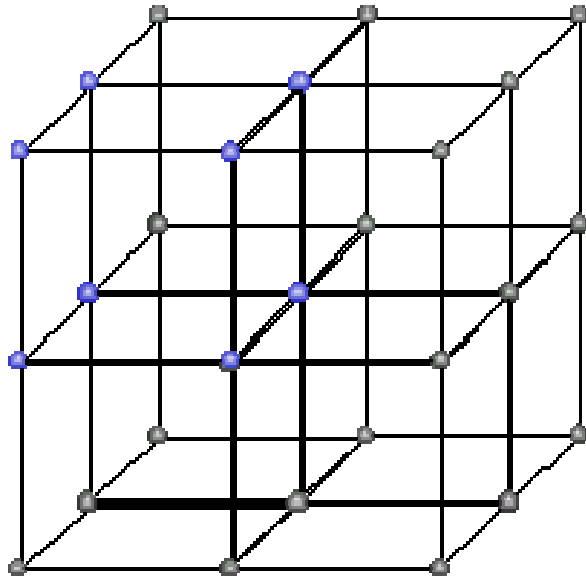
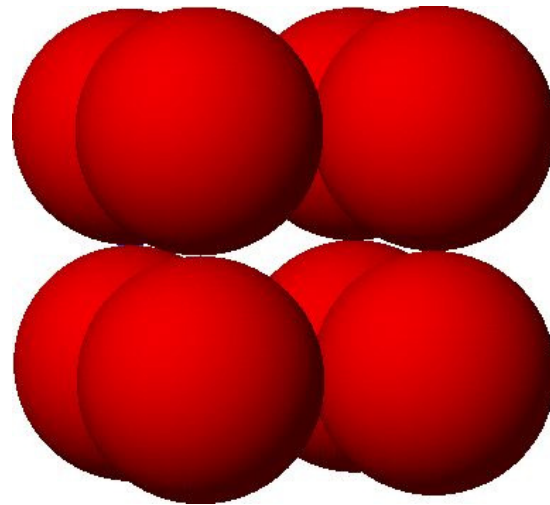
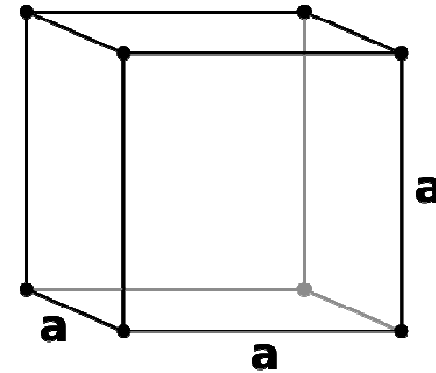


Slides  
Condensed Matter Physics  
Lecture 10

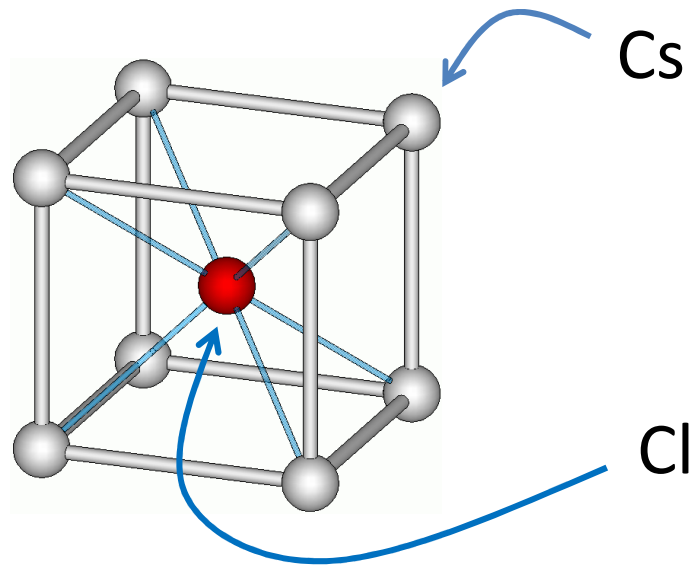
# Simple (Primitive) Cubic Lattice (Notated Cubic-P)



## Simple Cubic Unit Cell



Atoms arranged in  
Simple Cubic Lattice  
(very unusual)

