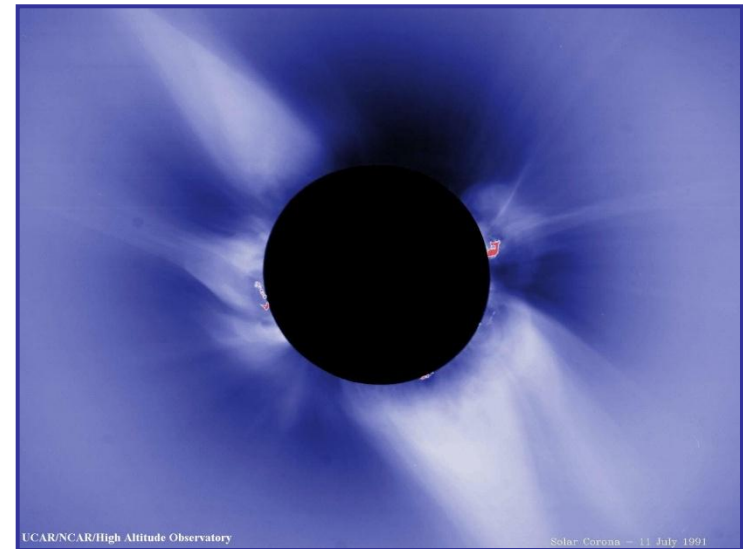


# Observational evidence for anisotropic solar wind turbulence on fluid and kinetic scales

Tim Horbury  
Imperial College London

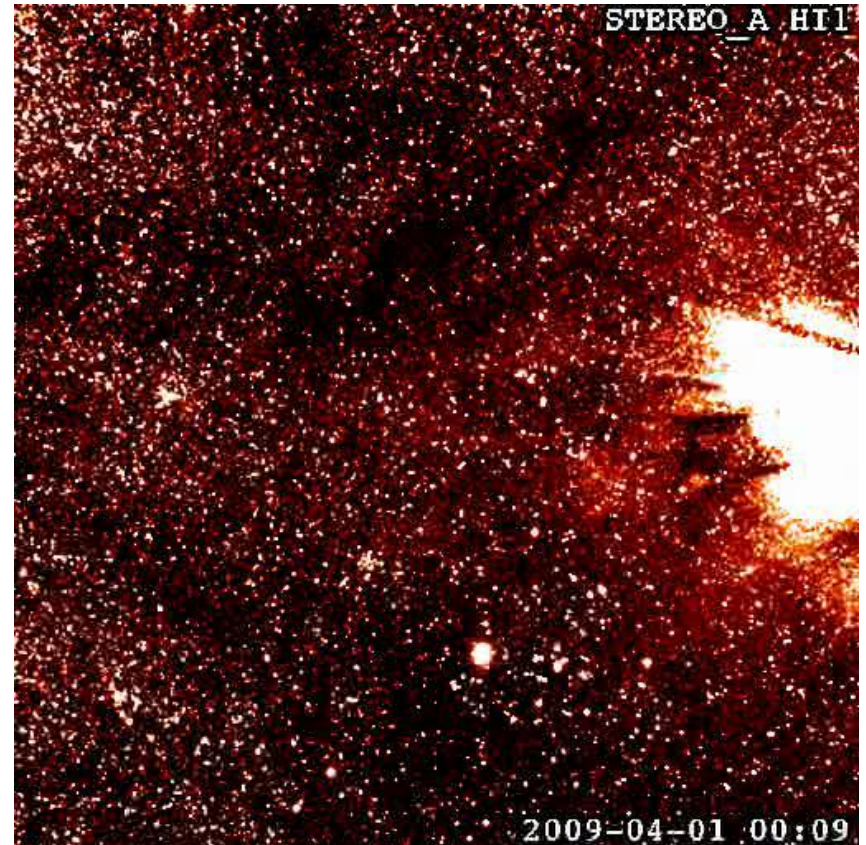
*Thanks to Chris Chen, Robert Wicks, Alex Schekochihin, Miriam Forman*

- The solar wind as a turbulence laboratory
- What we know: the basics
- MHD scale cascade
- Ion scale cascade
- Kinetics: instabilities
- Open questions



# What is the solar wind?

- Collisionless, magnetised plasma
- Continual, but variable, outflow from Sun's corona
- Carries waves and turbulence from corona
  
- **Complex** due to solar variability, solar rotation, and in situ processes
- **Variable** on all measured scales, from sub-second → centuries



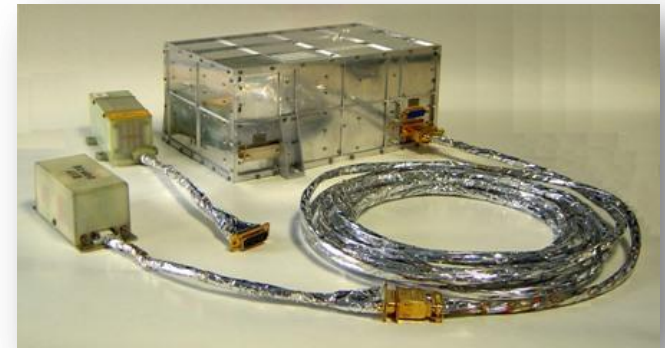
STEREO/HI

# Typical solar wind parameters (near Earth)

Composition	Mostly protons, few percent alpha, small heavies
Ion temperature	$\sim 10^5$ K
Bulk speed	250-800 km/s
Alfven speed	$\sim 40$ km/s
Debye length	$\sim 10$ m
Mean free path	$\sim 1$ AU
Proton gyroradius	$\sim 100$ km
Proton inertial length	$\sim 100$ km
Magnetic field	$\sim 5$ nT
Proton beta	$\sim 1$

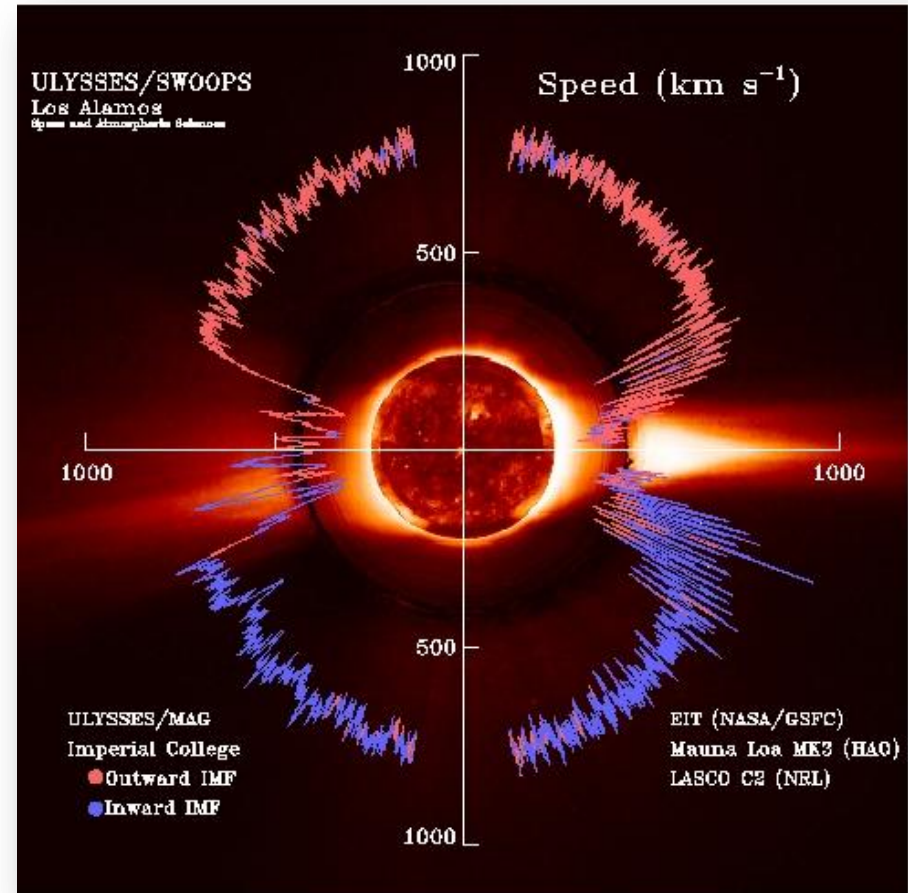
# Spacecraft as sensors

- Spacecraft are (mostly) test particles
- Natural fields are very small – significant spacecraft interference issues
- Typical measurements
  - Magnetic field (DC to tens Hz)
  - Electric field
  - Bulk ion properties (velocity, temperature, density)
  - Bulk electron properties (velocity, temperature, density)
  - Full plasma distributions including composition
  - Energetic particles



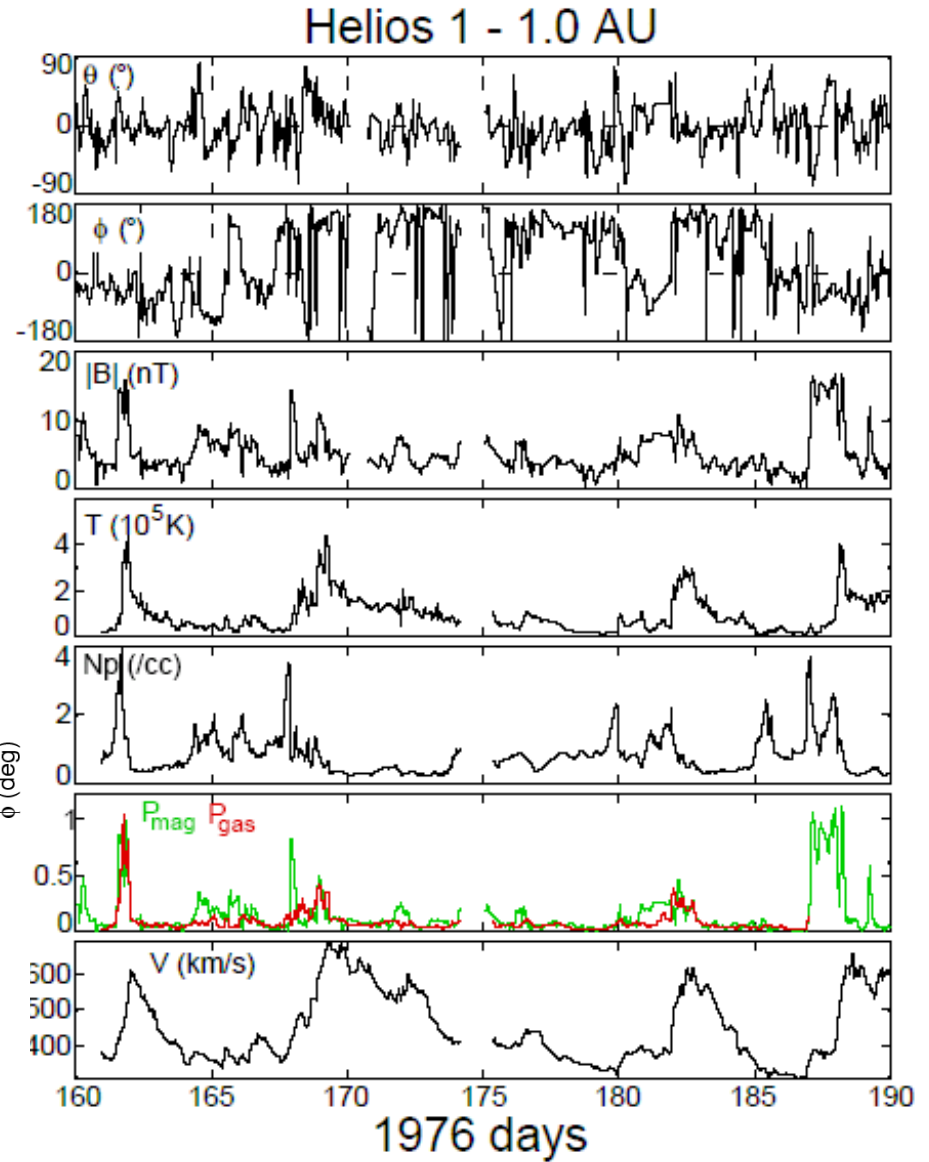
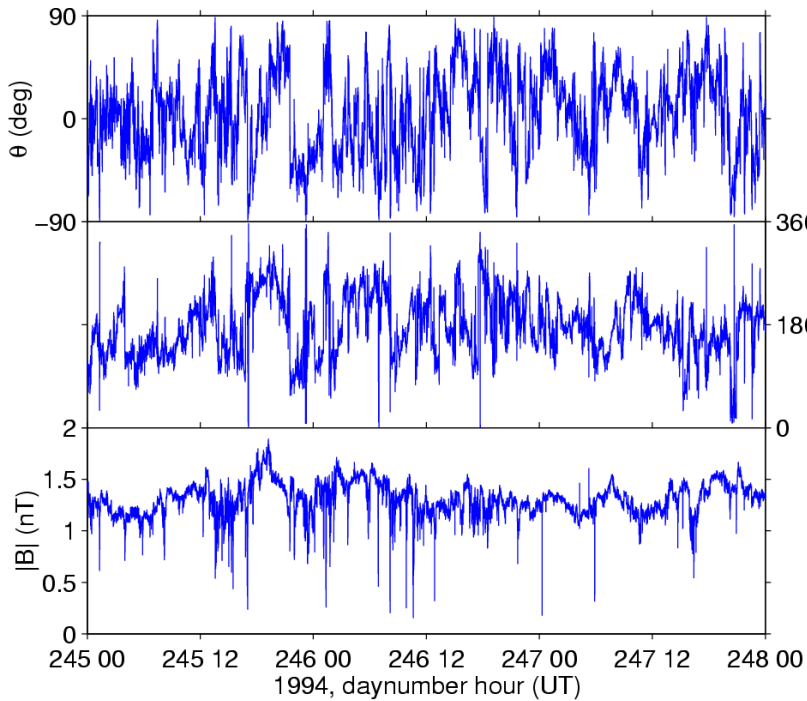
# Exploring the solar system

