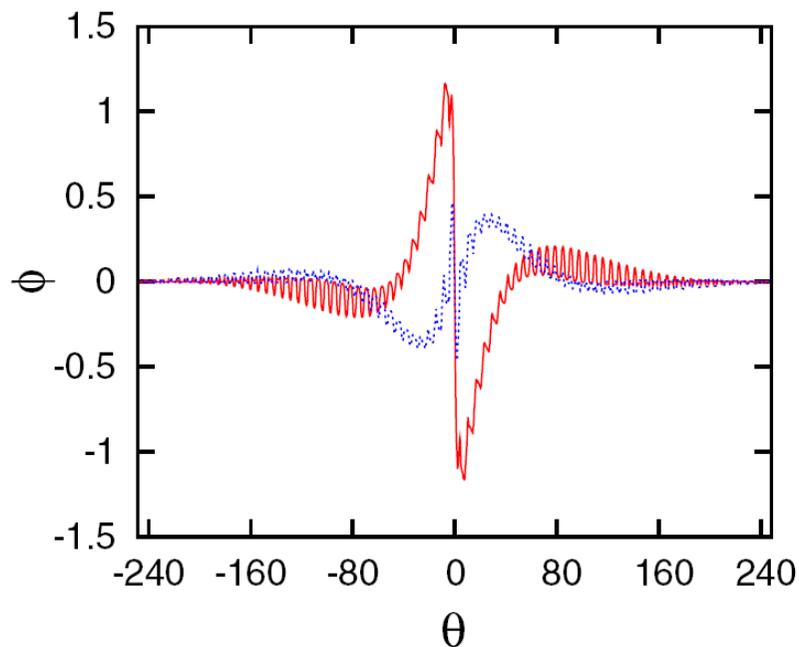
[1] Applegate *et al*, Phys Plasmas **11**, 5085, (2004).

[2] Redi et al, EPS, St Petersburg (2003)

[3] Kotschenreuther *et al*, Nuc Fus **40**, 677 (2000),

[4] H R Wilson et al, Nuclear Fusion, 44, 917 (2004)

MAST tearing parity modes rotate in **electron** diamagnetic drift direction



Visualising Micro-tearing Mode in Real Space

Poincaré plot shows perturbed magnetic field at intersection of GS2 flux-tube with the outboard mid-plane.

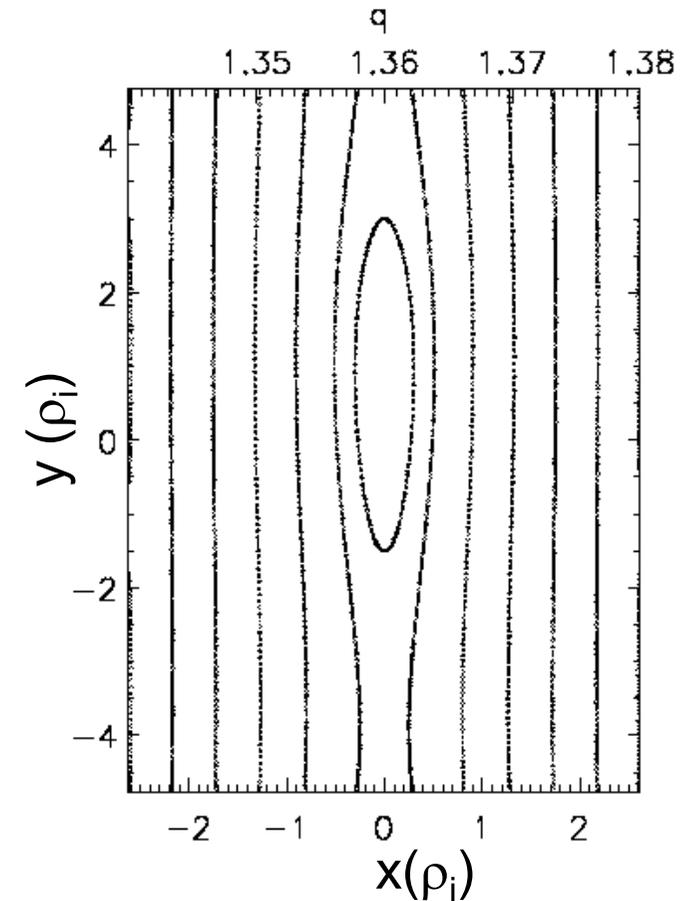
Magnetic island on rational surface at $x=0$.

Microtearing mode is candidate to explain electron transport

Two Major Questions:

What is the linear physics mechanism underlying these modes?

How much anomalous transport is generated at nonlinear saturation?



Analytic Theories of Microtearing Instabilities

∇T_e microtearing drive discovered in cylinder

- *Hazeltine Dobrott and Wang (1975)*: kinetic, collisions key, any v_e/ω

Further slab calculations confirm ∇T_e drive at high v_e/ω

- *Drake and Lee (1977)*, *Gladd et al (1980)*: kinetic, *Hassam (1980)*: fluid
- => collisional slab drive requires energy dependent $v_e(E)$**

Kinetic calculations in toroidal geometry (large R/a), for low v_e/ω

- *Catto and Rosenbluth (1981)*, *Connor, Cowley and Hastie (1990)*

=> low collisionality drive from trapped particle collisions on passing particles also requires energy dependent $v_e(E)$

MAST has small R/a and $v_e/\omega \sim 0.5$

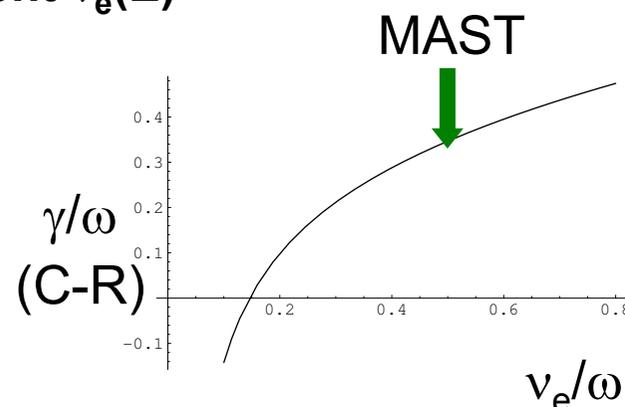
so analytic theories should be poor.

Catto-Rosenbluth trapped particle

drive mechanism, nevertheless,

predicts growth with MAST parameters!

....Connor, Cowley, Hastie does not!



CM Roach *et al*, PPCF **47**, B323 (2005)

Analytic Theories of Microtearing Drives and Properties of the GS2 Modes

Two classes of linear drive in analytic theory literature:

- time dependent thermal force (high collisionality, $\nu_{ei} > \omega$)
- collisions close to the trapped-passing boundary ($\nu_{ei} < \omega$)

Both drives require

- finite dT_e/dr
- energy dependent collision frequency $\nu_{ei}(v)$

Some properties of the GS2 mode:

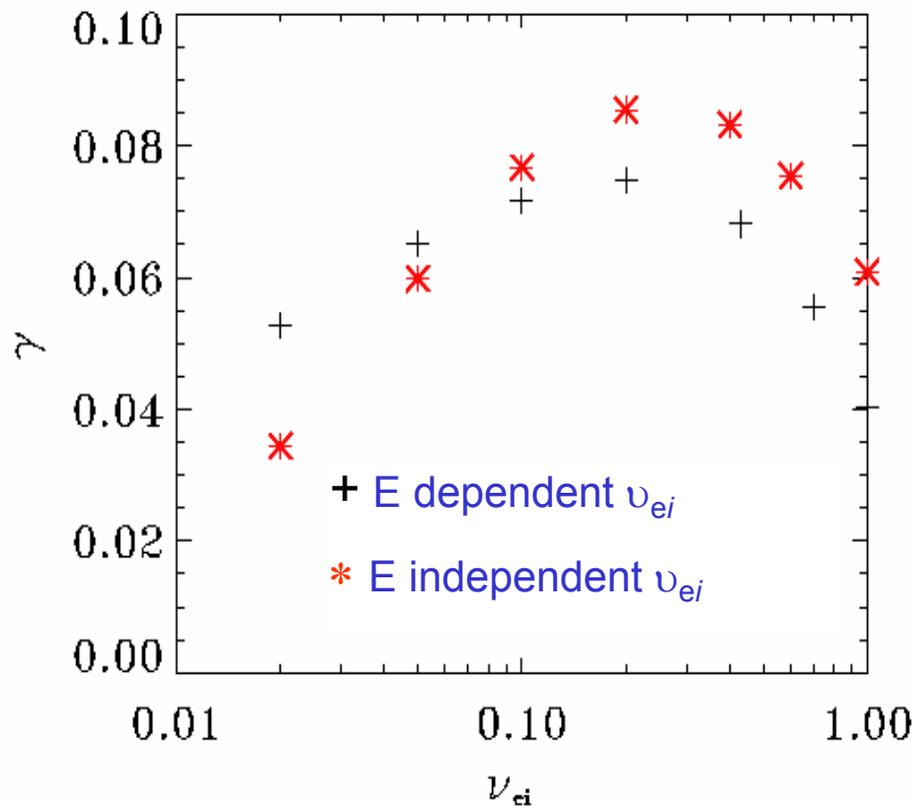
- **sensitive** to electron physics ν_e , ∇T_e and ∇n_e
- **sensitive** to β , ∇p , s
- **insensitive** to ion parameters ν_i and ∇T_i and $\delta B_{||}$
- current layer width $\sim O(\rho_i)$

