### Magnetically generated currents in the QGP

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arXiv:1401.3805 with D. Kharzeev and K. Rajagopal arXiv:1212.3894 with I. Iatrakis, E. Kiritsis, F. Nitti, A. O' Bannon

# **QCD under external magnetic fields**

- Schwinger pair production if  $F > m_e^2/e$  for  $eB \approx 10^{13}$  G.
- Magnetic catalysis: B (de)catalyzes  $\langle \bar{q}q \rangle$ ,  $T_c(B)$  is complicated Bali et al '12
- rho-meson condensation ⇒ superconducting QCD vacuum! Chernodub '10
- Changes in the phase diagram in  $\mu T B$

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This talk: Electric currents in QGP generated by magnetic fields

- Chiral anomaly Kharzeev, McLerran, Warringa '07
- Faraday + Hall in expanding plasmas U.G, Kharzeev, Rajagopal '14

# Heavy ion collisions and magnetic fields



- Initial magnitude of B
- Bio-Savart:  $B_0 \sim \gamma Z e \frac{b}{R^3} \Rightarrow$ ~  $10^{18} (10^{19})$  G at RHIC (LHC).
- $B_0 \sim 10^{10} 10^{13}$ G (neutron stars),  $10^{15}$  (magnetars)
- More relevantly  $eB \approx 5 15 \times m_{\pi}^2$  RHIC (LHC).

#### PART I: Chiral Magnetic Current

**Chiral Anomaly in QCD** 

# **Chiral Anomaly in QCD**

- *massless* fermions are chiral: left and right-handed quarks.
- Classically QGP chiral symmetric:  $N_L = N_R$ as  $T \approx 500 \text{ MeV} \gg m_u, m_d$
- Axial current  $\partial_{\mu}J^{\mu5} = \partial_{\mu}\left(\langle \bar{\psi}\gamma^{\mu}\psi\rangle_{L} \langle \bar{\psi}\gamma^{\mu}\psi\rangle_{R}\right) = 0$
- However there is a QM anomaly:  $\partial_{\mu}j^{\mu 5} = -\frac{N_f g^2}{16\pi^2}F^a_{\mu\nu}\tilde{F}^{\mu\nu}_a$ .

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- Due to topologically non-trivial gluon configurations
- Gluon winding number:  $Q_w = \frac{g^2}{32\pi^2} \int d^4x F^a_{\mu\nu} \tilde{F}^{\mu\nu}_a \in \mathbb{Z}.$
- Atiyah-Singer index theorem:  $\Delta(N_L N_R) = 2N_f Q_w$

# **How to produce** $Q_w$ **in QGP?**



- Sphalerons: thermally induced changes in  $Q_w$
- The most dominant  $Q_w$  decay Moore et al '97 due to sphalerons
- Sphaleron decay rate:  $\frac{d(N_L N_R)}{dtd^3x} \approx 192.8 \,\alpha_s^5 \, T^4$

# **Chiral Magnetic Current**

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• Under B spin degeneracy of quarks lifted due  $H \sim -q\vec{s} \cdot \vec{B}$ :



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• Under B spin degeneracy of quarks lifted due  $H \sim -q\vec{s} \cdot \vec{B}$ :



- Macroscopic manifestation of the axial anomaly
- Anomalous magnetohydrodynamics:  $\vec{J} = \frac{e^2}{2\pi^2} \mu_5 \vec{B}$ Kharzeev et al '07, Son, Surowka '09
- $\mu_5$  encodes the imbalance  $N_L \neq N_R$

- If  $Q_w \neq 0$  ( or  $\mu_5$  finite )
- If there is an external magnetic field
- There exists  $J^{\mu} \propto B$  due to chiral anomaly
- In QGP the main source of  $Q_w$  is sphalerons
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• But QGP is strongly interacting... Why trust perturbative calculations?