- Spacecraft have explored most of the solar system
- None has a fully comprehensive instrument package
- Big changes in properties with distance, latitude, solar cycle
- Biggest factor is fast vs slow solar wind



# Typical conditions at 1.0 AU

- Individual streams last a few days
- Always need to consider the context



# Interpreting spacecraft measurements

- In the solar wind (usually),

$$V_A \sim 50 \text{ km/s}, V_{SW} > \sim 300 \text{ km/s}$$

- Therefore,

$$V_{SW} \gg V_A$$

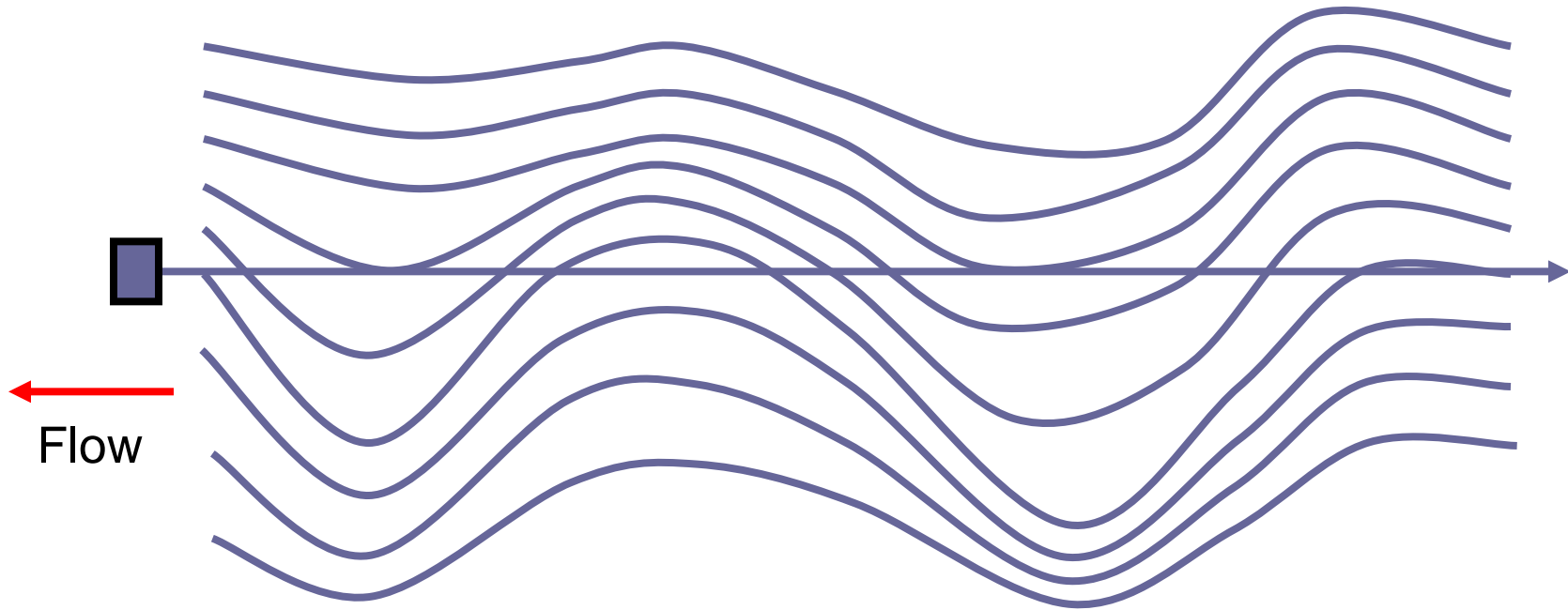
- **Taylor's hypothesis:** time series can be considered a spatial sample
- We can convert spacecraft frequency  $f$  into a plasma frame wavenumber  $k$ :

$$k = 2\pi f / V_{SW}$$

- Almost always valid in the solar wind
- Makes analysis much easier
- Not valid in, e.g. magnetosheath, upper corona, kinetic scales(?)

# Interpreting spacecraft measurements

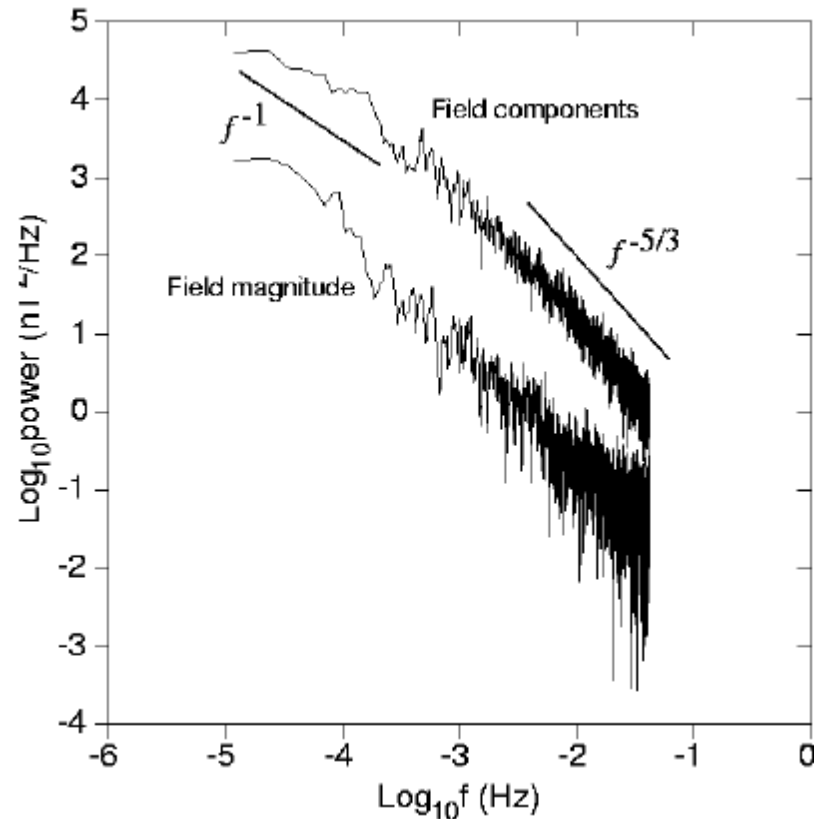
- Solar wind flows radially away from Sun, over spacecraft
- Time series is a one dimensional spatial sample through the plasma
- Measure variations along one flow line





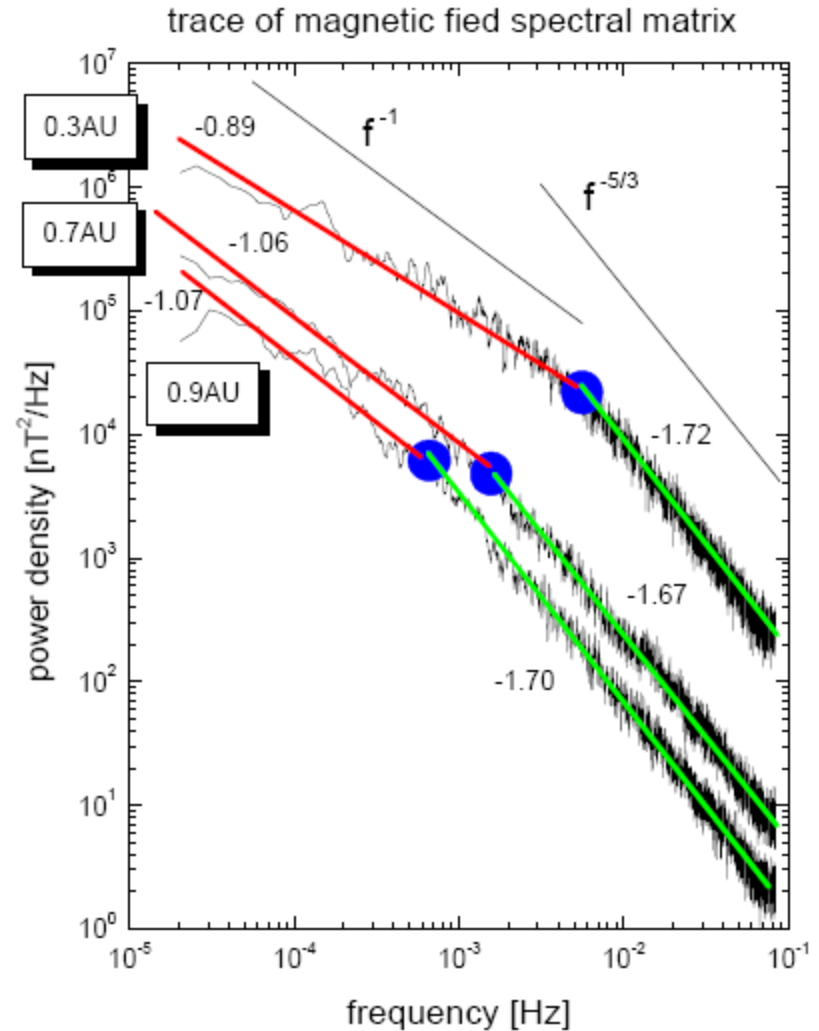
# Things we know: power spectrum

- Extended fluid scale inertial range
- Magnetic field power spectrum:
  - $f^{-5/3}$
- Inertial range covers  $\sim 10^2$  in scale
- Components much higher power than magnitude
  - Largely non-compressive