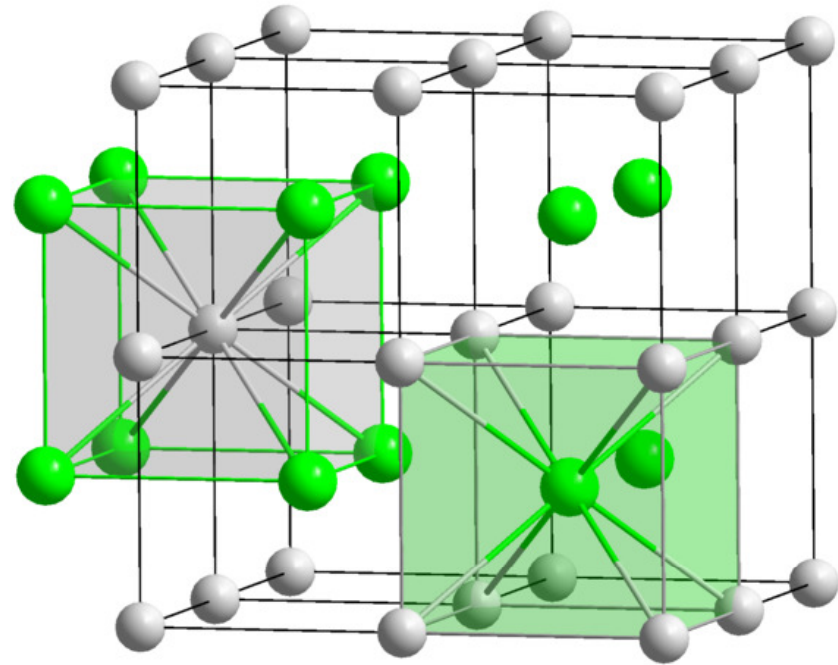
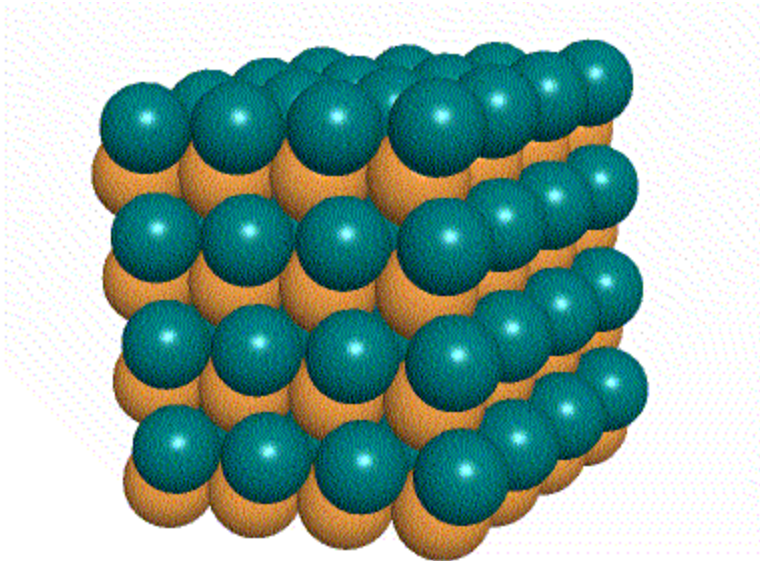


Cesium Chloride (CsCl): A simple cubic Lattice with a Basis

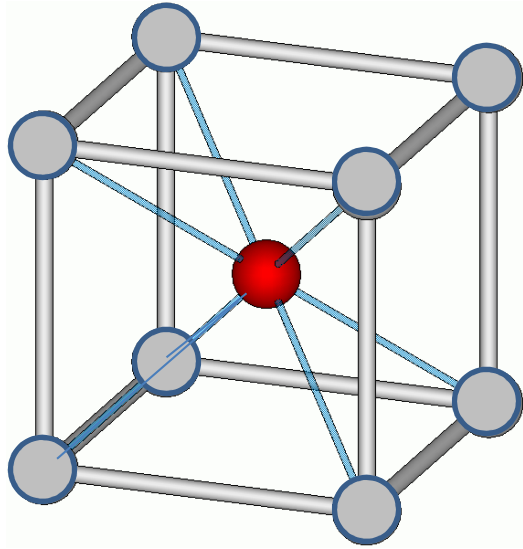
Basis:

Cs at  $[0, 0, 0]$  (i.e., on the simple cubic)

Cl at  $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$  (i.e., in the middle of each cube)

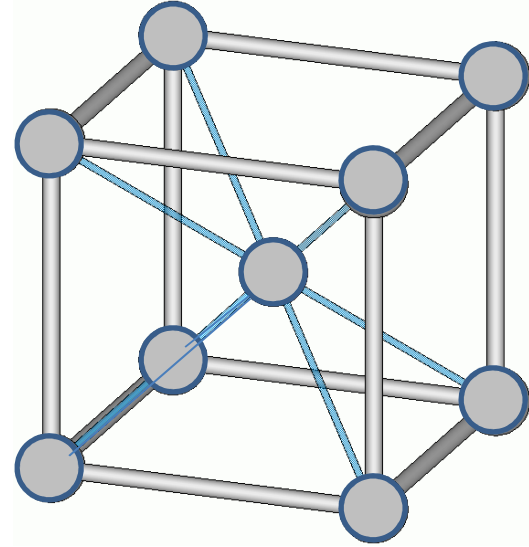


Two depictions of the CsCl lattice structure =  
Two interlocking simple cubics



CsCl = Simple Cubic  
with Basis

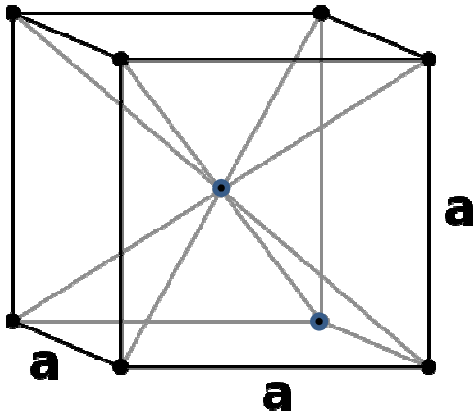
Cs at  $[0, 0, 0]$   
Cl at  $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$



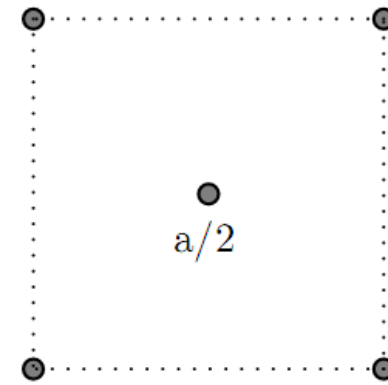
Cs = Simple Cubic  
with Basis

Cs at  $[0, 0, 0]$   
Cs at  $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$

Unit cell of Body Centered Cubic Lattice (BCC) (Notated cubic-I)