# **Holographic calculation**



Finite T,  $N_c \gg 1$ ,  $\alpha_s \gg 1$  QFT  $\Leftrightarrow$  GR on black holes in 5D

Maldacena '97; Witten; Gubser, Klebanov, Polyakov '98

1.  $\langle \mathcal{O}(x_1)\mathcal{O}(x_2)\rangle$  computed from  $\hat{\nabla}^2\phi = m^2\phi$  on the BH.

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- 1.  $\langle \mathcal{O}(x_1)\mathcal{O}(x_2)\rangle$  computed from  $\hat{\nabla}^2\phi = m^2\phi$  on the BH.
- 2. Recall  $\omega J^{\mu 5}(\omega) \propto \text{Tr} F \tilde{F}(\omega)$ . Introduce CP odd axion a(r, x)
- 3. The source term  $\int d^4x a_0(x) \text{Tr} F \tilde{F}(x)$  with  $a(r, x) \to a_0(x)$  at the boundary.

- Initial excess  $N^5 \equiv N_L N_R$  near thermal equilibrium.
- Described by perturbation  $\mathcal{L} \to \mathcal{L} + \epsilon \mathrm{Tr} F \tilde{F}$
- Linear response theory:  $\frac{d}{dt}N_5 \to \omega J^{05} \propto \langle \text{Tr}F\tilde{F} \text{Tr}F\tilde{F}(\omega) \rangle N_5$
- Should calculate the decay rate  $\Gamma_{CS} \sim \langle \text{Tr} F \tilde{F} \text{Tr} F \tilde{F}(\omega) \rangle$
- Holography: Study  $\hat{\nabla}^2 a(r, x) = 0$  on the 5D BH.

AdS/CFT:  $\Gamma_{CS} = \frac{(g^2 N_c)^2}{256\pi^3}T^4$ , Son, Starinets '02

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Phenomenologically interesting region  $T \approx T_c$  where conformality breaks down:



### Improved holographic QCD U.G., Nitti, Kiritsis '07

• 
$$\frac{S_{GR}}{M_p^3 N_c^2} = \int d^5 x \sqrt{-g} \left( R - (\partial \Phi)^2 + V(\Phi) - \frac{1}{2N_c^2} Z(\Phi) (\partial \alpha)^2 \right)$$

- Parametrize  $Z(\lambda) = Z_0 \left( 1 + c_1 \lambda + c_4 \lambda^4 \right)$
- Result:  $\Gamma_{CS}(T_c) \geq C \, s(T_c) T_c \chi$  O'Bannon, U.G, Iatrakis, Kiritsis, Nitti '12
- where  $\chi = \frac{\partial^2 \epsilon(\theta)}{\partial \theta^2}$  is the topological susceptibility



for ihQCD to reproduce lattice  $0^{+-}$  glueball spectrum within  $1\sigma$ .

# **Summary - part I**

- Calculated the  $\Gamma_{CS}$  in non-conformal holography
- CME is proportional to  $\Gamma_{CS}$
- Comparison of AdS/CFT with non-AdS/non-CFT at  $T_c$ :  $\Gamma_{CS}^{CFT} \approx 0.045 T_c^4$  vs.  $\Gamma_{CS} > 1.64 T_c^4$
- Precise value at  $T_c$  ambiguous but a lower limit exists.
- Linear response  $\Rightarrow \mu_5 \propto \frac{\sqrt{\Gamma_{CS}}}{V_3 \chi}$
- "Realistic" holography in favor of the chiral magnetic effect in HICs

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#### Outlook:

- To fix the ambiguity, determine  $Z(\phi) \Rightarrow$  compare  $\text{Tr}F \land F$ Euclidean correlators with lattice
- Determine  $\Gamma_{CS}(B,T)$
- What is  $\mu_5$  if generated far from equilibrium?