# Active turbulent cascade in fast wind

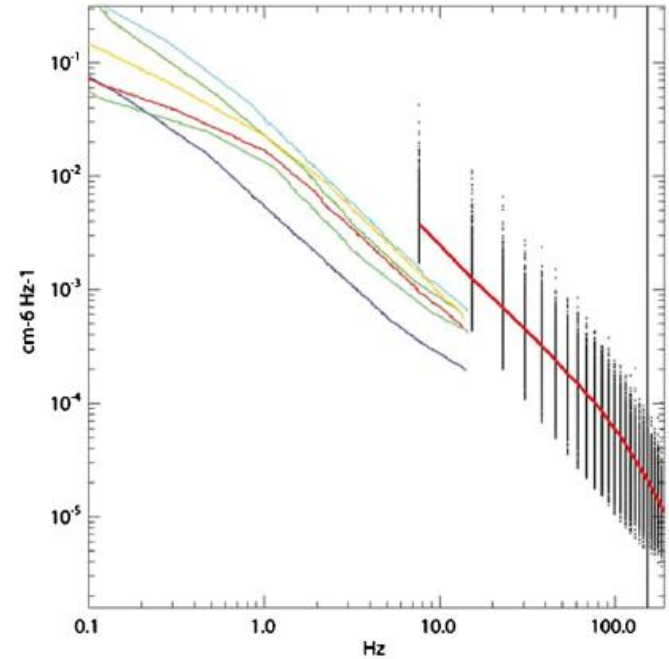
- Bavassano et al (1982)
- Fast wind: “knee” in spectrum
- Spectrum steepens further from the Sun
- Evidence of energy transfer between scales: **turbulent cascade**



after Bavassano et al 1982

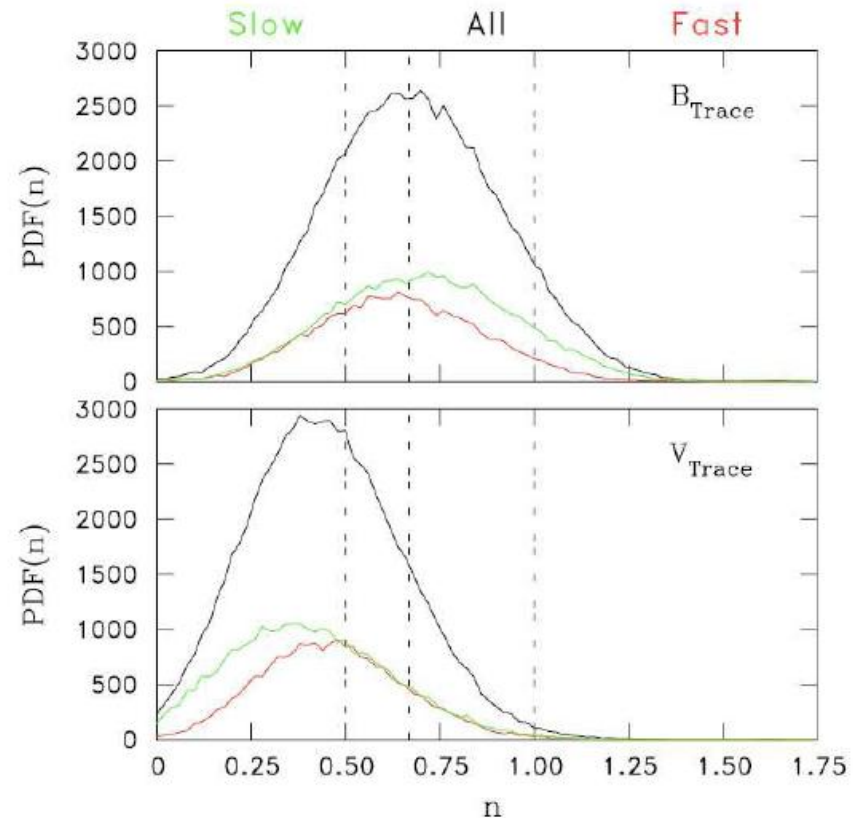
# Density spectrum

- Malaspina et al., Ap. J., v.711, 322, 2010
- See also Celnikier et al., Astron. Astrophys., v.181, 138, 1987
- Broadband density spectrum
- Evidence for break at ion gyroscale
- Behaviour as a passive scalar on MHD scales?



# Velocity vs magnetic field scaling

- Magnetic field has  $5/3$  spectral index
- Velocity has  $3/2$  spectral index (Podesta, 2009)
- Physical cause of this effect?
  - Related to Alfvénicity?



Tessein et al., 2009

# Alfvén waves

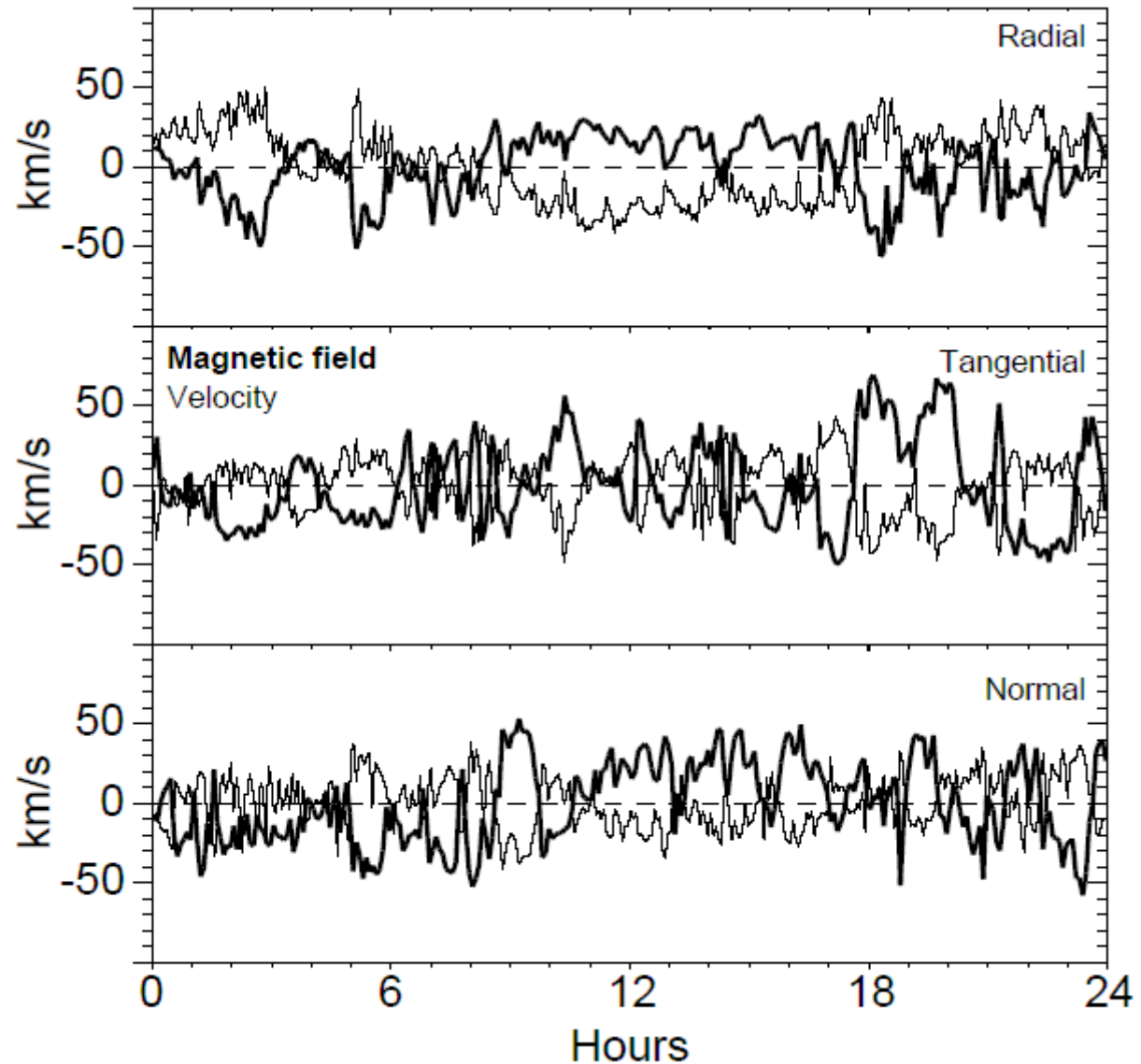
**Field-parallel** Alfvén wave:

- B and V variations anti-correlated

**Field-anti-parallel**

Alfvén wave:

- B and V variations correlated
- See this very clearly in the solar wind
- Most common in high speed wind



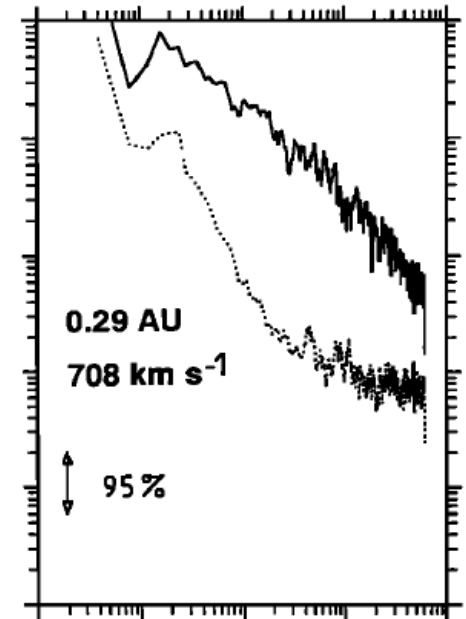
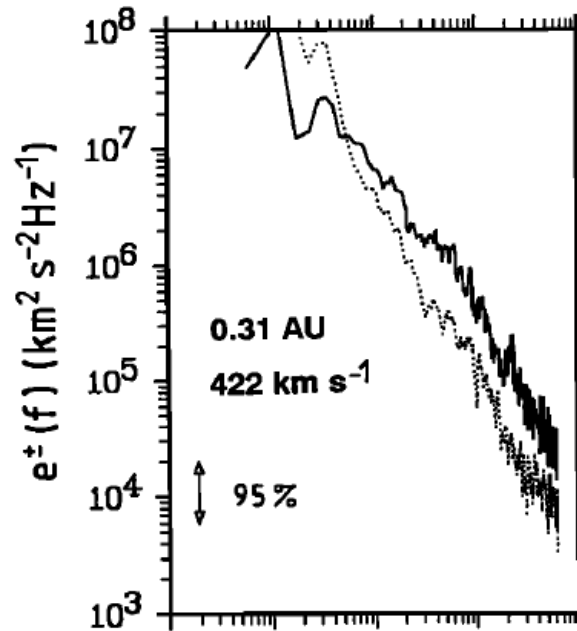
# Elsasser variable power spectra

## Fast wind

- Imbalanced, dominant outward component
- “Diamond” spectrum

## Slow wind

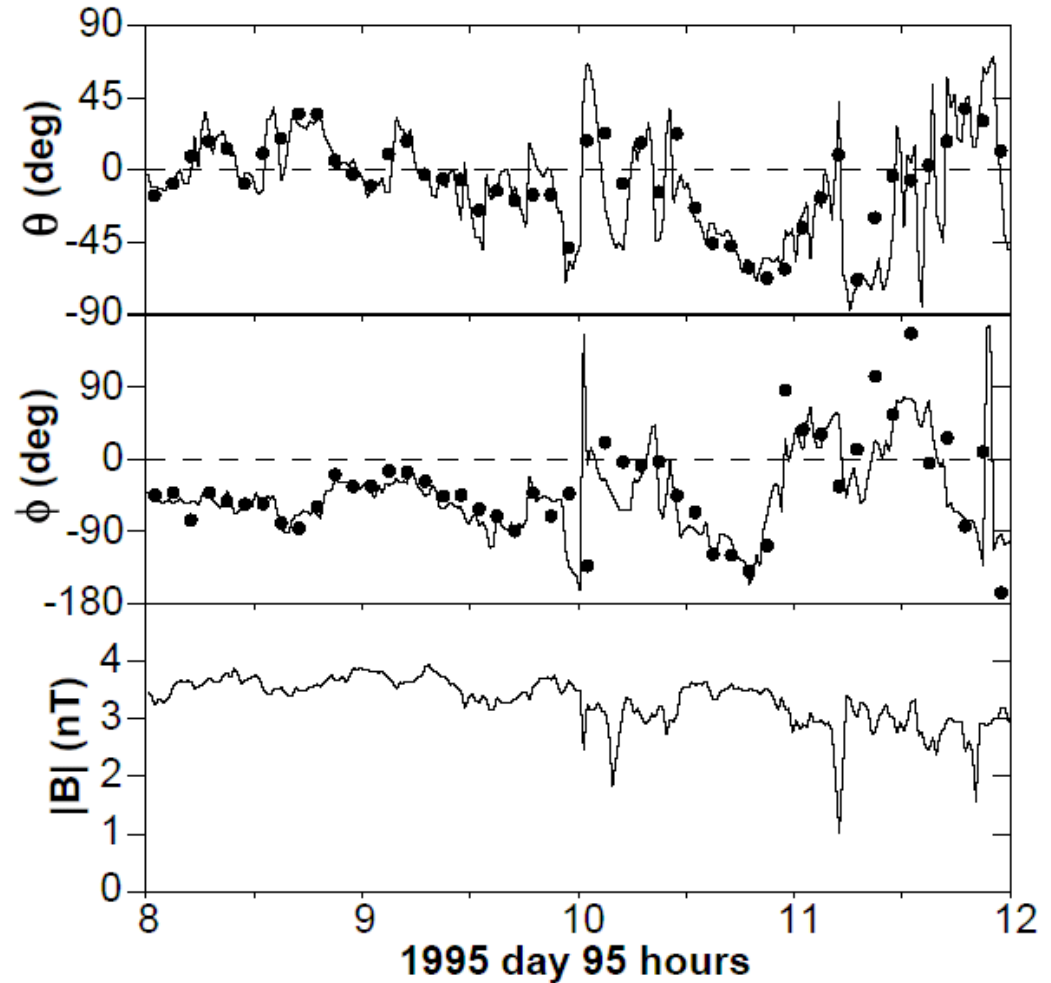
- More balanced on average
- Longer inertial range
- **Solar wind often shows significant imbalance**