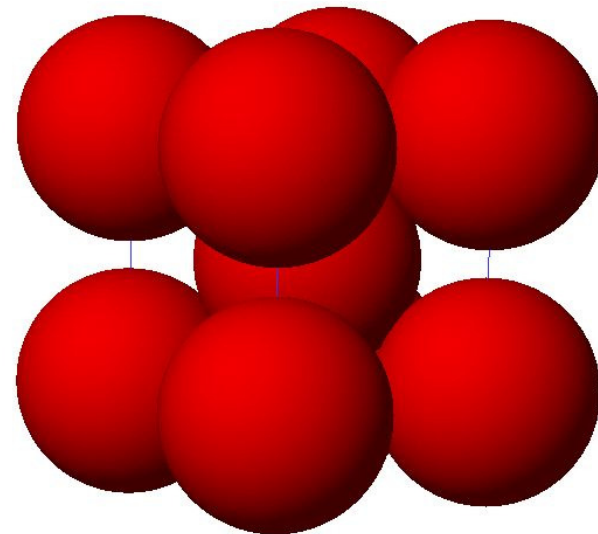


Conventional Unit Cell

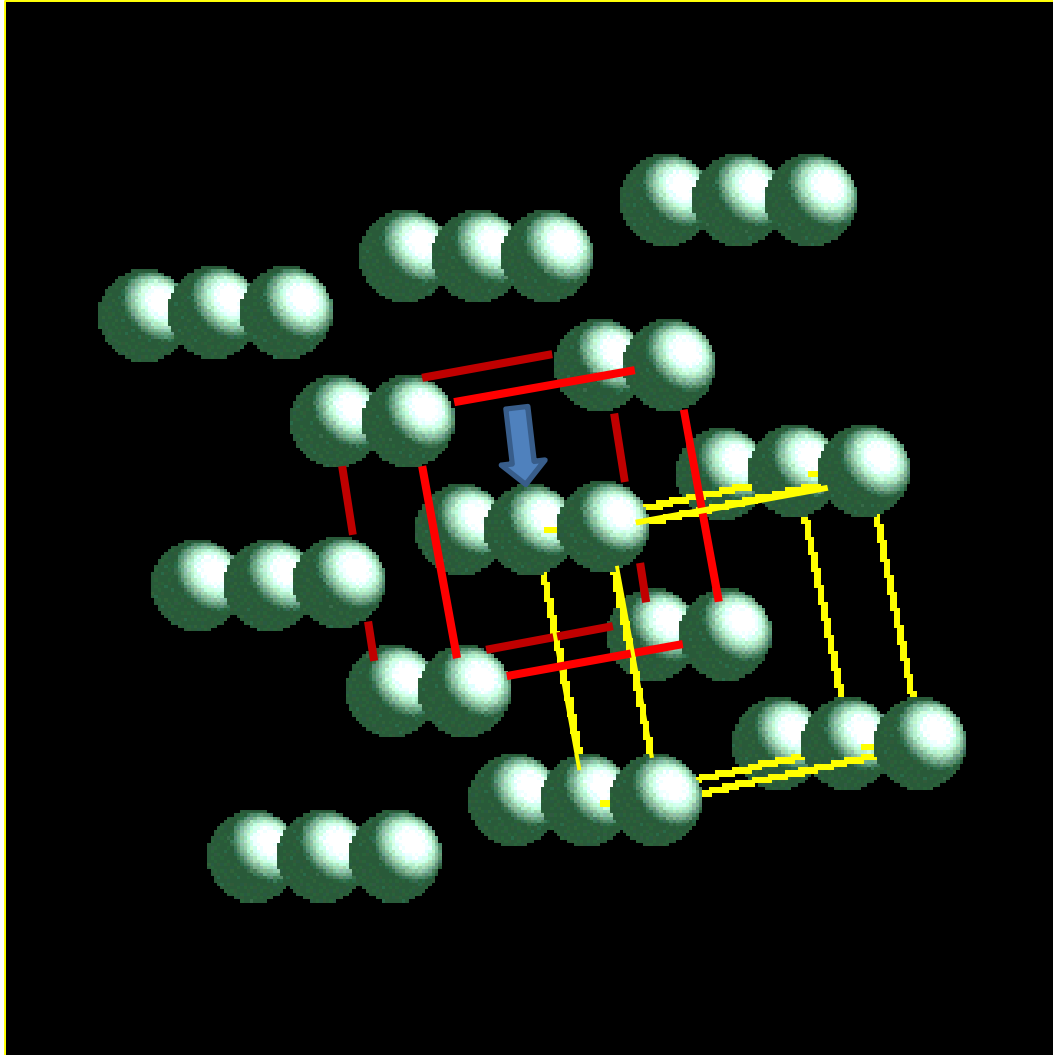


Plan View

(unlabeled points at height 0 and a)

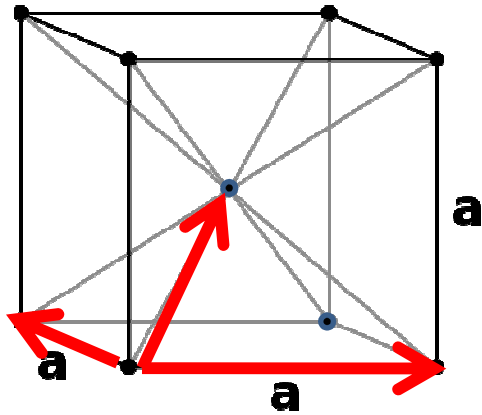


(More efficient sphere packing)

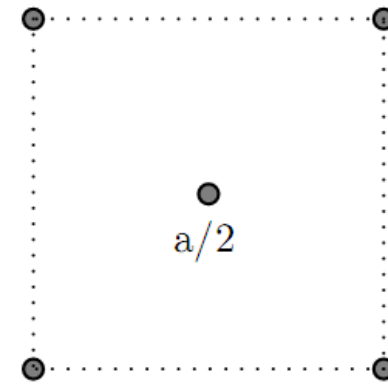


BCC Lattice

Unit cell of Body Centered Cubic Lattice (BCC) (Notated cubic-I)