#### PART II: Faraday + Hall currents

ongoing work with D. Kharzeev and K. Rajagopal



"Classical" currents in charged and expanding medium:

- Faraday currents  $\vec{J}_F \sim \sigma \vec{E}_F$  with  $\nabla \times \vec{E}_F = -\frac{\partial \vec{B}}{\partial t}$
- Hall currents  $\vec{J}_H \sim \sigma \vec{E}_H$  with  $\vec{E}_H = \vec{u} \times \vec{B}$
- Also a "quantum" current  $\vec{J}_{CME} \sim \mu_5 \vec{B}$  considered in part I.

# **Calculating the magnetic field in HICs**

• Maxwell with a point-like moving source source:

$$\nabla^2 \vec{B} - \partial_t^2 \vec{B} - \sigma \partial_t \vec{B} = -e\beta \nabla \times \left[ \hat{z} \delta(z - \beta t) \delta(\vec{x}_\perp - \vec{x'}_\perp) \right]$$

- Integrate over participant and spectator distributions:
  - Simplifying assumption hard-sphere distribution for spectators and participants
  - For participants empirical distribution over Y:

Kharzeev et al. 2007

 $f(Y_b) = (4\sinh(Y_0/2))^{-1} e^{Y_b/2}, \qquad -Y_0 \le Y_b \le Y_0$ 

# **Time profile of B at LHC**



• with  $\sigma = 0.023 \text{fm}^{-1}$  and with  $\sigma = 0$ :



- QGP is an expanding fluid with 4-velocity  $u^{\mu}(x)$
- One has to add the induced velocity  $v_B$  to  $u^{\mu}(x)$
- Suppose we know  $u^{\mu}$ , assume  $|\vec{v}_B| \ll |\vec{u}|$
- Treat  $v_B$  as perturbation, ignore backreaction on expanding fluid profile u:
- Construct the total 4-velocity  $V^{\mu} \sim u^{\mu} + v^{\mu}_{B}$ : contains all observable information on time varying B.

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  - 1. Boost invariance along z:  $\xi = z\partial_t + t\partial_x$
  - 2. Rotation around z:  $\xi = x\partial_y y\partial_x$
  - 3. Translations in transverse plane:  $\xi = \partial_x$  and  $\xi = \partial_y$
- Solution to  $[\xi, u] = 0$  is  $u = \partial_{\tau} (ds^2 = -d\tau^2 + \tau^2 d\eta^2 + dx_{\perp}^2 + x_{\perp}^2 d\phi^2)$
- Hydrodynamics:  $\nabla_{\mu}T^{\mu\nu} = 0$  with  $T_{\mu\nu} = \epsilon u_{\mu}u_{\nu} + p(g_{\mu\nu} + u_{\mu}u_{\nu}) + \text{visc.}$
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- Bjorken's flow: fine except transverse translations
- Gubser's flow Gubser '10
- Replace  $\xi = \partial_x$ ,  $\partial_y$  with  $\xi_i = \partial_i + q^2 \left[ 2x^i x^\mu \partial_\mu x^\mu x_\mu \partial_i \right]$
- Solution to  $[\xi, u] = 0$  is  $u = \cosh \kappa \partial_{\tau} + \sinh \kappa \partial_{\perp}$  with  $\kappa = \frac{2q^2 \tau x_{\perp}}{1+q^2 \tau^2 + q^2 x_{\perp}^2}$
- Solution to Hydrodynamics:  $\nabla_{\mu}T^{\mu\nu} = 0$  with

$$\epsilon = \frac{\hat{\epsilon}_0}{\tau^{4/3}} \frac{(2q)^{8/3}}{\left[1 + 2q^2(\tau^2 + x_\perp^2) + q^4(\tau^2 - x_\perp^2)^2\right]^{4/3}}$$

### How to test Gubser's flow?

• Hadron spectrum from hydrodynamic flow: Cooper-Frye:

 $S_i = p^0 \frac{dN_i}{dp^3} = -\frac{g_i}{(2\pi)^3} \int d\Sigma_\mu p^\mu F\left(\frac{p^\mu V_\mu}{T_f}\right)$ 