Marsch and Tu, JGR, 1990

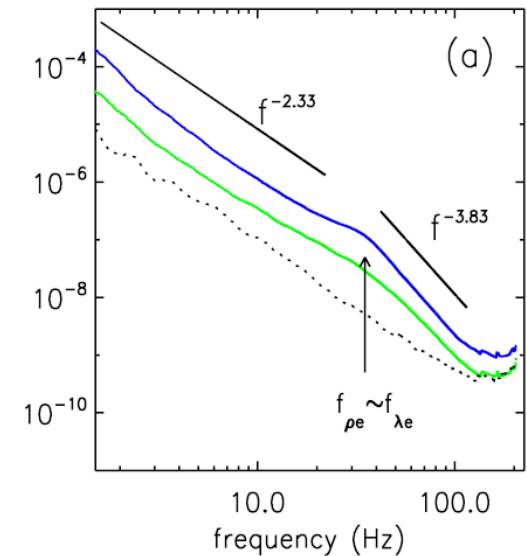
# Field-aligned anisotropy

- Power levels tend to be perpendicular to local magnetic field direction  
→ **anisotropy**
- Dots: local minimum variance direction
- Track large scale changes in field direction
- Small scale turbulence “rides” on the back of large scale waves

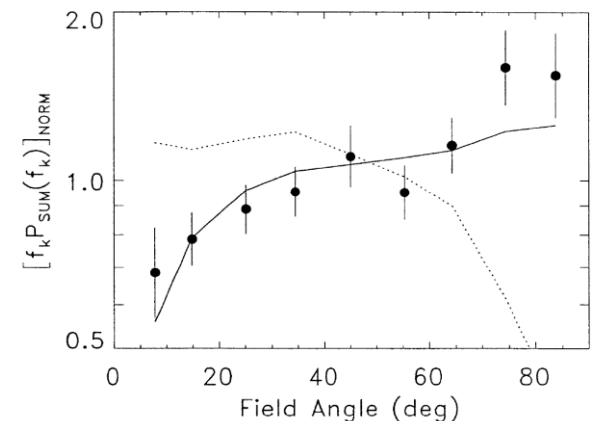


# Types of anisotropy

- Variance anisotropy
  - $\delta B_{\perp} > \delta B_{\parallel}$  (e.g. Belcher and Davis, 1971)
- Wavevector anisotropy
  - Different energy in wavevectors in different directions (e.g. Bieber et al., 1996)
- Scaling anisotropy
  - Different power laws in different directions
- Anisotropy of energy transfer
  - Turbulent cascade can have different rates in different directions
- “Imbalance”
  - Parallel/anti-parallel propagation of Alfvénic turbulence



Sahraoui et al., 2009



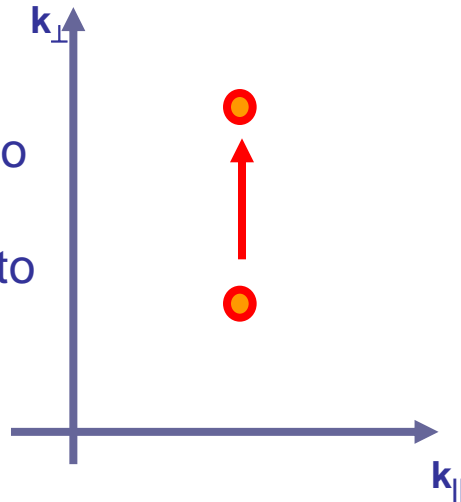
Bieber et al., 1996



# Anisotropic energy transfer

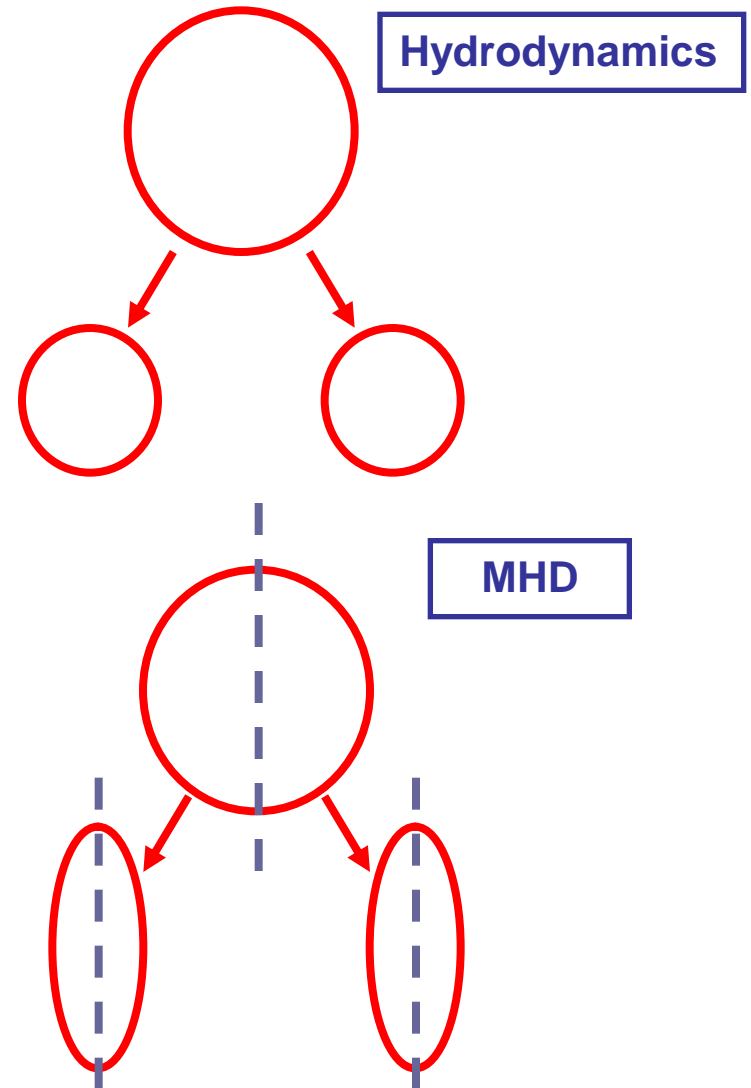
## Wavevectors

- Energy tends to move perpendicular to magnetic field



## Eddies

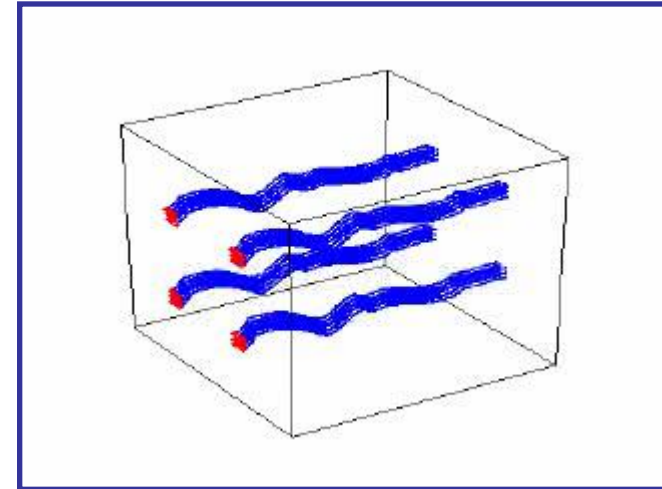
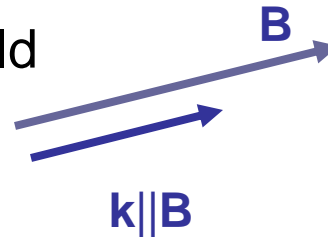
- On average, tend to become smaller perpendicular to field
- Results in long, fine structures along the magnetic field



# Anisotropy and 3D magnetic field structure

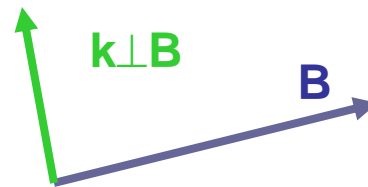
## Slab

- Plane waves
- Infinite correlation length perpendicular to magnetic field
- Flux tubes stay together

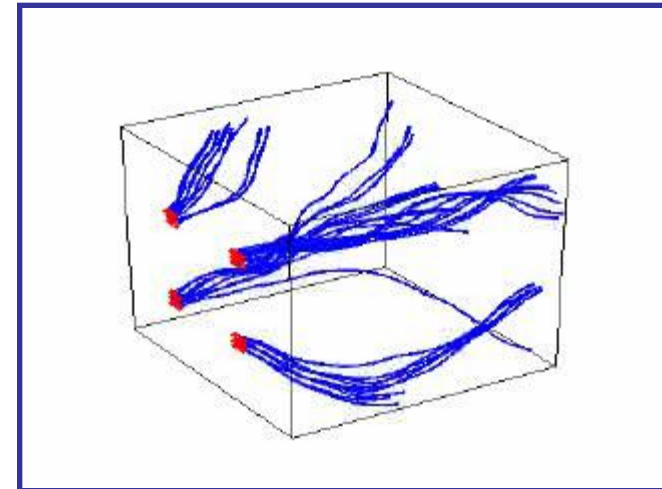


## 2D (+slab)

- Finite perpendicular correlation length
- Flux tubes “shred”