[1] DJ Applegate *et al*, PPCF **49**, 1113 (2007) and PhD Imperial College (2006)

Experiment with Collision Operator

DJ Applegate *et al*, PPCF **49**, 1113 (2007) and PhD Imperial College (2006)

GS2 Lorentz collision operator can capture boundary layers.
Removed energy dependent collisions by setting $\nu_e(E)=\text{constant}$



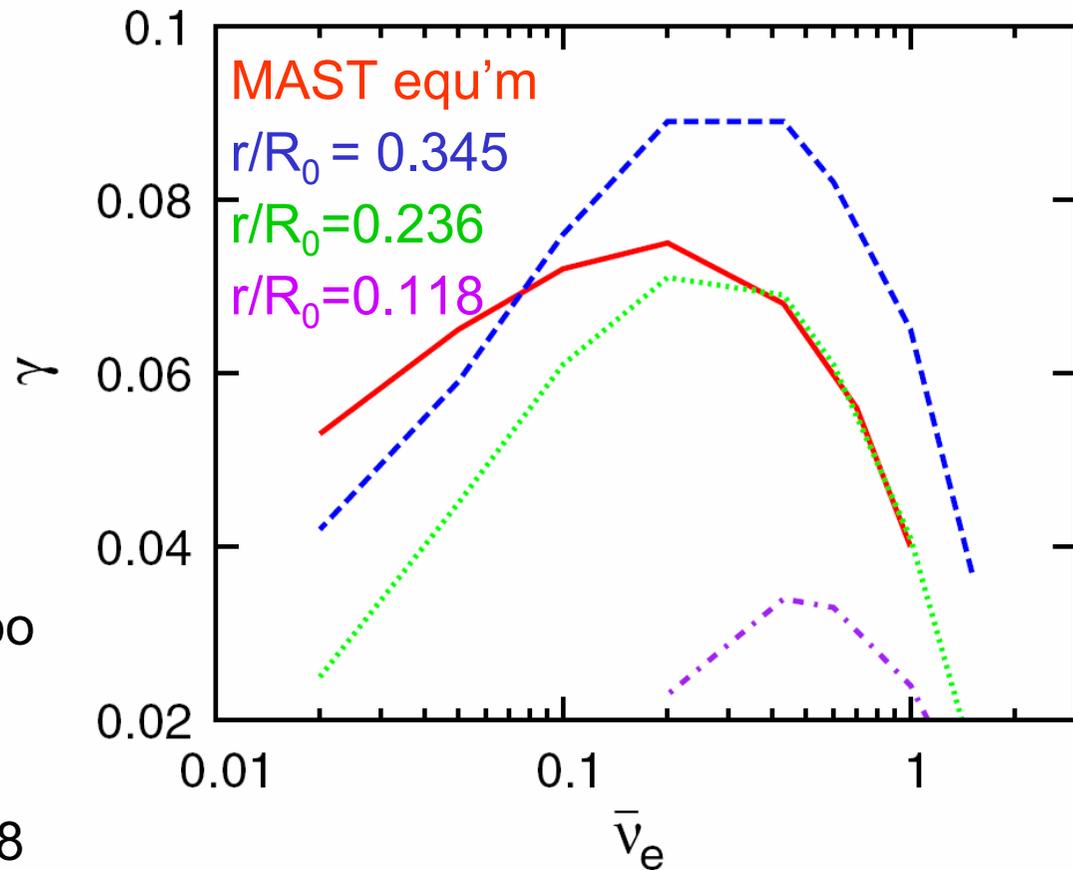
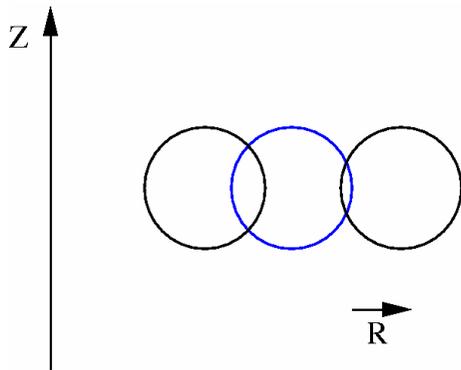
Modest affect on tearing γ

➤ not consistent with analytic drive models!

Experiments Using s- α Model Equilibrium: Scan Aspect Ratio by varying R_0 at Fixed r

DJ Applegate *et al*, PPCF **49**, 1113 (2007)

Fit MAST mid-radius surface with s- α model for fixed β , a/L_T , a/L_n , q , s
Scan r/R_0 by varying R_0 and fixing r and other parameters, varies drifts + f_t



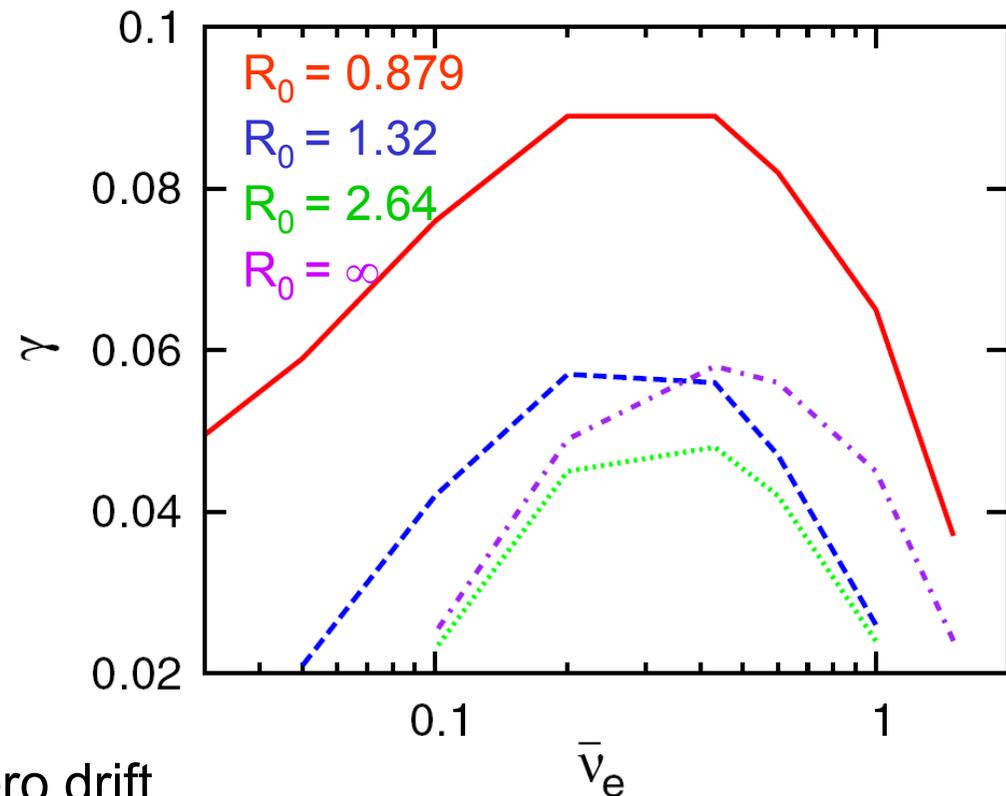
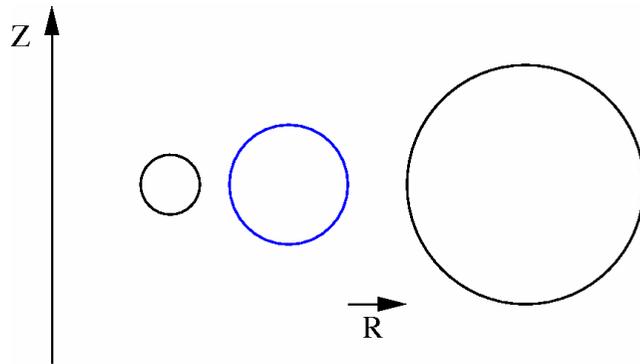
- **MAST** instability in s- α too
 \Rightarrow shaping not essential
- $\gamma \downarrow$ as $r/R_0 \downarrow$
- still unstable at $r/R_0=0.118$