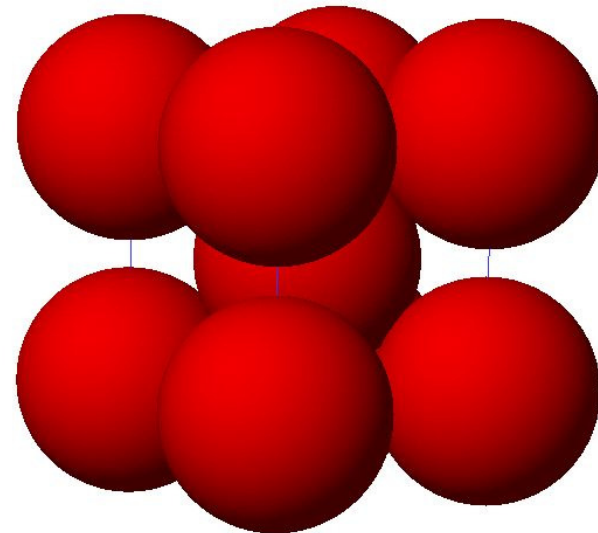


Conventional Unit Cell



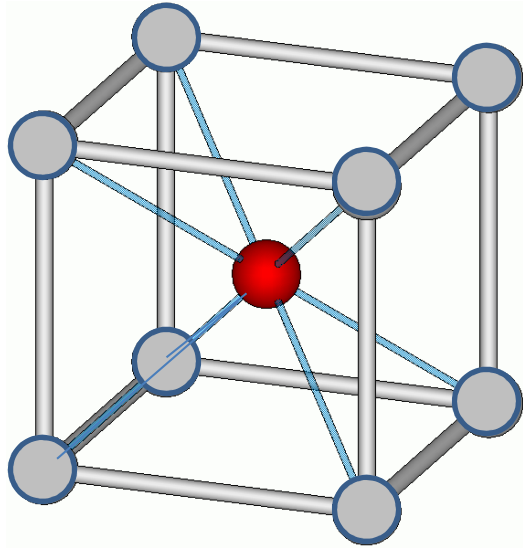
Plan View

(unlabeled points at height 0 and a)



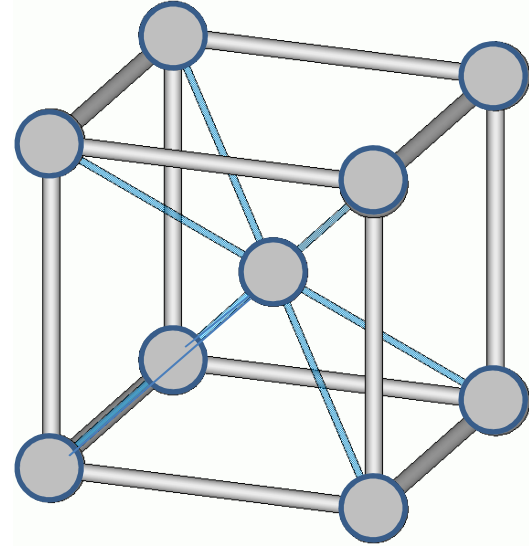
(More efficient sphere packing)





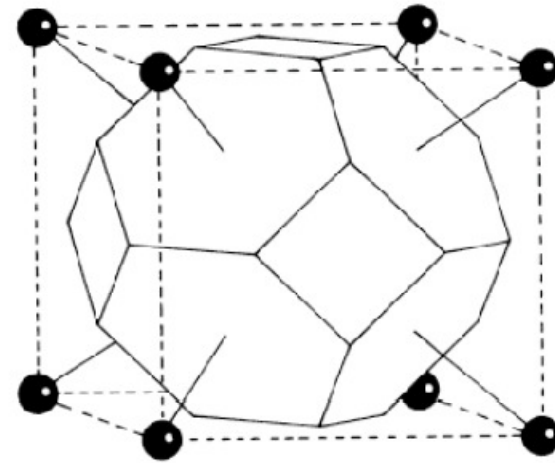
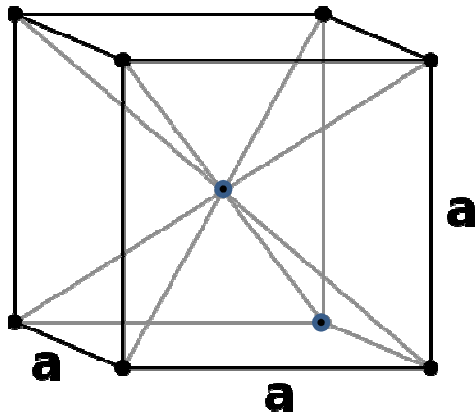
CsCl = Simple Cubic  
with Basis

Cs at  $[0, 0, 0]$   
Cl at  $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$