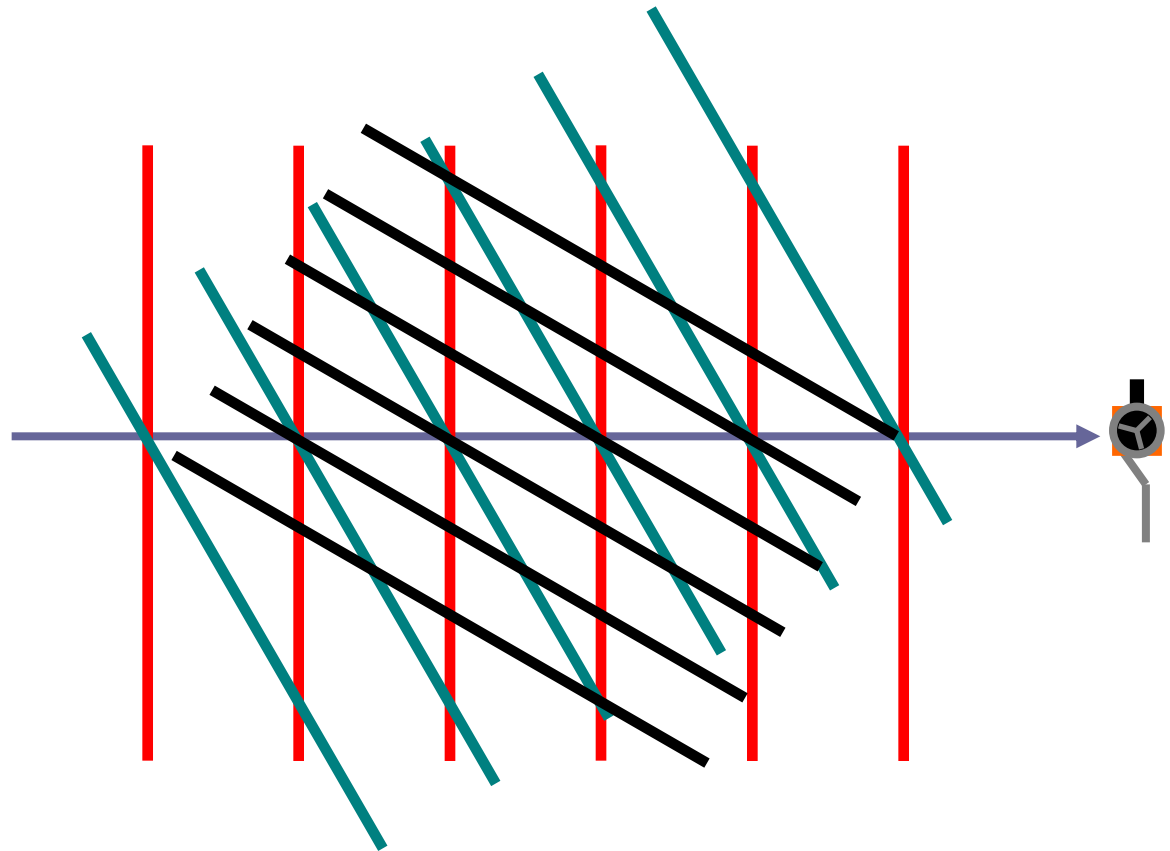


→ Important consequences for particle transport



# Measuring anisotropy: reduced spectrum

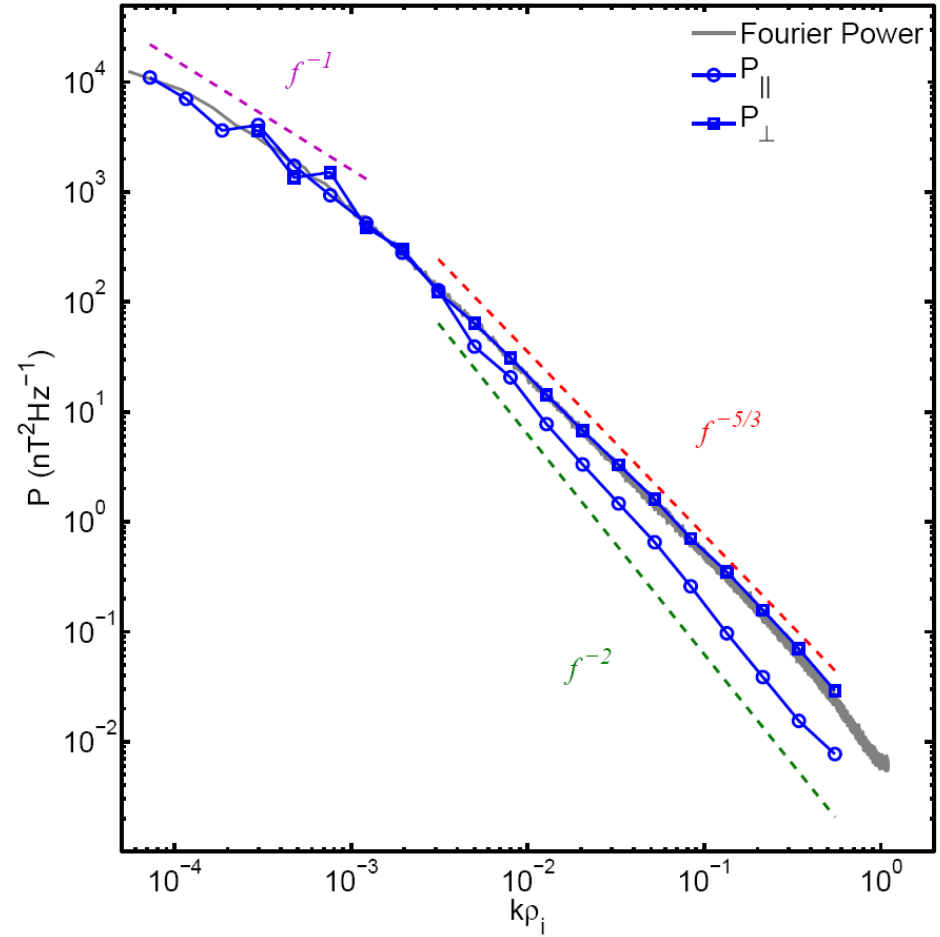
- For a given spacecraft frequency  $f$ , this corresponds to a flow-parallel scale  $\lambda = V_{SW} / f$
- ...and a flow-parallel wavenumber  $k_{||} = 2\pi f / V_{SW}$
- But sensitive to all waves with  $k \cdot V_{SW} = 2\pi f$



→ “reduced spectrum”

# Power anisotropy

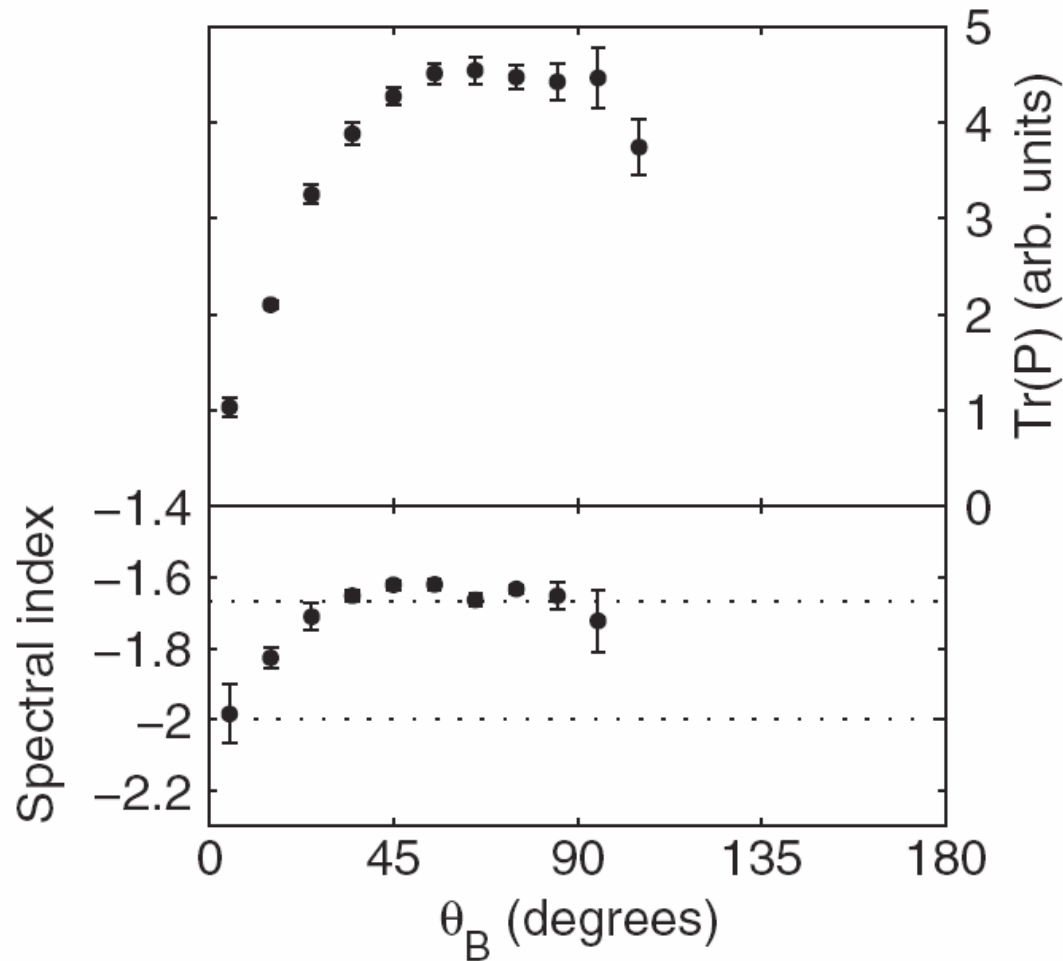
- Significant power anisotropy in the inertial range
- Power anisotropy seems to be generated through cascade
- Note: isotropy at the “outer scale”
- Wicks et al., Mon. Not. Roy. Astron. Soc., 2010



# Consistency with critical balance

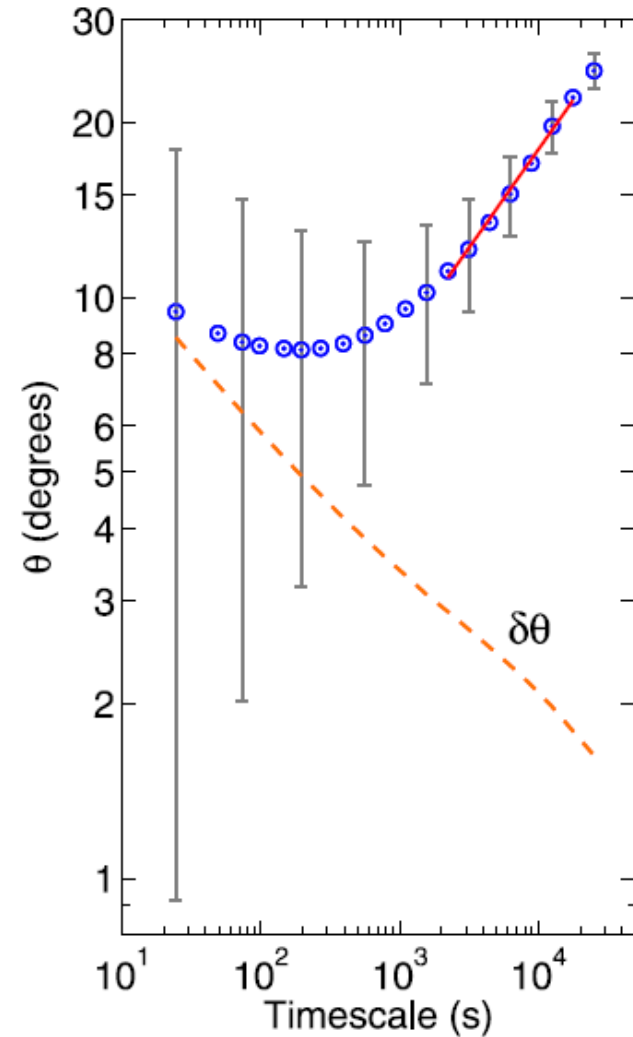
## Inertial range

- $5/3$  spectral index perpendicular to field
- 2 spectral index parallel to field
- Consistent with critical balance
- Other explanations are possible!
- Horbury et al., 2008

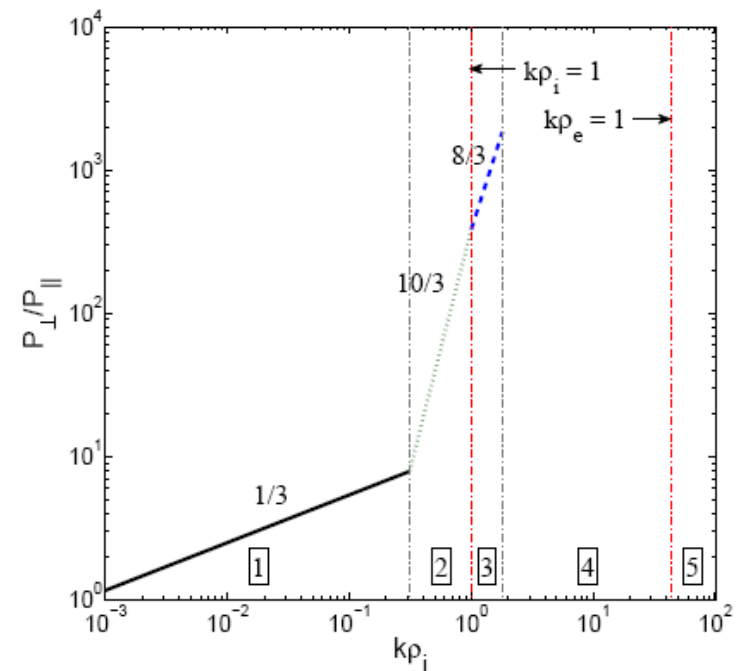
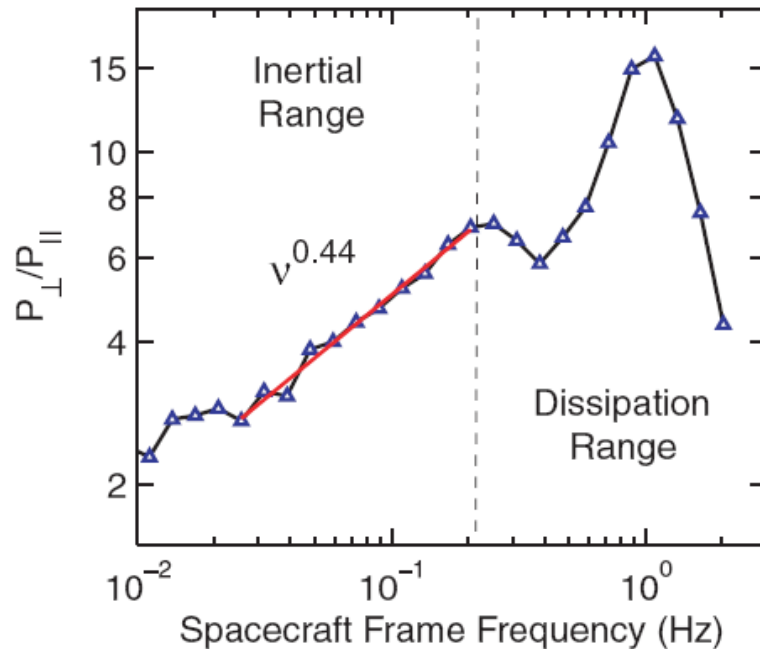


# Dynamic alignment in the solar wind?

- Boldyrev, 2005
  - Angle between  $\delta b$  and  $\delta v$  should reduce down the cascade
- Podesta et al., J. Geophys. Res., A01107, 2009
  - Evidence for dynamic alignment in the solar wind?
- Timescale consistent with inertial range?