\Rightarrow μ tearing may appear at conventional aspect ratio

Experiments Using s- α Model Equilibrium: Scan R_0 at fixed r/R_0 to Vary Drifts

DJ Applegate *et al*, PPCF **49**, 1113 (2007)

Now scan in R_0 at fixed r/R_0 with other parameters constant



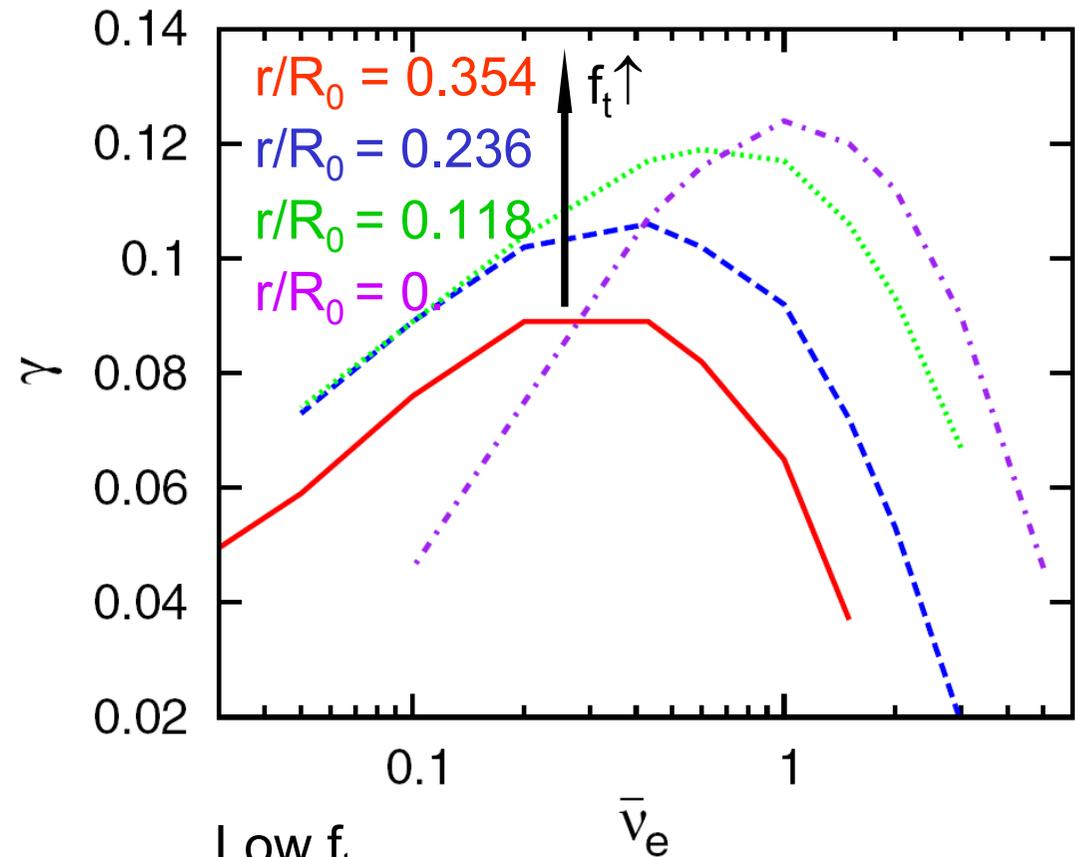
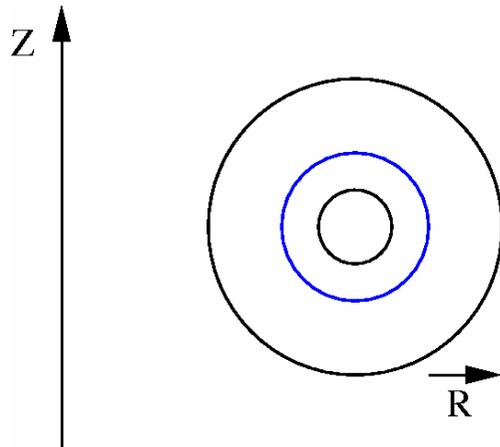
Mode survives at $R_0 = \infty$ i.e. zero drift

- mode has slab drive

Experiments Using s- α Model Equilibrium: Scan in Trapped Particle Fraction, f_t

DJ Applegate *et al*, PPCF **49**, 1113 (2007)

Now scan r/R_0 to vary f_t at fixed R_0 and other parameters



High f_t

- $\gamma \uparrow$ at low v_e
- $\gamma \downarrow$ at high v_e (fewer passing e)

Low f_t

- γ more sensitive to energy dependent collision rate $v_e(E)$

Overview of Most Interesting Findings

DJ Applegate *et al*, PPCF **49**, 1113 (2007)

Microtearing mode is driven by dT_e/dr as expected.

Mode is complicated and in awkward regime for analytic theory:

- unstable over broad range of collisionality $0.05 < \nu_{ei}/\omega < 1.2$
- current layer width $\sim O(\rho_i)$, so need ion FLR effects

Regimes where mode robust to energy independent collisions \Rightarrow puzzle

Mode not only unstable in ST

- unstable in large aspect ratio s - α model equilibria

Gyrokinetic microtearing also at $r/R \sim 0.3$ (\sim MAST mid-radius) in conventional aspect ratio: D Told *et al*, Phys. Plasmas **15**, 102306 (2008)

* Very High β : Microstability in STPP

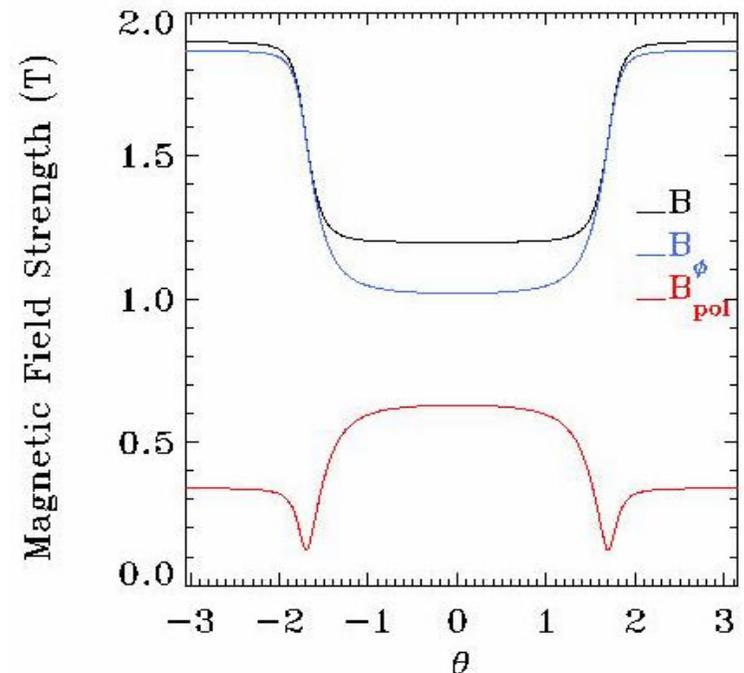
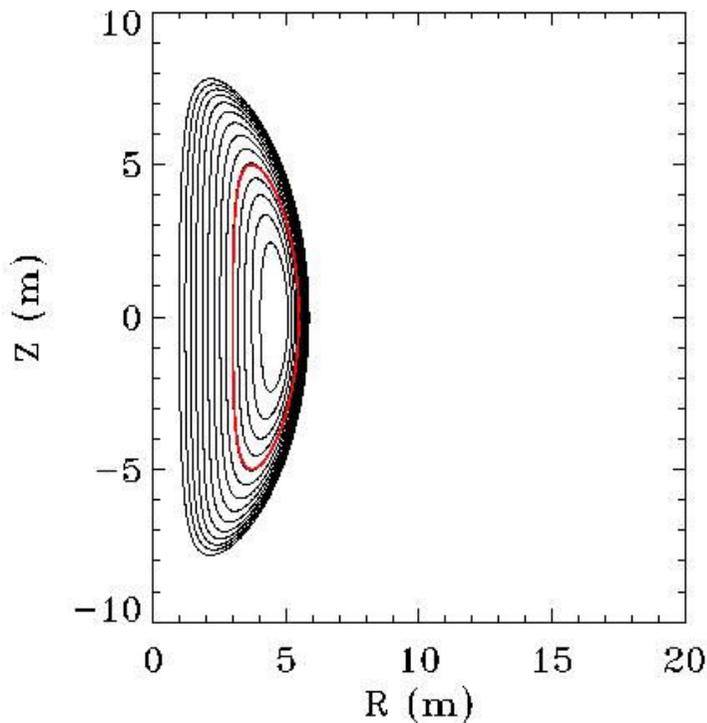
see H R Wilson *et al*, Nuc Fus 44, 917 (2004)

Conceptual Culham ST Power Plant (STPP), 1GW electrical, $\beta=0.59$

GS2 used for microstability analysis of mid-radius flux-surface, $\Psi_n=0.35$.