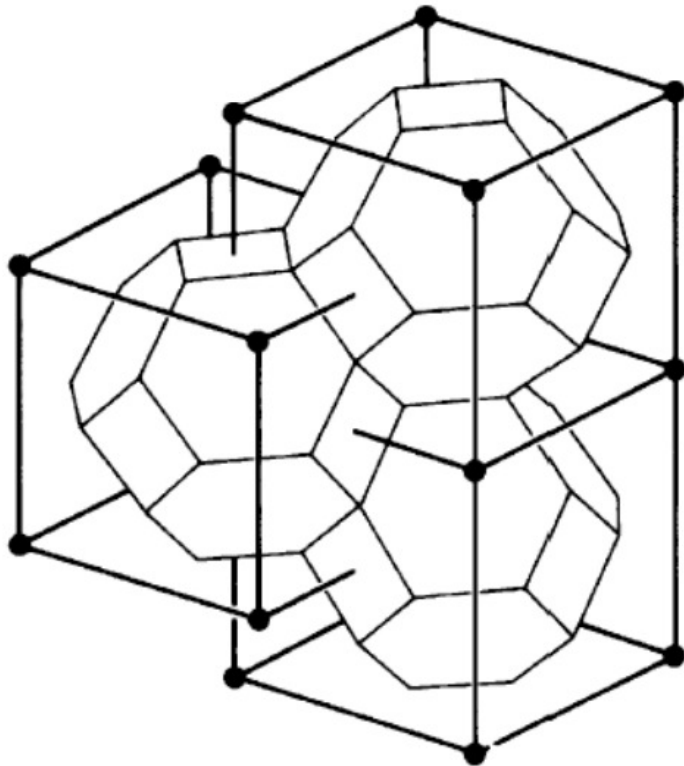


Cs = Simple Cubic  
with Basis

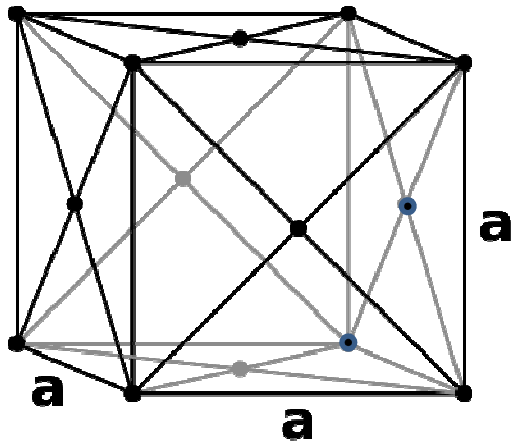
Cs at  $[0, 0, 0]$   
Cs at  $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$



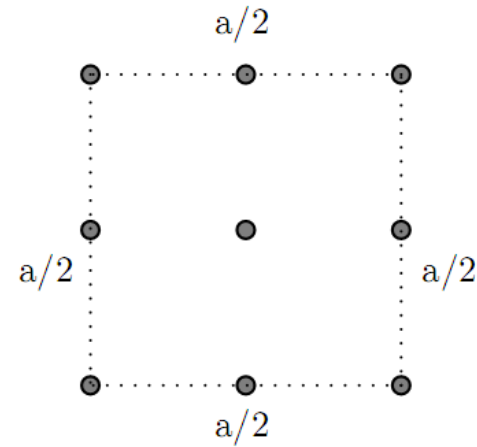
The Wigner-Seitz (Primitive)  
Unit Cell for the BCC lattice