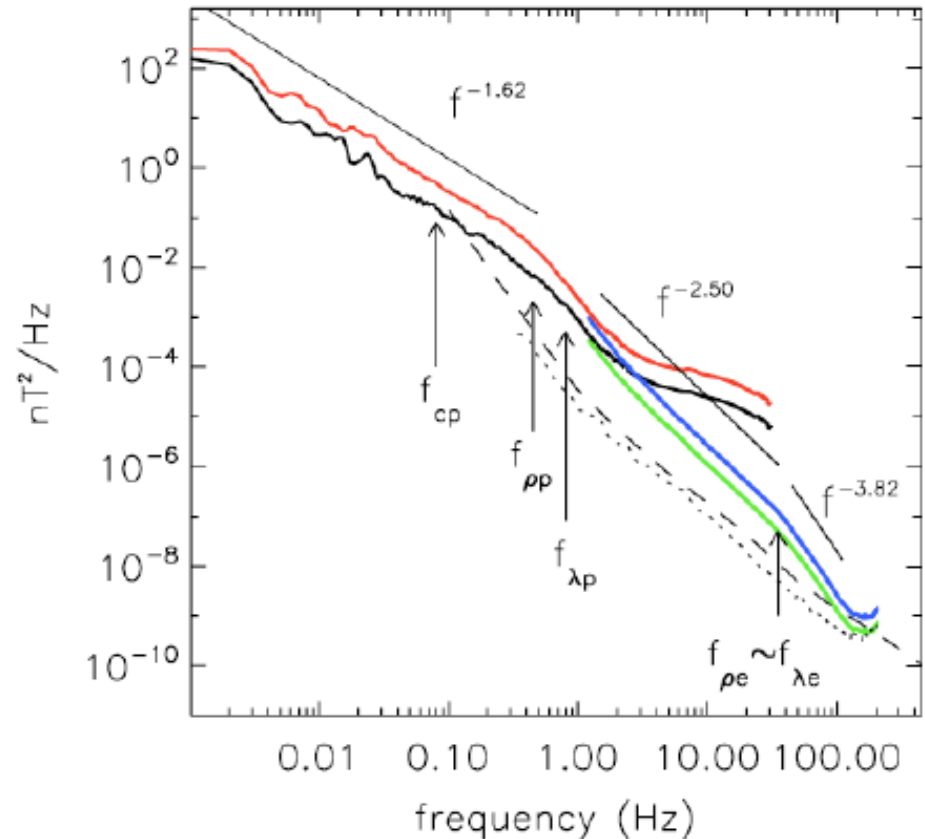
# Transition to ion kinetic scales



- How does anisotropy vary across the transition to ion kinetics?
- Podesta, 2009: evidence for decreased anisotropy at ion gyroscale: instabilities?
- Chen et al., 2010: predictions for scaling based on CB gyrokinetic scalings

# Kinetic effects

- Multiple possible dissipation mechanisms
    - Whistlers, kinetic Alfvén waves, ...
  - Which one(s) is/are operating in the solar wind?
  - Evidence for another power law at smaller scales
- Continued energy transfer, not just dissipation

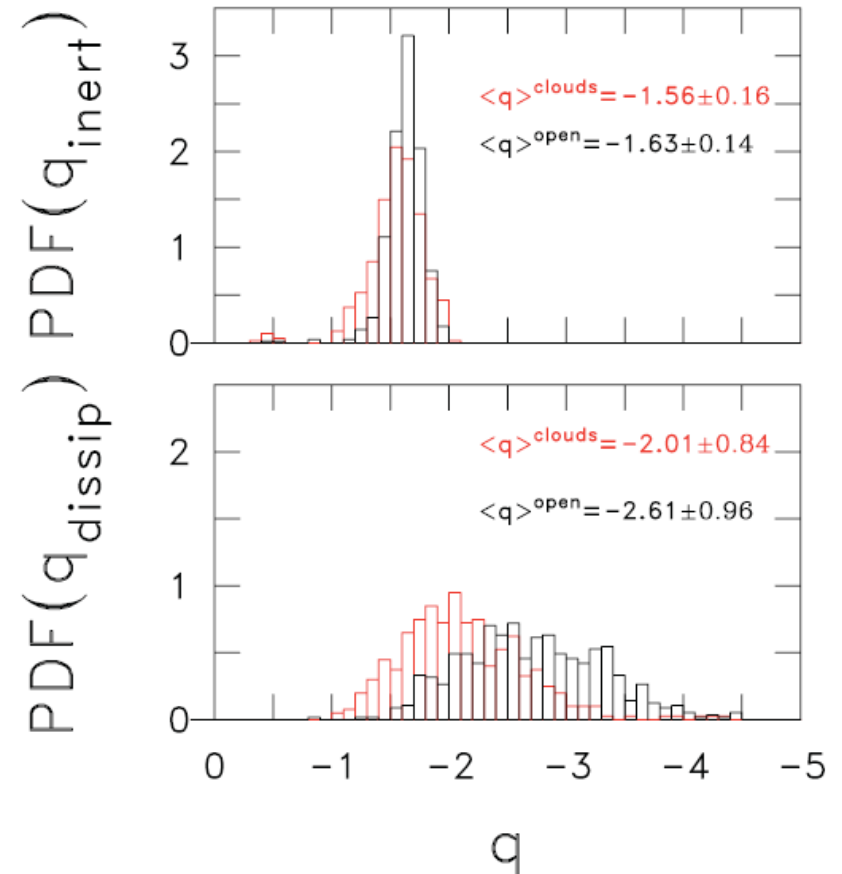


Sahraoui, 2009



# Dispersion scale spectral index

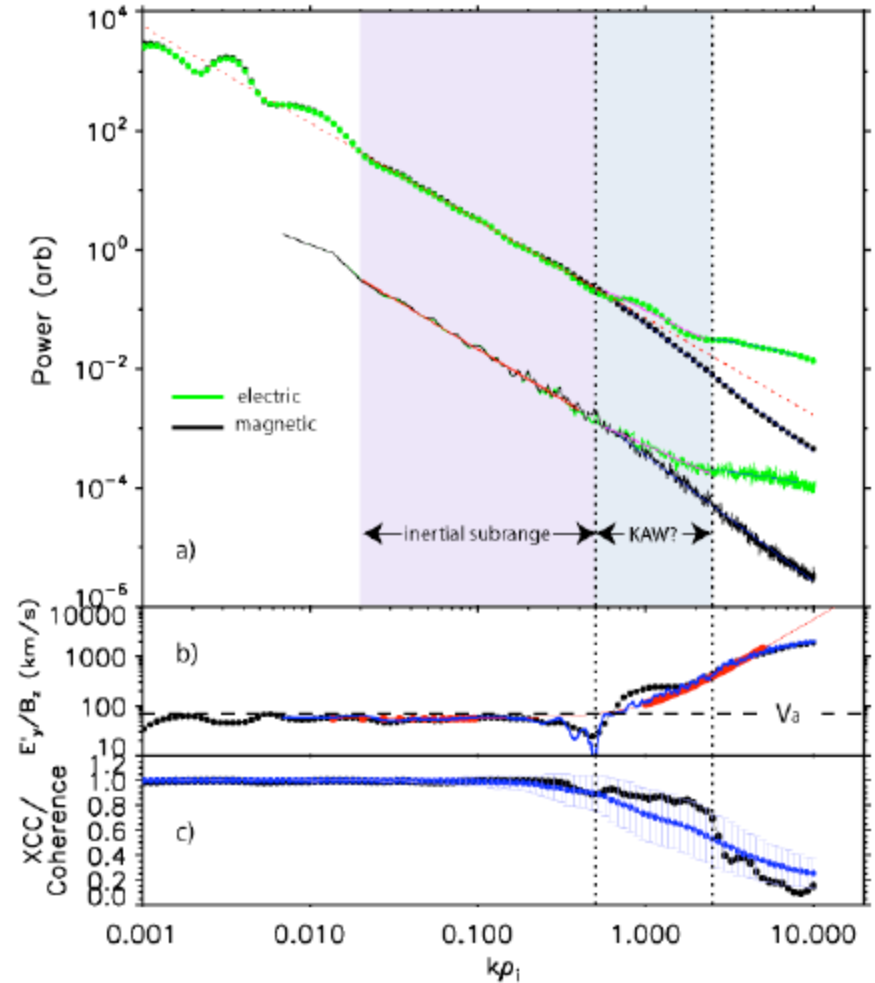
- MHD inertial range
  - Spectral index near  $5/3$
- What happens in dissipation (dispersion?) range?
- Steeper spectrum
  - **Much more variable**



Smith et al., 2006

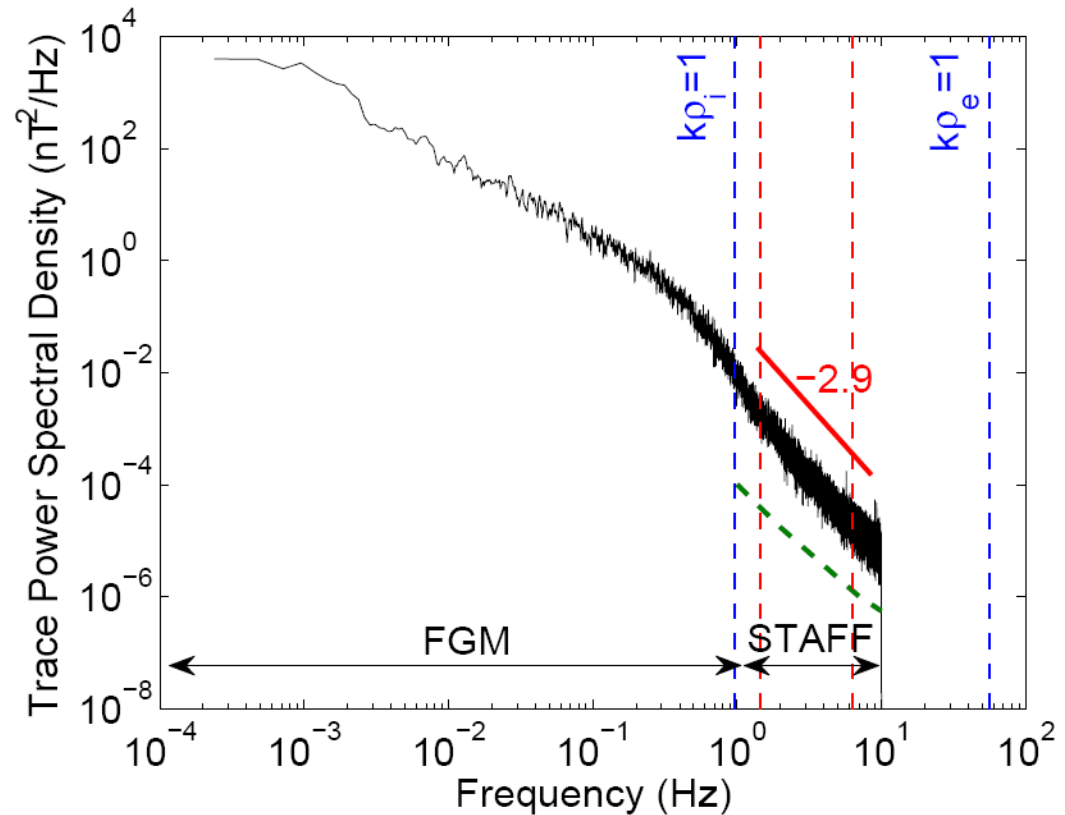
# E and B spectrum in the kinetic regime