Equilibrium features:

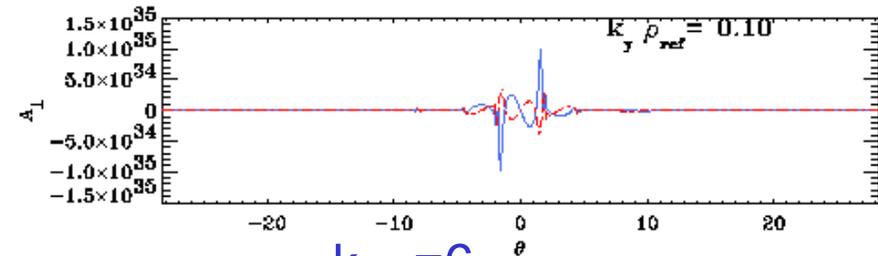
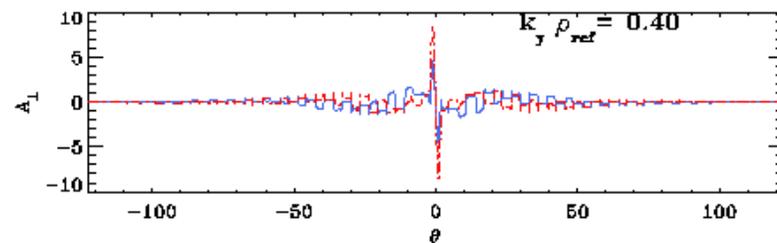
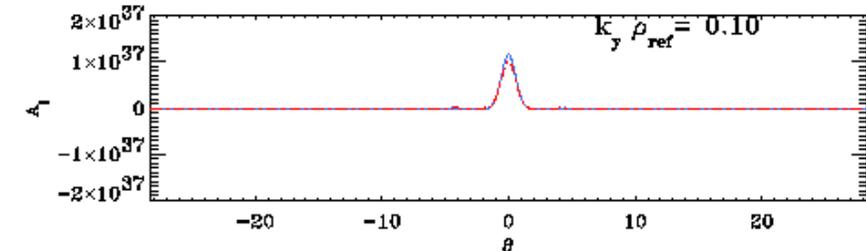
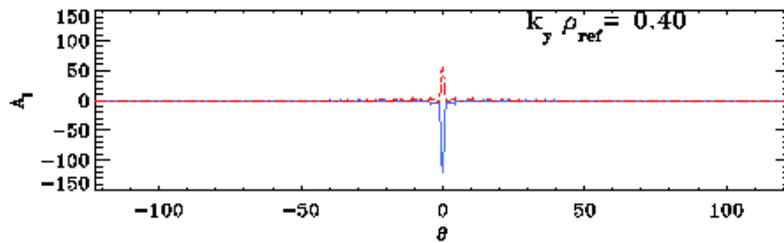
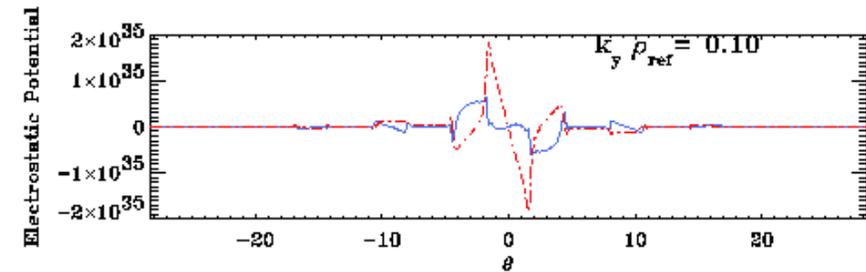
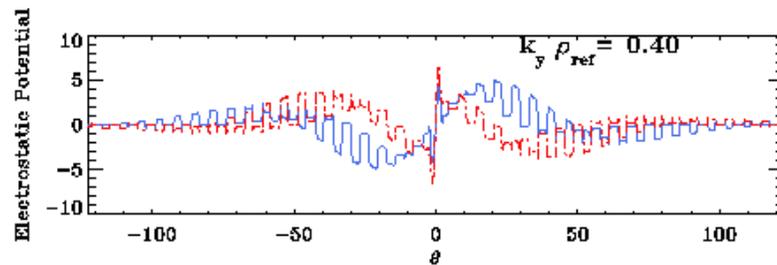
- striking variation in $|B|$ around the magnetic flux surface
- magnetic drift reversal owing to high pressure gradient
- diamagnetic ω_{se} strongly peaked on outboard midplane



* Microstability Results for Mid-radius Surface in STPP

STPP surface $\Psi_n=0.35$

- no electrostatic instabilities, α stabilisation giving drift reversal
- including EM gives tearing parity modes at ion and electron scales



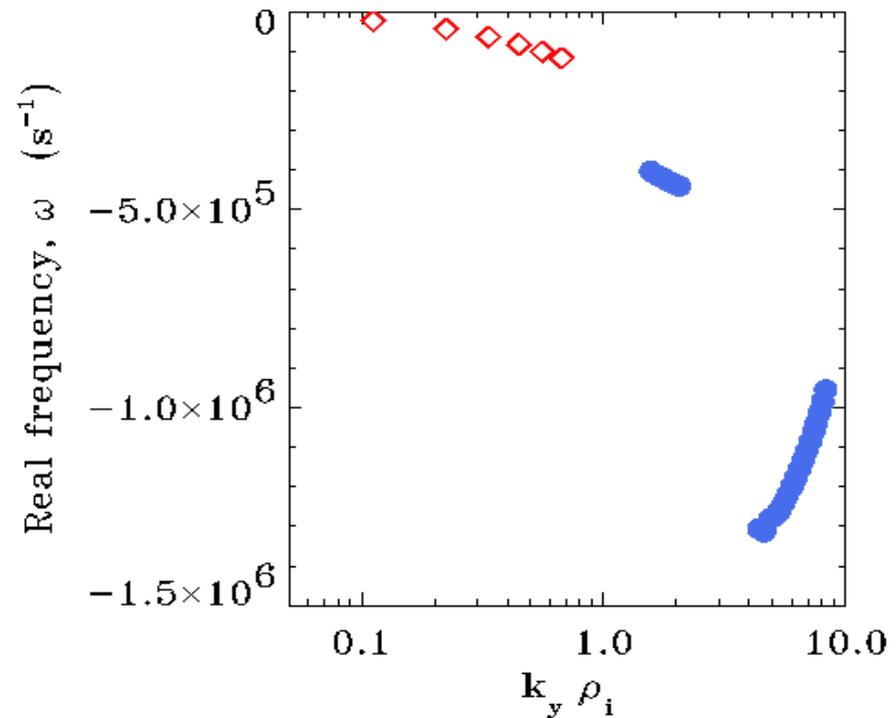
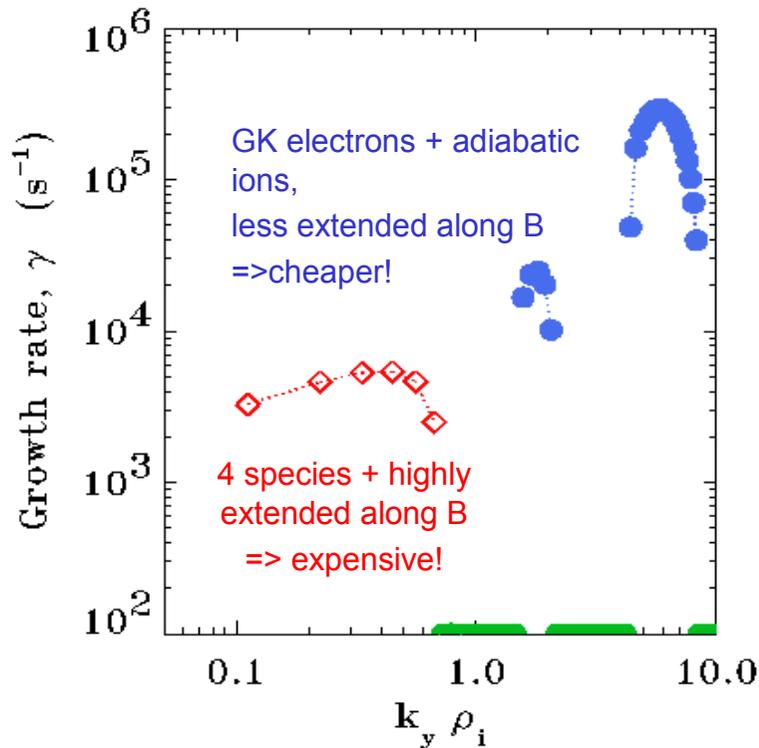
$k_y \rho_i = 0.4$