# Unit cell of Face Centered Cubic Lattice (FCC) (Notated cubic-F)

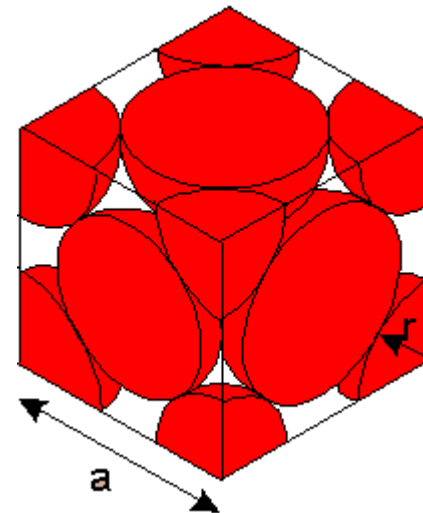


Conventional Unit Cell

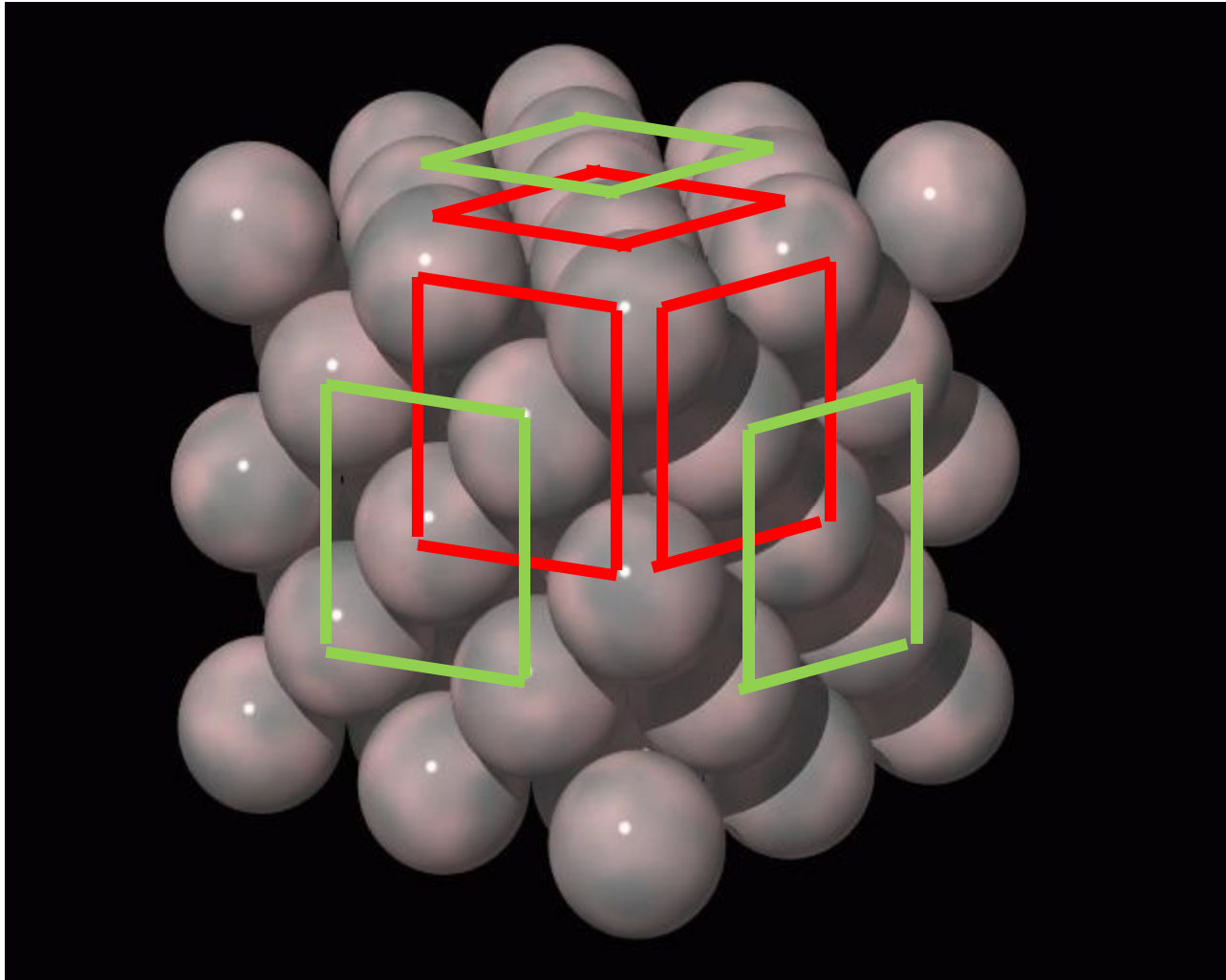


Plan View

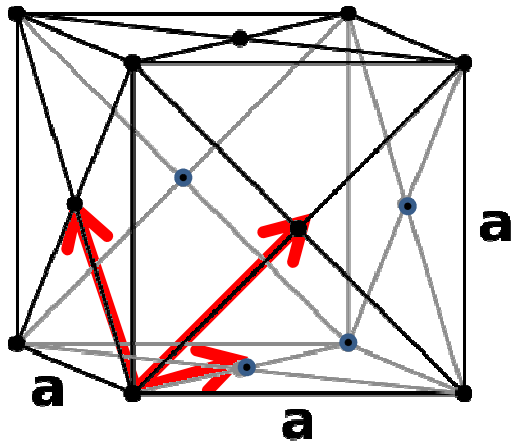
(unlabeled points at height 0 and a)



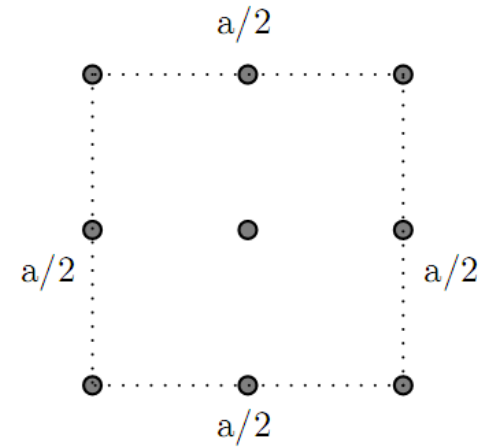
Most efficient sphere packing  
same density as "hcp" packing which  
we don't learn this year



# Unit cell of Face Centered Cubic Lattice (FCC) (Notated cubic-F)



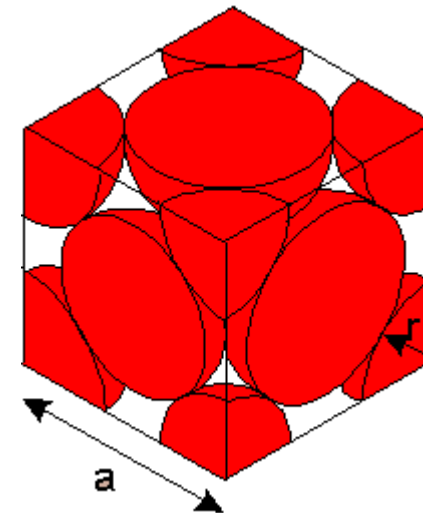
Conventional Unit Cell



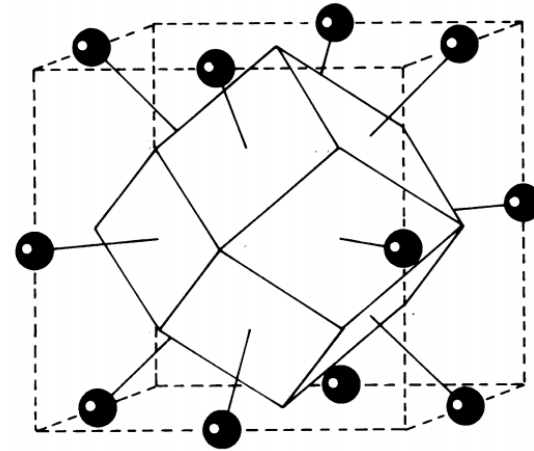
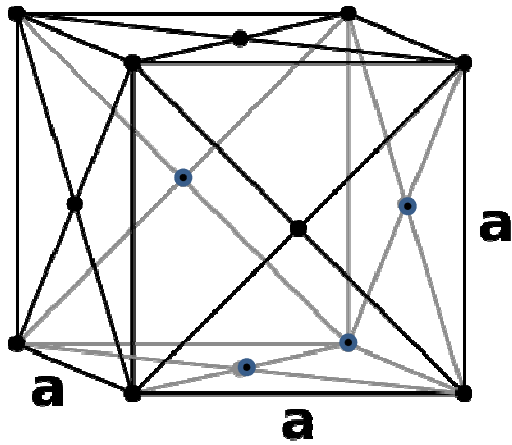
Plan View

(unlabeled points at height 0 and a)

## FCC lattice



Most efficient sphere packing  
same density as "hcp" packing which  
we don't learn this year



The Wigner-Seitz (Primitive)  
Unit Cell for the FCC lattice



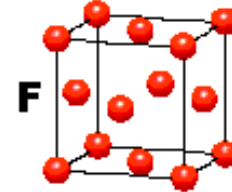
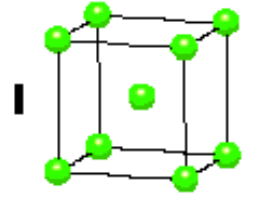
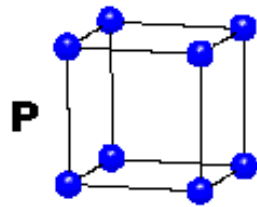
Packing Wigner Seitz  
cells to fill space