- Evidence for kinetic Alfvén waves?
- Bale, 2005



# Dissipation scales with multi-spacecraft

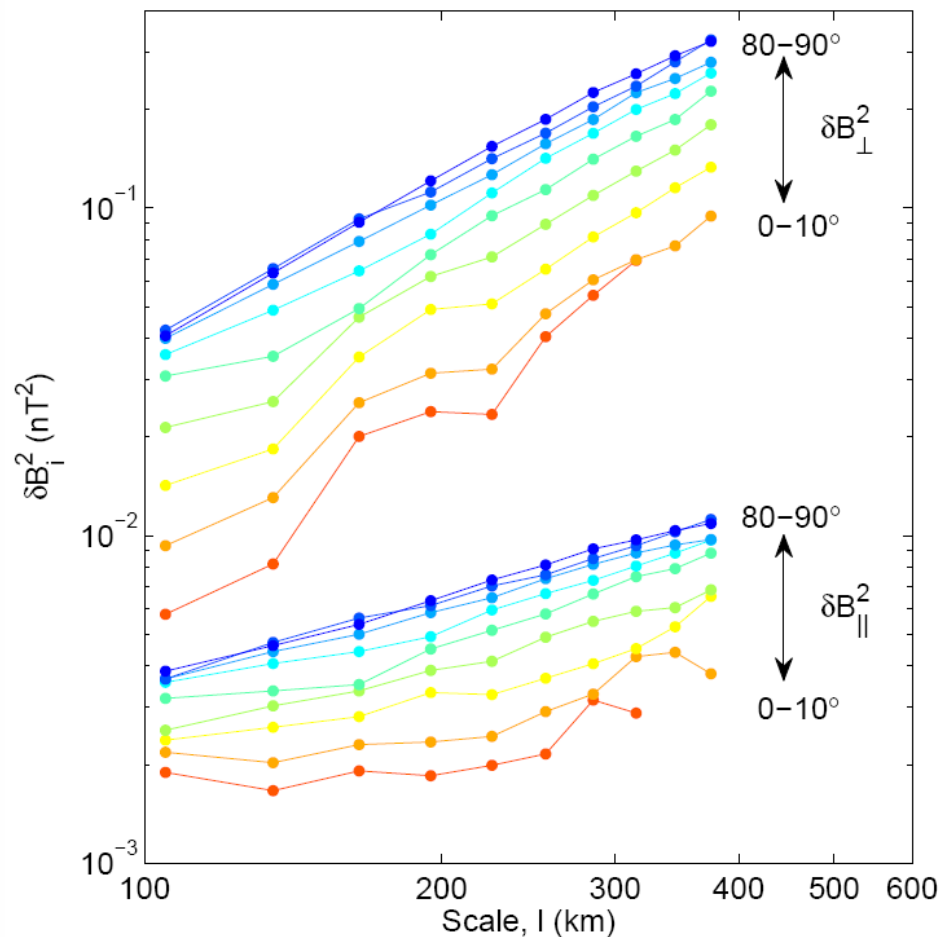
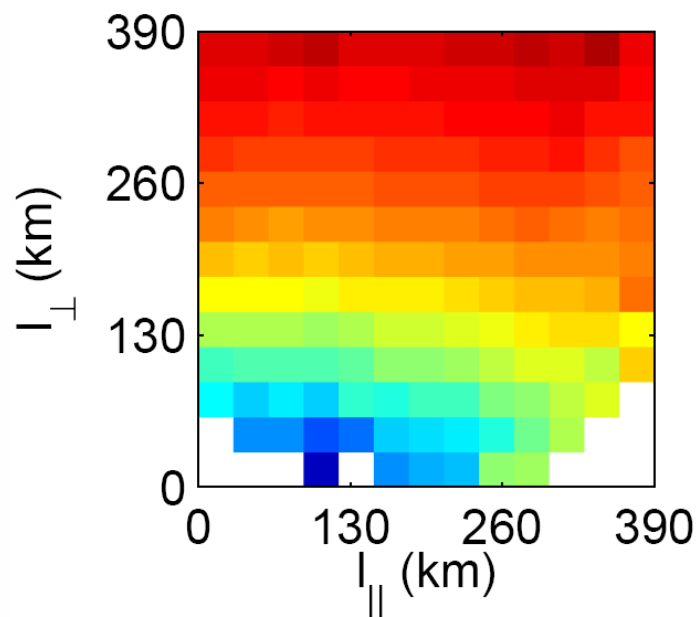
- Use four Cluster spacecraft on 100km scales
  - Provides information down to tens of km
- First measurement of power and spectral index anisotropy on dissipation scales



Chen et al., 2010

# Multi-point structure functions

- Power law scaling on ion kinetic scales -> turbulent cascade
- Chen et al., PRL, 2010



# Anisotropy on ion kinetic scales

- See power anisotropy similar to MHD scales

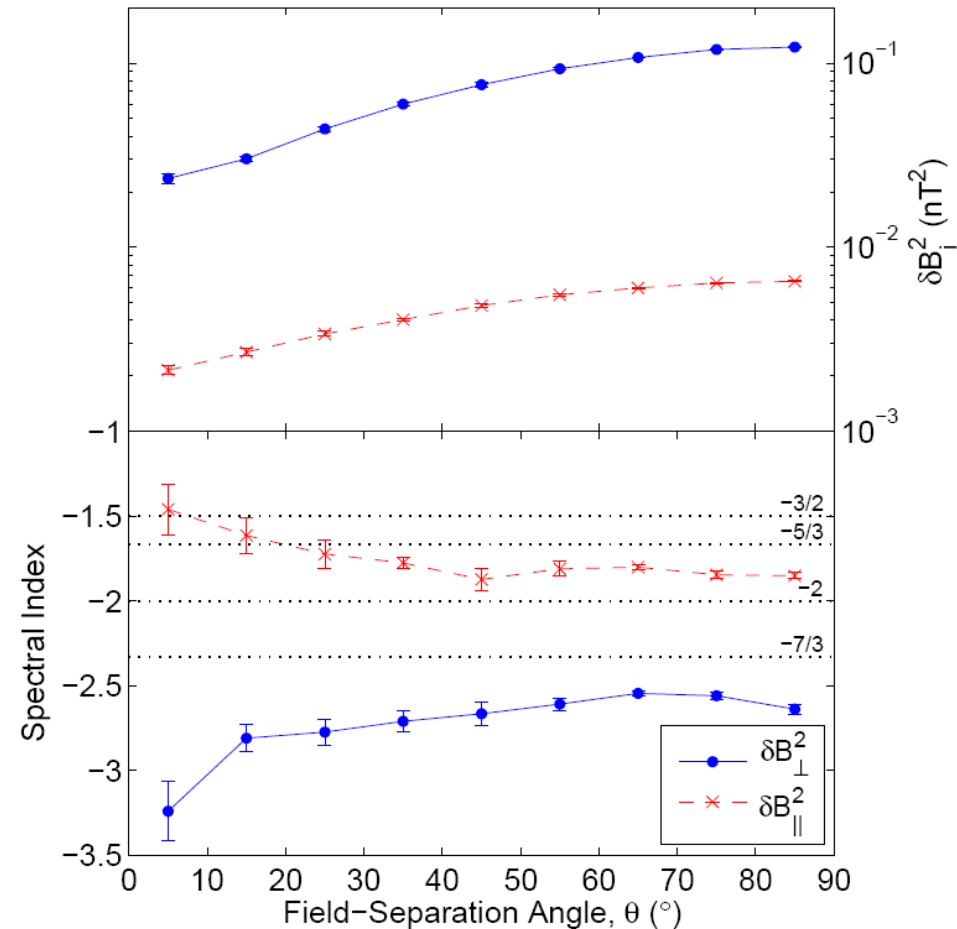
## Field-perpendicular fluctuations

- Spectral index variations consistent with critically-balanced kinetic Alfvén waves

## Field-parallel fluctuations

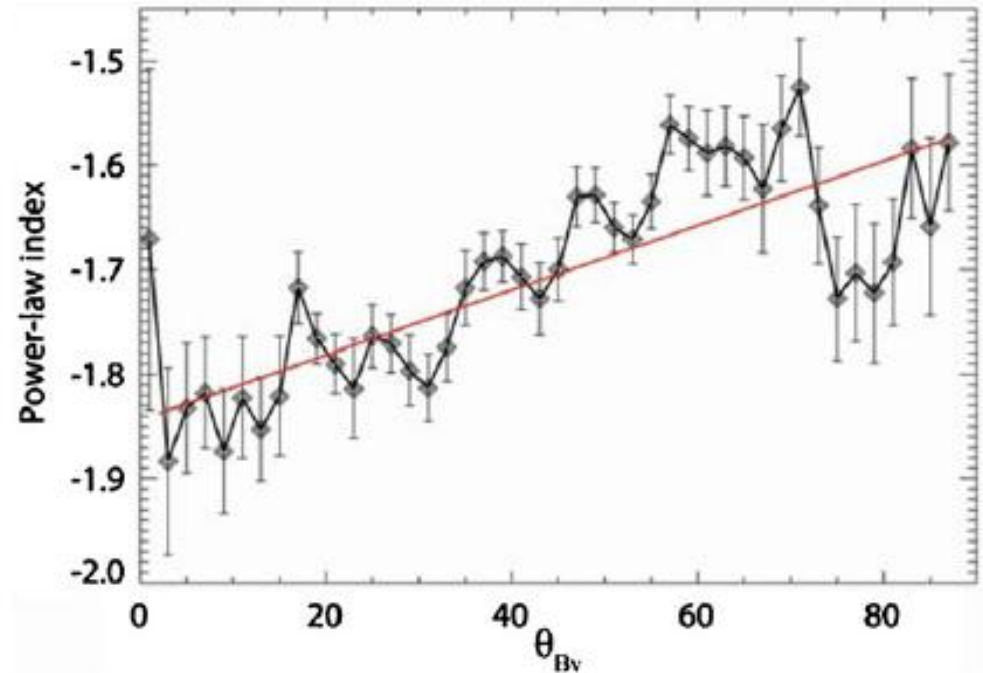
- Not consistent with critically-balanced kinetic Alfvén waves

Chen et al., PRL, 2010



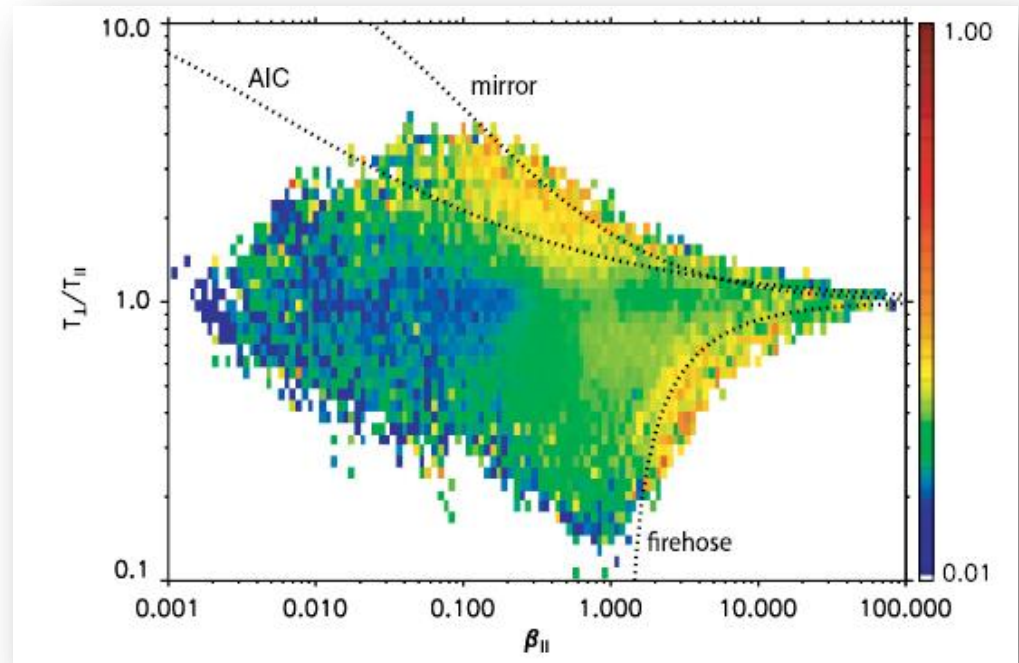
# Anisotropic density scaling in the ion kinetic range

- Evidence for anisotropic scaling of density fluctuations
- Malaspina et al., 2010
- This is in the ion kinetic range
- Not consistent with theory?