$k_y \rho_i = 6$

* Microstability Results for Mid-radius Surface in STPP

STPP surface $\Psi_n=0.35$

- **no electrostatic instabilities** (α stabilisation from drift reversal)
- EM effects gives **tearing parity modes at ion and electron scales**, all propagating in electron drift direction
- Mixing length $\chi \sim 4\text{m}^2\text{s}^{-1}$ (no ω_{se})



Nonlinear Microtearing Simulations with GS2

D J Applegate

First nonlinear GK simulations with GS2 [1,2] :

- modified mid-radius MAST equilibrium for increased tractability

	MAST Equilibrium	Nonlinear Model
q	1.3463	1.3463
\hat{s}	0.286	1.4
β	0.0495	0.12
a/L_{ne}	-0.1766	2.4
a/L_{Te}	2.0433	2.0433
a/L_{Pe}	1.8667	4.4433
a/L_{ni}	-0.1766	2.4
a/L_{Ti}	2.0433	2.0433
a/L_{Pi}	1.8667	4.4433

reduces radial box size
by factor 5

Few k_y modes: $n_{ky}=4$, $n_{kx}=47$, $n_\theta=32$, $n_E=8$, $n_\lambda \sim 20$

- “pseudo-saturation” with low transport, blows up later at high k_x
- small timesteps imposed by the CFL condition

[1] D J Applegate PhD Thesis, Imperial College (2007).

[2] D J Applegate et al, 32nd EPS, Tarragona, ECA volume 29C, P5-101, 2005

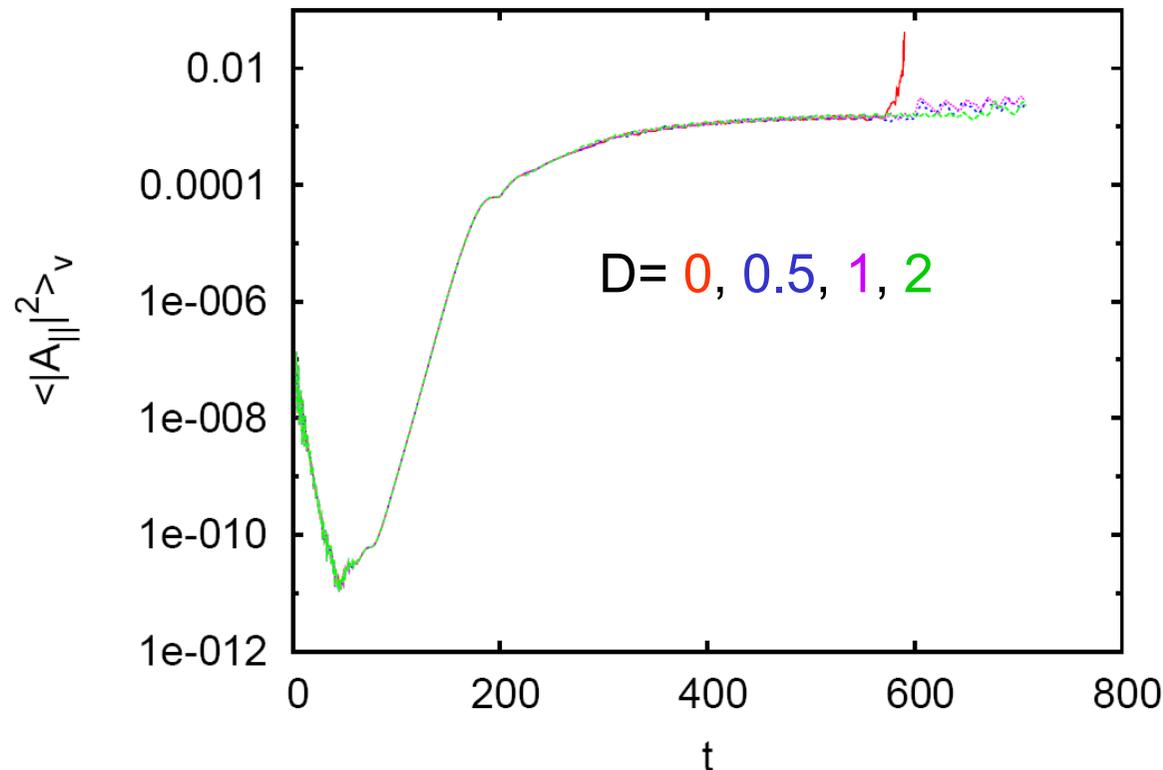
Impact of Adding Dissipation at High k

R J Akers et al, IAEA FEC, Geneva, October 2008 EX/2-2

Use hyperviscosity for high k dissipation, parameterised by D

- no impact on linear physics
- improves convergence
- “saturation” insensitive to D

but what are we throwing away?