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- $T_f$  is the freezout temperature,  $T_f \approx 130 \text{ MeV}$
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•  $S_i(p_T) =$ 

 $\frac{g_i}{2\pi^2} \int dx_{\perp} x_{\perp} \tau_f \left\{ K_1(\frac{m_T u^{\tau}}{T_f}) I_0(\frac{p_T u^{\perp}}{T_f}) - \tau_f' \, p_T K_0(\frac{m_T u^{\tau}}{T_f}) I_1(\frac{p_T u^{\perp}}{T_f}) \right\}$ 

• Gubser's flow is independent of  $\Phi_p$  and Y

# **Fixing parameters**

- Need to fix parameters q and  $\hat{\epsilon}_0$ .
- Some tension between realistic spectrum and hydronization temperature  $T_h \approx 400 - 550 \text{ MeV} \Rightarrow$
- Optimal solution  $q^{-1} = 6.5$  fm and  $\hat{\epsilon}_0 = (8.7)^4$

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- Comparison with ALICE data for pions and protons:



### Effect of induced currents on spectra

- Decompose spectrum in flow parameters:  $S_i = v_0 (1 + v_1(p_T, Y) \cos(\phi_p) + \cdots)$
- Effects of magnetically induced currents most clearly seen in " charge identified directed flow parameter"  $v_1$ :
- Directed flow only from  $\pi^+$  or  $\pi^-$  or p.
- $v_1|_{\text{Gubser}} = 0$  but  $v_1|_{\text{Gubser}+B} \neq 0$ , solely due to B!
- Partial results at RHIC, no charge identified results at LHC yet.

# **Calculation of** $v_1$

- Need to calculate the total current  $V_{Gubser+B}$
- In lab frame:  $u^{\mu}$ , B,  $E_{Faraday}$
- Go to fluid rest frame by  $\Lambda(-\vec{u}) \Rightarrow B'$  and E' include both Faraday and Hall
- Solve for stationary current:  $m\frac{d\langle v_B^{\vec{i}}\rangle}{dt} = q\langle v_B^{\vec{i}}\rangle \times \vec{B'} + q\vec{E'} - \mu m\langle v_B^{\vec{i}}\rangle = 0,$
- Go back to lab frame  $\Lambda(-\vec{u}) \Rightarrow V$  includes both  $\langle v_B \rangle$  and u.
- Calculation is trustable only when  $\langle |\vec{v}_B| \rangle \ll |\vec{u}|$

# **Predictions for charge identified** $v_1$

• Pions and protons at LHC





• Pions and protons at RHIC



#### • Summary - part II:

- Calculated the contribution of the time-varying B in an expanding plasma, using a perturbative approach to magnetohydrodynamics.
- Effect odd under charge and rapidity.
- Competition between Faraday and "Hall" effects.
- However the magnitude is very small.

- Summary part II:
  - Calculated the contribution of the time-varying B in an expanding plasma, using a perturbative approach to magnetohydrodynamics.
  - Effect odd under charge and rapidity.
  - Competition between Faraday and "Hall" effects.
  - However the magnitude is very small.
- Observables and outlook:
  - Define  $A_1^{+-}(Y_1, Y_2) = v_1^+(Y_1) v_1^-(Y_2)$ ,  $A_1^{++}(Y_1, Y_2) = v_1^+(Y_1) - v_1^+(Y_2)$ , etc.

to eliminate charge independent contributions to  $v_1$  produced in event-by-event fluctuations

- Look at quadratic observables C<sub>1</sub><sup>+−,+−</sup>(Y, Y) = ⟨A<sub>1</sub><sup>+−</sup>(Y, Y)A<sub>1</sub><sup>+−</sup>(Y, Y)⟩ = 4⟨v<sub>1</sub><sup>+</sup>(Y)v<sub>1</sub><sup>+</sup>(Y)⟩ to eliminate event-by-event fluctuations in direction of B.
- To be compared with data  $\cdots$

#### THANK YOU !