# Kinetic instabilities

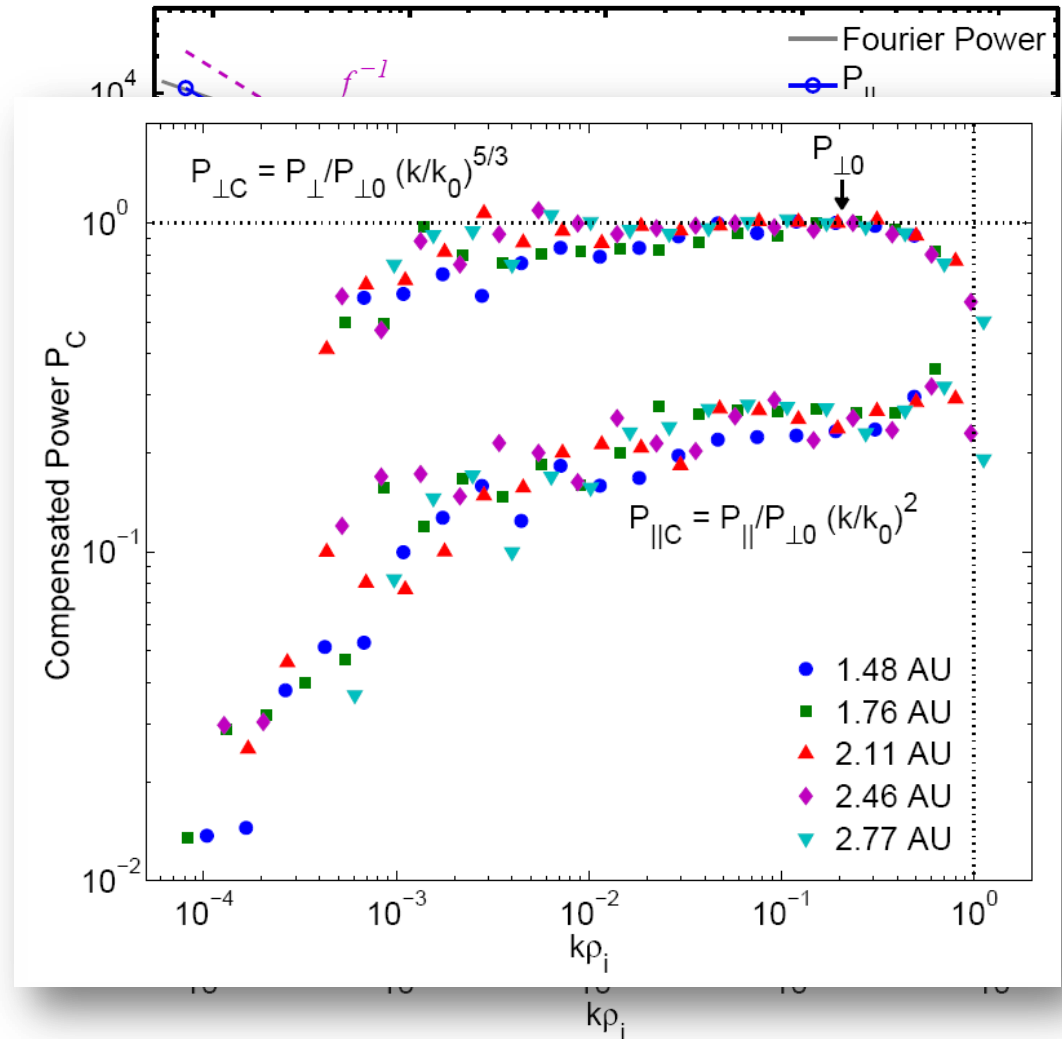
- Expansion of solar wind drives particle distributions towards firehose and mirror mode instabilities (Kasper, Hellinger, Matteini)
- Good evidence for generation of fluctuations on ion kinetic scales due to these
- See talks by Bale, Kasper



Bale et al., PRL, 2009

# Evidence for firehose instability

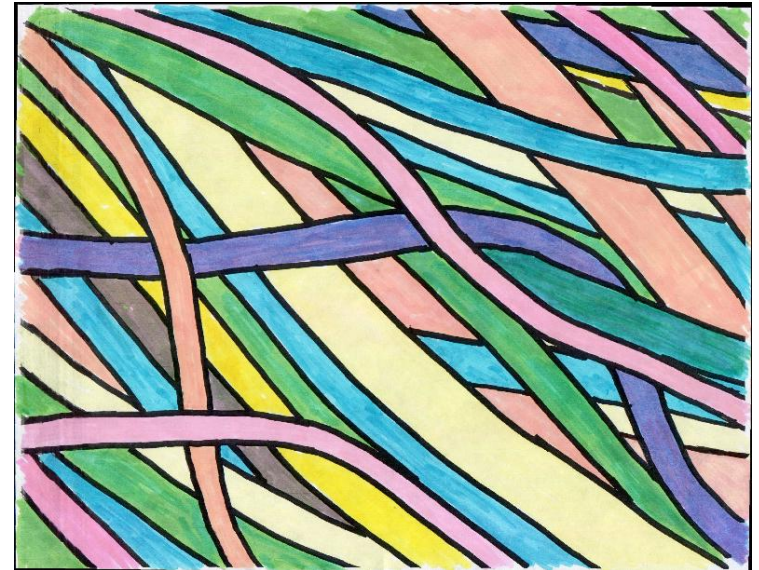
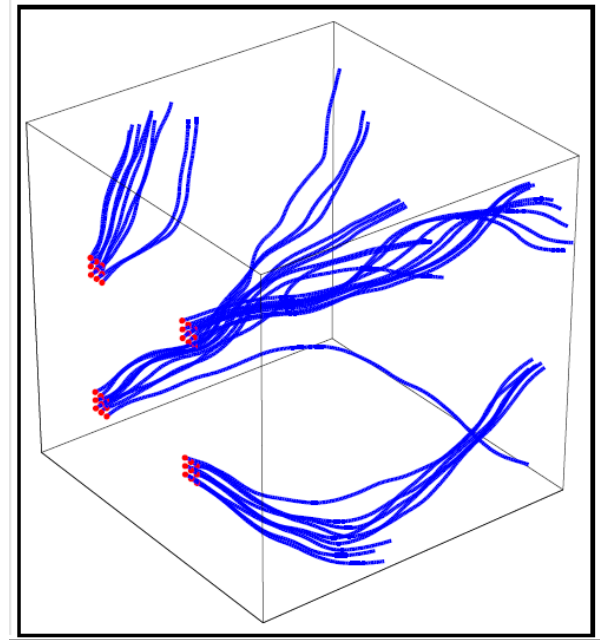
- Consistent with plasma near firehose instability
- Appears to have field-parallel wavevector
- Only visible using wavelet analysis
- Wicks et al., MNRAS, 2010





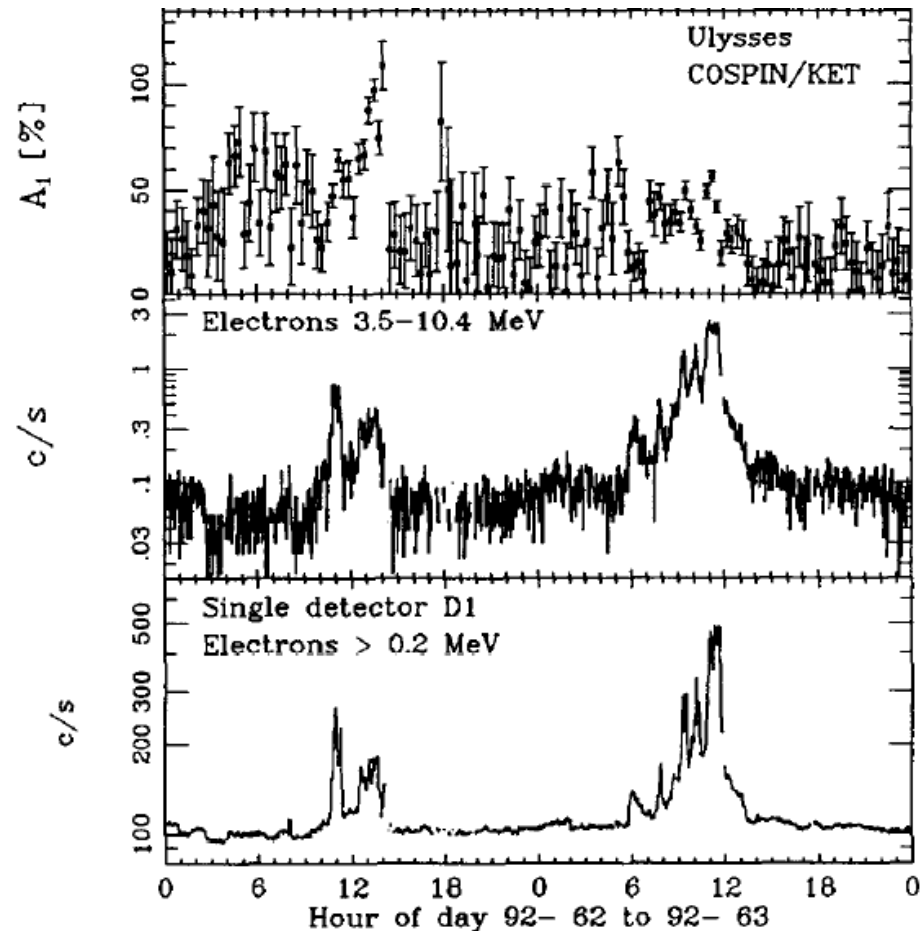
# Discontinuities vs turbulence

- Turbulence
  - Field-perpendicular cascade generates short scales across the field
  - Tube-like structures
  - Not topological boundaries
- Flux tubes
  - Sourced from Sun
  - Topological boundary?
- Solar wind is likely a combination of both at the same time



# Using particles to study turbulence

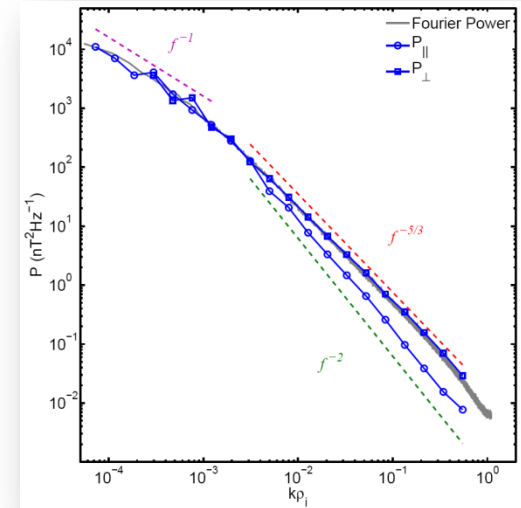
- Jovian electron bursts
  - Electrons highly tied to field lines
  - Relativistic electrons are instantaneous diagnostics of connectivity
  - Seen up to several hundred million km from planet
- Evidence for very fine scale structure



Ferrando et al., 1993

# Summary and questions

- Anisotropic cascades on both MHD and ion kinetic scales
- Anisotropy in magnetic field, velocity and density, but some differences
- Evidence for kinetic instabilities, sometimes
- Imbalance is also sometimes present



## Outstanding questions

- Is critical balance actually present on MHD or ion kinetic scales?
- What is the form of the ion kinetic cascade?
- What is the effect of imbalance?
- How important are instabilities and/or structures in solar wind dynamics?