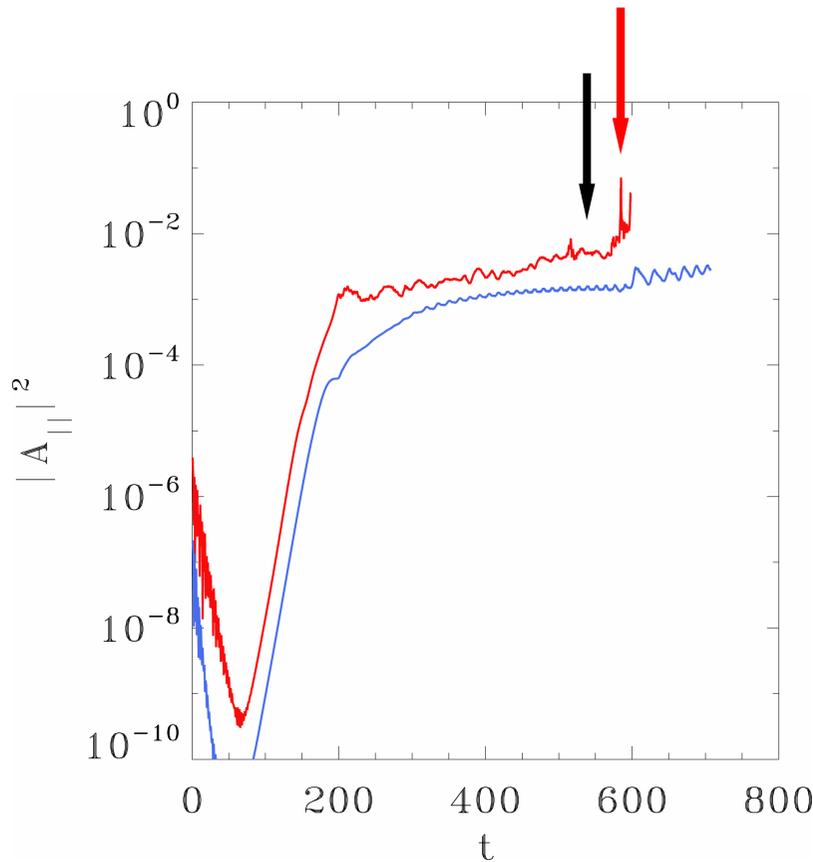


Nonlinear Electron Heat Flux

D J Applegate

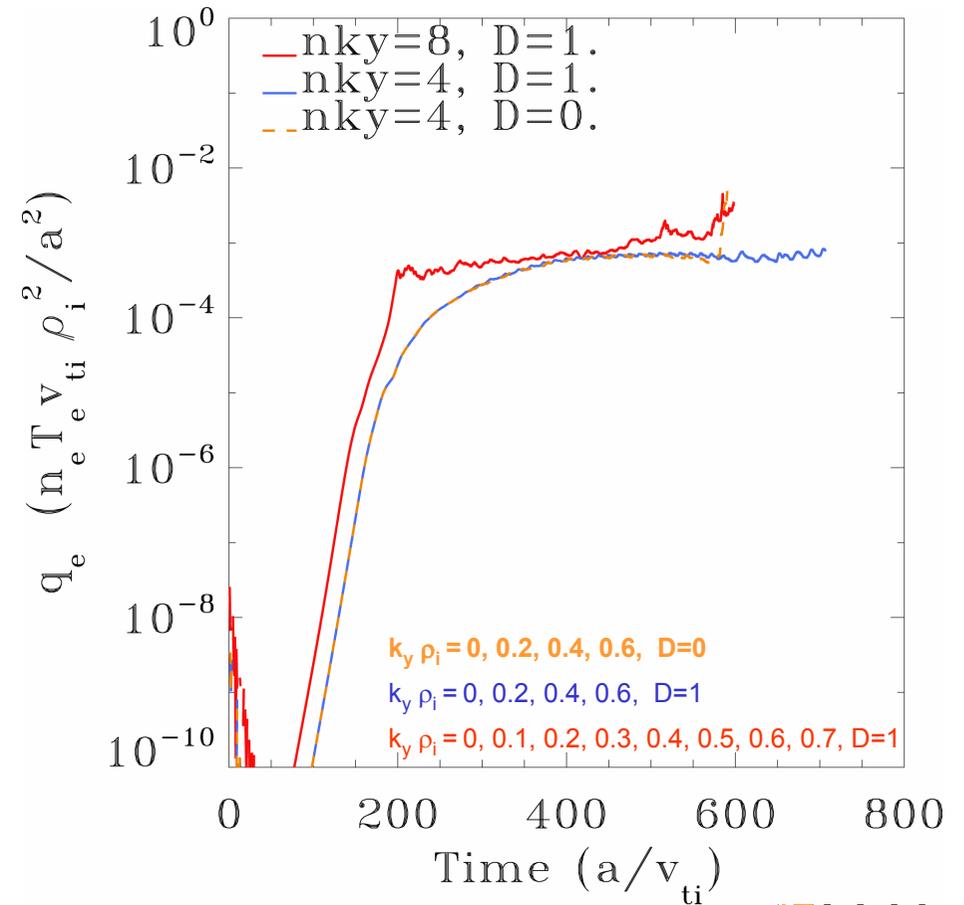
Hyperviscosity smoothes high k_x

- spike events reappear at $nky=8$



$A_{||}$ contribution dominates q_e

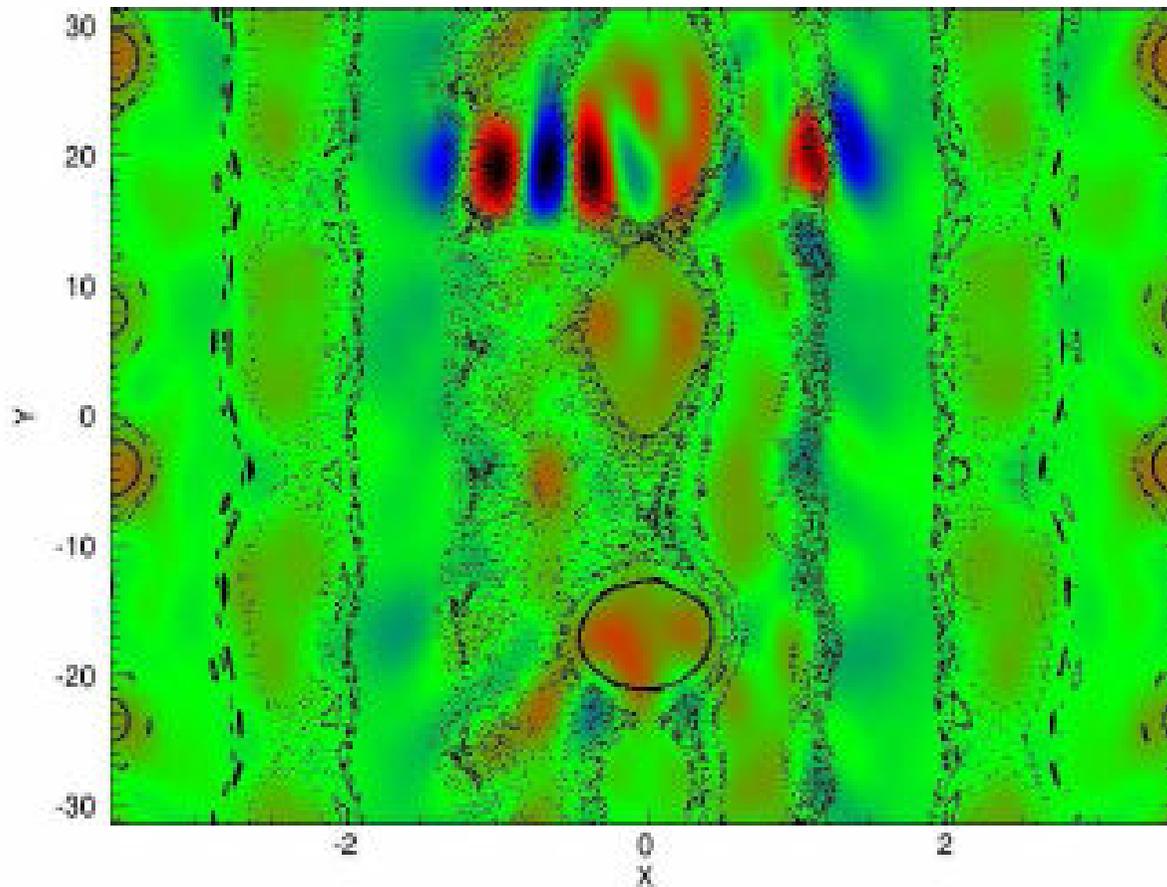
- low heat fluxes at “saturation”



Poincaré Plot and $\delta j_{||}$ contours at $\theta=0$

D J Applegate

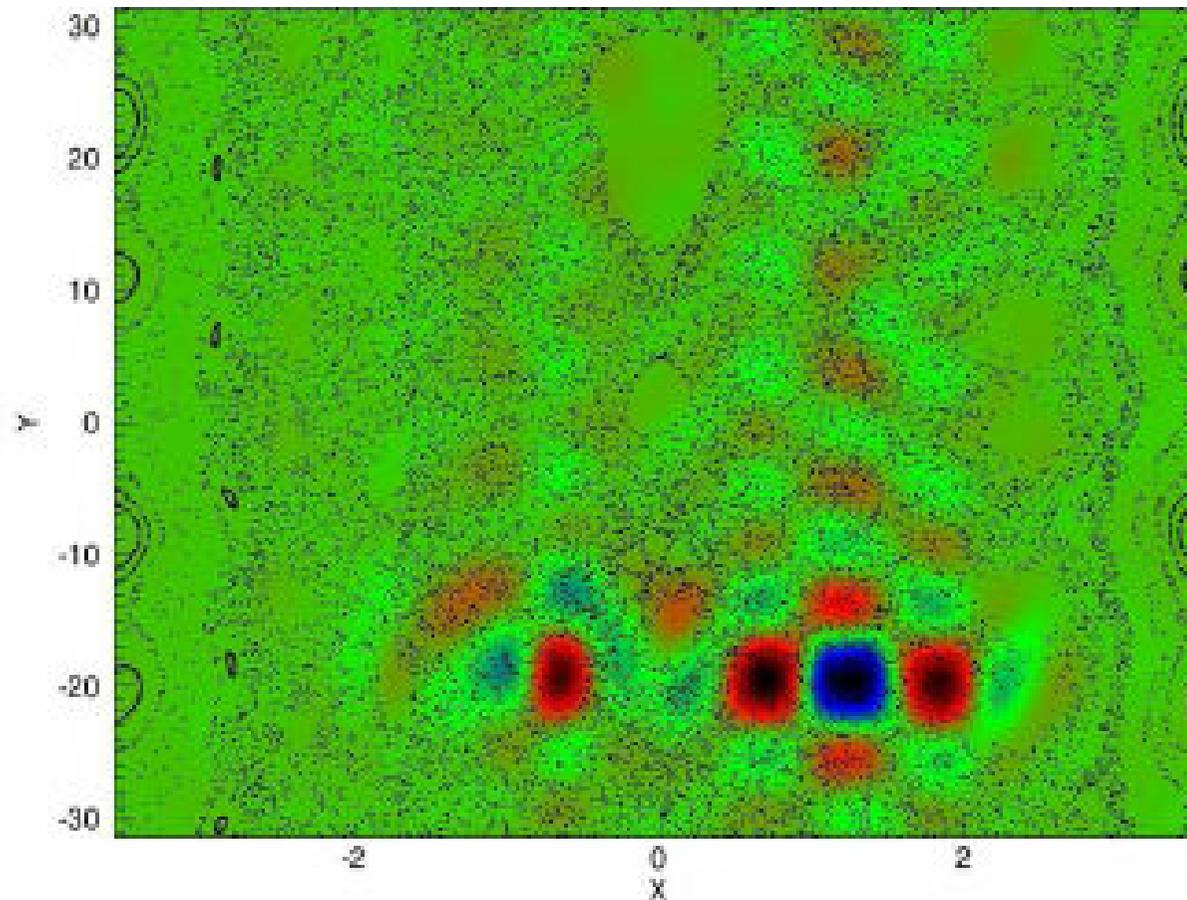
before spike event, $t=532$



Poincaré Plot and δj_{\parallel} contours at $\theta=0$, $t=598$.