# The 14 Bravais Lattice Types

## CUBIC

$$a = b = c$$

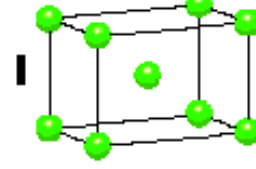
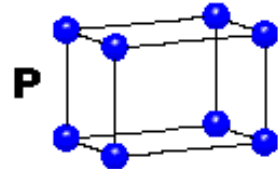
$$\alpha = \beta = \gamma = 90^\circ$$



## TETRAGONAL

$$a = b \neq c$$

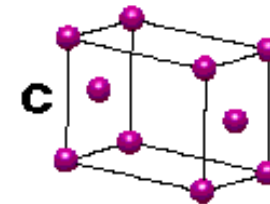
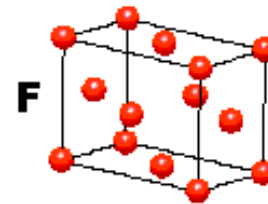
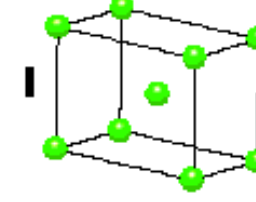
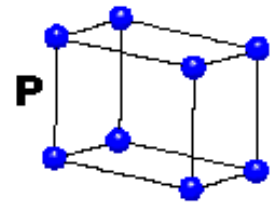
$$\alpha = \beta = \gamma = 90^\circ$$



## ORTHORHOMBIC

$$a \neq b \neq c$$

$$\alpha = \beta = \gamma = 90^\circ$$

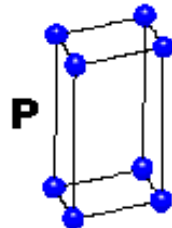


## HEXAGONAL

$$a = b \neq c$$

$$\alpha = \beta = 90^\circ$$

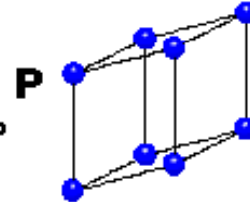
$$\gamma = 120^\circ$$



## TRIGONAL

$$a = b = c$$

$$\alpha = \beta = \gamma \neq 90^\circ$$

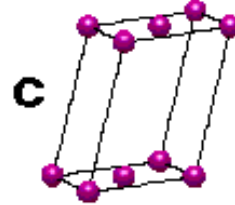
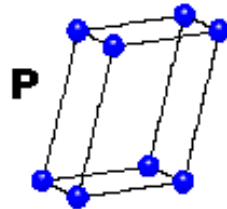


## MONOCLINIC

$$a \neq b \neq c$$

$$\alpha = \gamma = 90^\circ$$

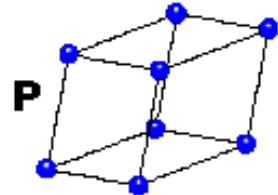
$$\beta \neq 120^\circ$$



## TRICLINIC

$$a \neq b \neq c$$

$$\alpha \neq \beta \neq \gamma \neq 90^\circ$$



### 4 Types of Unit Cell

**P** = Primitive

**I** = Body-Centred

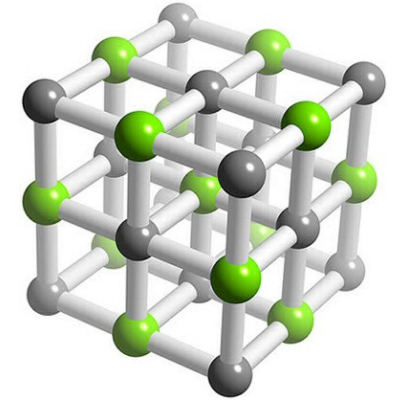
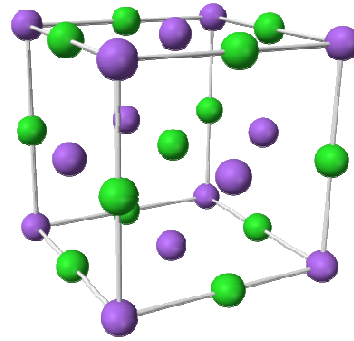
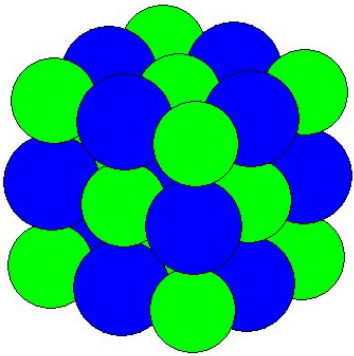
**F** = Face-Centred

**C** = Side-Centred

+

7 Crystal Classes

→ 14 Bravais Lattices



## sodium chloride (NaCl)

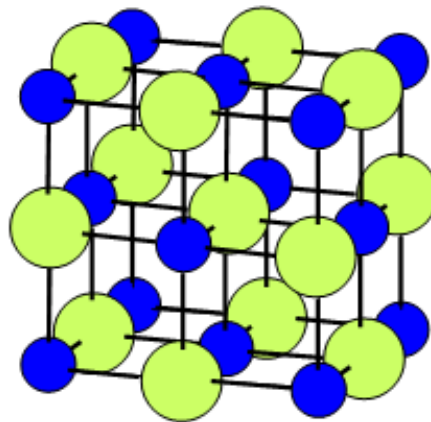
lattice: cubic F

basis :