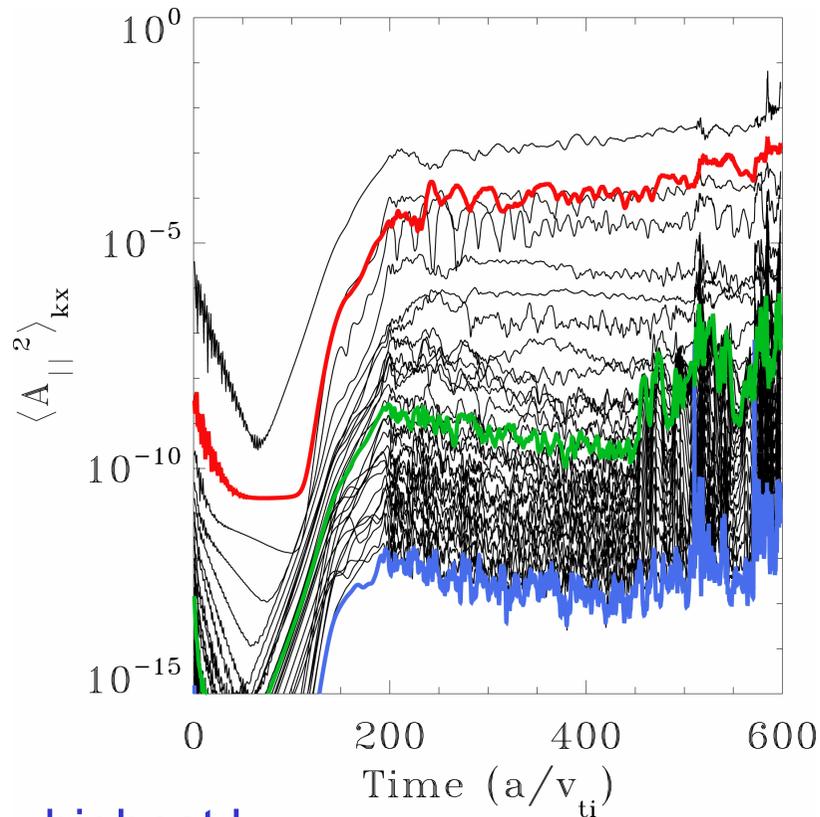
D J Applegate

after spike event perturbed field wanders further, transport \uparrow



A_{\parallel} Spectra for $n_{ky}=8$ Simulation

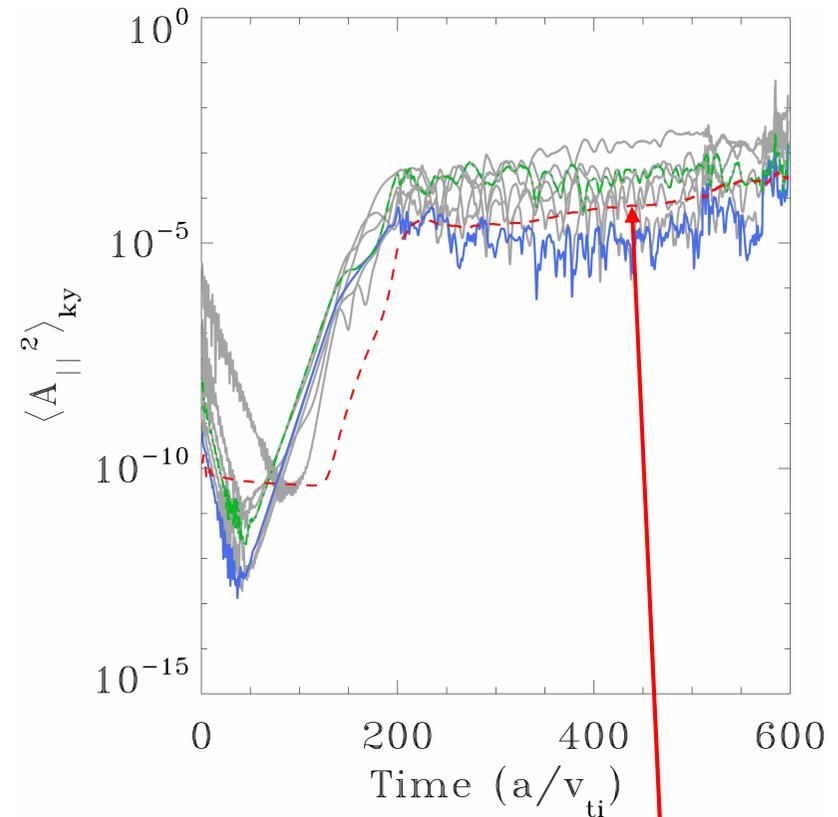
Spikes most evident at high k , but are controlled by D



highest k

middle k

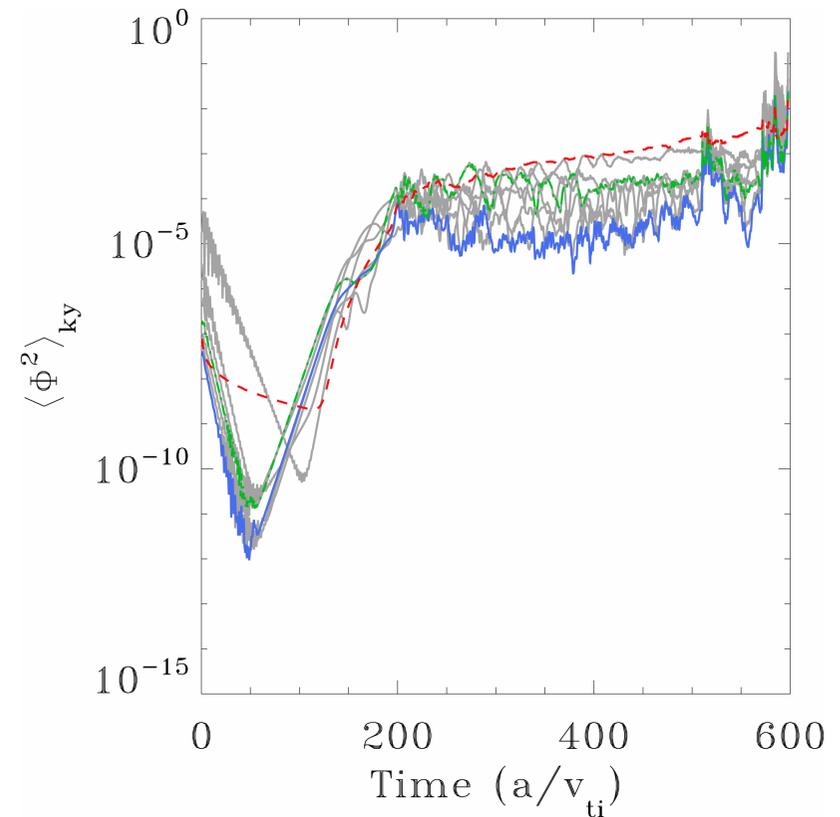
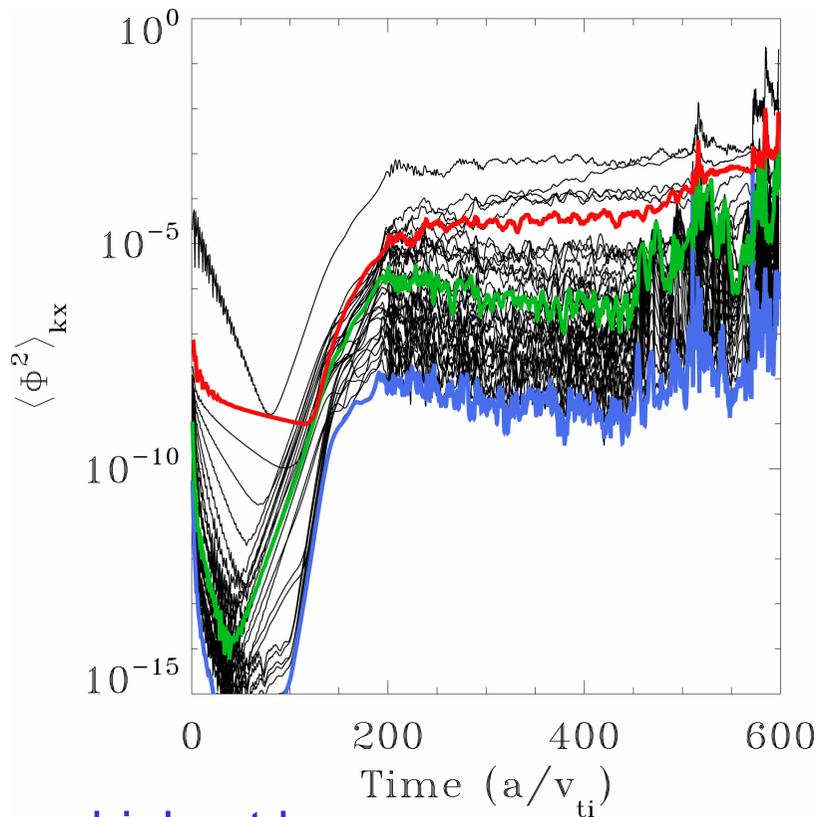
lowest finite k_x , or $k_y=0$



steady growth in zonal modes

* Φ Spectra for nky=8 Simulation

Spikes most evident at high k, but suppressed by D



highest k

middle k

lowest finite k_x , or $k_y=0$

Fidelity Issues

D J Applegate

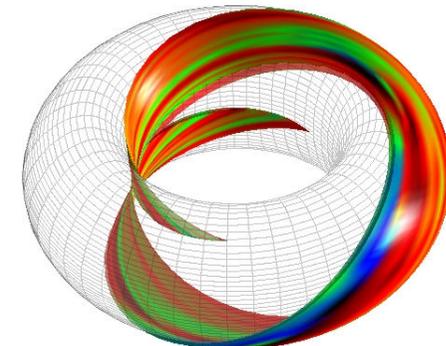
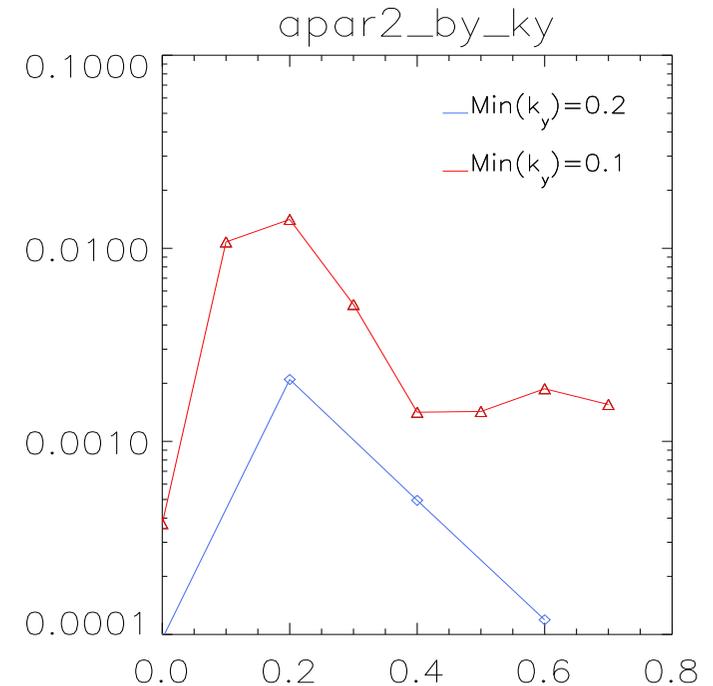
Convergence?

- saturation sensitive to $\text{Min}(k_y)$, and we need to go lower in k_y !
- what causes the high k spikes?
- are we dissipating important physics?

Flux-Tube equilibrium?

- as reduce $\text{Min}(k_y \rho_i)$, we go to low n
- $s^{\text{SIM}} = 5 s^{\text{MAST}}$ so L_x artificially small
- at lower k_y and s , flux-tube gets fatter, to challenge local approximations

More work needed!

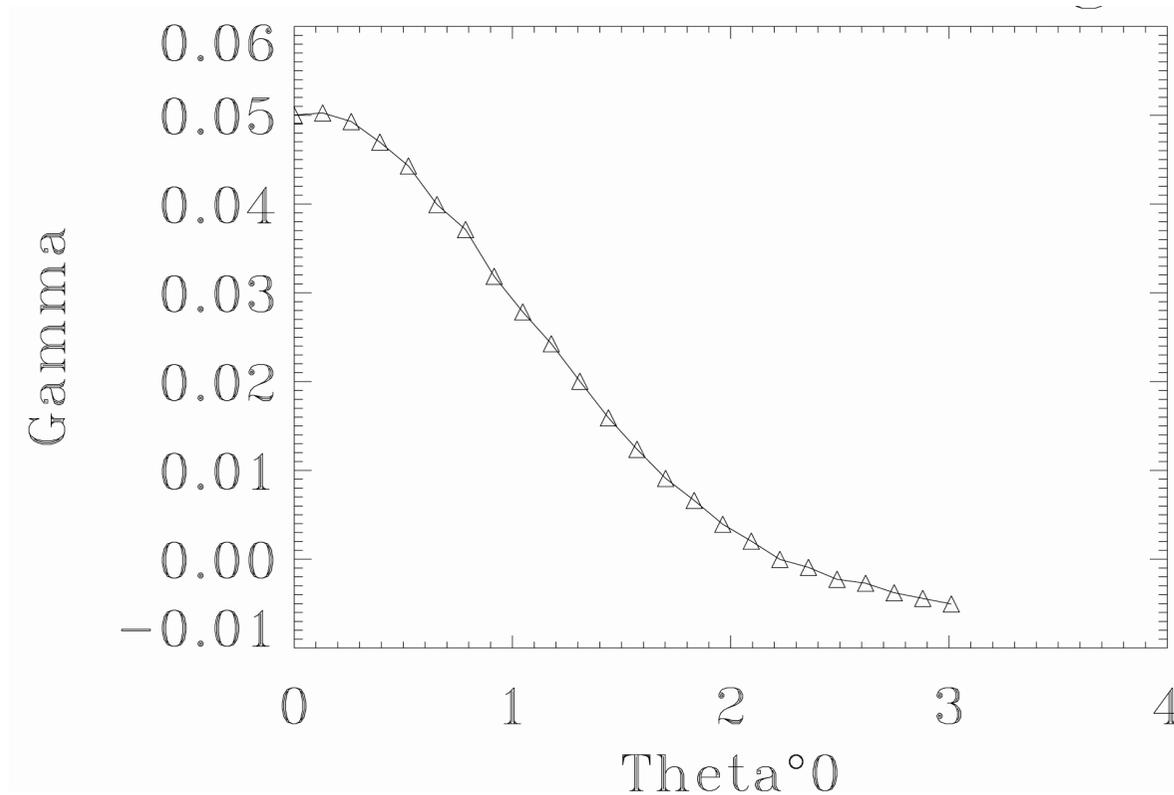


Do Microtearing Modes Matter in MAST Anyway?

D Dickinson, York

Impact of FLOW SHEAR on microtearing modes?

- $\gamma_E > \gamma_{lin}$ so will they be suppressed?
- slab drive may make suppression more difficult
- almost done



Conclusions

Microtearing modes from GS2 simulations of MAST are complicated!

- trapped and passing particles contribute drive with dT_e/dr
- insensitivity of γ to energy dependent collision frequency is puzzling
- μ tearing specific neither to ST geometry nor to GS2!
 - linear benchmark?
 - map out where μ tearing important

Limited comparisons with analytic theory so far.

- do better in easier limits?

Preliminary nonlinear simulations for MAST mid-radius are interesting, but:

- more work needed to test convergence
- what is happening at high k ?
- local flux-tube equilibrium is challenged if n gets too small!
 - easier equilibria?
 - impact of FLOW SHEAR?