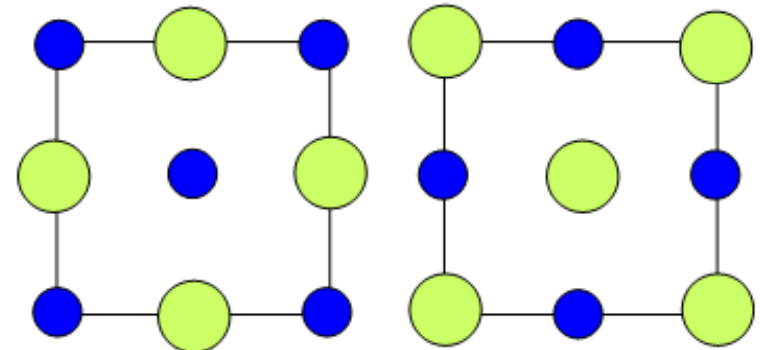
Na 000



Cl  $\frac{1}{2}\frac{1}{2}\frac{1}{2}$



Plan view



$z = 0$  layer

$z = \frac{1}{2}$  layer

Na forms FCC lattice.

Cl is displaced  $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$  from each Na



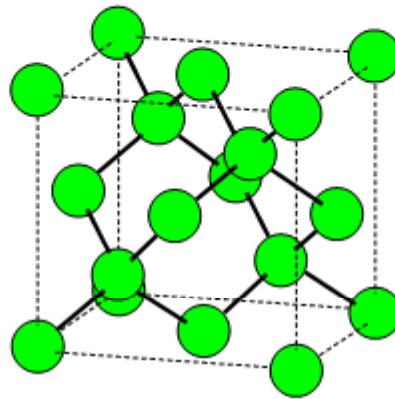
# diamond (C) — also Si, Ge

lattice: cubic F

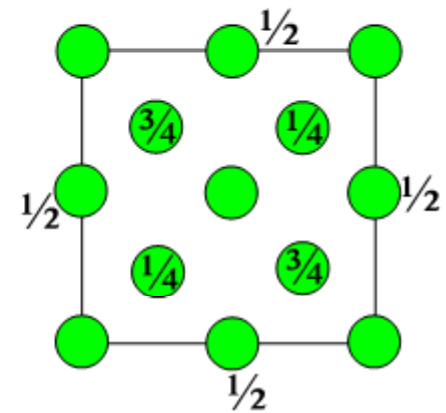
basis :

C 000     ●

C  $\frac{1}{4}\frac{1}{4}\frac{1}{4}$      ●

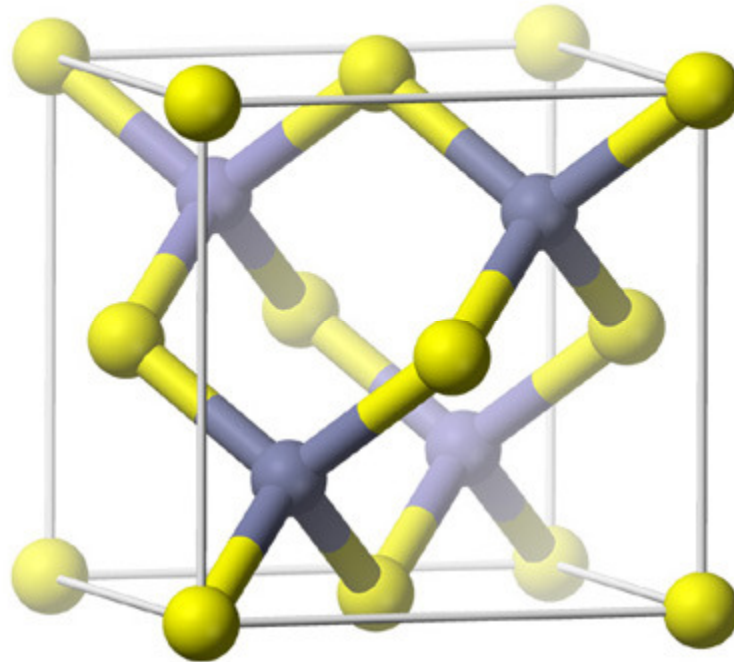


Plan view



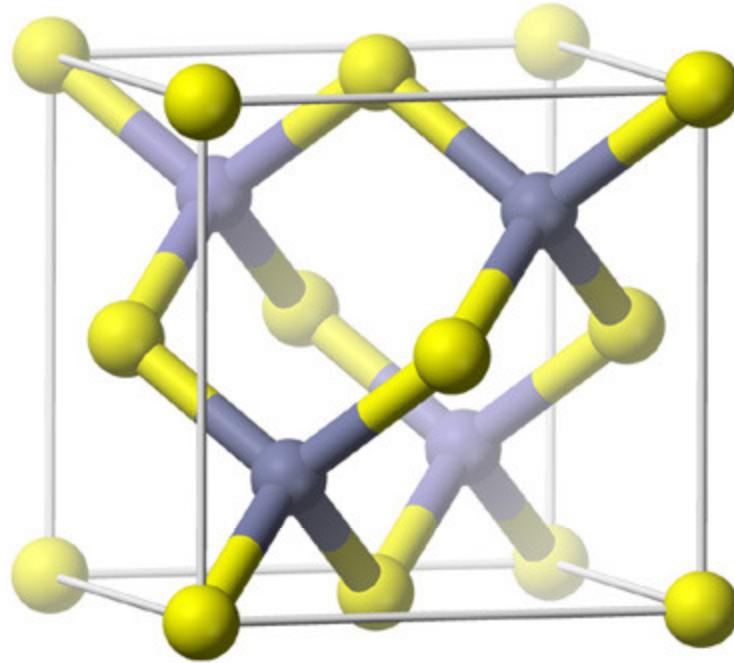


GaAs Structure...





GaAs Structure...



FCC:

Basis: Yellow at  $(0,0,0)$

Blue at  $(1/4,1/4,1/4)$