VKS experiment stationary dynamo

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Dynamo experiments



- Lowes & Wilkinson solid rotors (1963) (ω^2)
- Riga experiment (2000) (Ponomarenko flow)
- Karlsruhe experiment (2000) (Roberts flow)





sodium experiments

- U. Maryland (shear, spherical couette)
- U. Wisconsin (spherical 'VK' flow)
- Grenoble-DTS (spherical Couette)
- Dresden (cylindrical Couette)
- Perm (spin-down torus)





- Inductions ingredients: diff Rot, helicity Moffat, Cambridge UP, (1978)
- Kinematic dynamo simulation Duddley James, Proc. R. Soc. Lond. A425 (1989) Marié et al., *Eur. Phys. J* B33 (2003)
- DNS (P_m=1 down to 0.01) Nore et al., *Phys. Plasmas*, **4**, (1997)

Induction equation

$$\partial_t \vec{B} = \vec{\nabla} \times (\vec{u} \times \vec{B}) + \eta \Delta \vec{B}$$

Fluid equation

$$\partial_t \vec{u} + (\vec{u} \cdot \vec{\nabla})\vec{u} = -\vec{\nabla}\frac{p}{\rho} + \nu\Delta \vec{u} + \frac{(\vec{\nabla} \times \vec{B}) \times \vec{B}}{\mu_0 \rho} + \vec{F}$$

Dimensionless parameters

$$P_m = \frac{\nu}{\eta} = \mu_0 \sigma \nu \sim \mathcal{O}(10^{-6})$$
$$R_m = \frac{\text{induction}}{\text{diffusion}} = \mu_0 \sigma UL \ge \mathcal{O}(1)$$
$$Re = \frac{\text{inertia}}{\text{viscosity}} = \frac{UL}{\nu} \sim \mathcal{O}(10^6)$$

Fluid dynamos : Rm > Rm^c

$$Rm = \frac{induction}{dissipation} = \left(\mu_0 \sigma L U \right)_{engineering} = 10 \times 1$$

Fluid	conductivity	temperature	density
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Iron	1	10 ⁵	x 1,000	12
Mercury	3	104	ambiant	13.6
Gallium	3.7	10 ⁶	> 40°C	6.1
Sodium	1	107	> 100°C	0.93
Silver	6	107	> 950°C	10.5

Fluid dynamos : Power

$$\begin{array}{l} \mathsf{Rm} = \mu_0 \sigma \ \mathsf{L} \ \mathsf{U} = \mu_0 \sigma \nu \ (\mathsf{L} \ \mathsf{U}/\nu) = \Pr \mathbf{x} \ \mathsf{Re} \\ \mathsf{Pm} \approx 10^{-5} \qquad \mathsf{Re} > 10^6 \qquad : \ \mathsf{turbulence} \\ \mathsf{Assuming no global rotation} \quad \mathsf{P} = f(\rho, \nu, \mathsf{L}, \mathsf{U}) \\ \mathsf{P} = [\mathsf{E}_{\mathsf{K}}]/[\mathsf{t}] = (\rho \mathsf{L}^3) . \mathsf{U}^2/(\mathsf{L}/\mathsf{U}) \ \mathsf{g}(\mathsf{Re}) \\ \mathsf{Fully developped turbulence} \ : \ \mathsf{g}(\mathsf{Re}) \rightarrow \mathsf{Const.} \\ \mathsf{P} \approx \rho \mathsf{L}^2 \mathsf{U}^3 \end{array}$$

Fluid dynamos : Power





VKS2





stationary dynamo $F_1 = F_2$



Monchaux et al., PRL, 98 (2007)





















a turbulent dynamo

(m=0) / dipole dynamo

not generated by the mean flow (Cowling theorem)

New, compared to Riga & Karlsruhe exp.

kinematic modes for s2t2



Ravelet et al., *Phys. Fludis* **17**, 117104 (2005) M. Bourgoin et al., *Phys. Fluids* **16** (2004)

Transverse intermittent dipole Phys. Rev. Lett. 97, 044503 (2006).











Scaling at saturation



Comparison with Riga / Karlsruhe

Lundquist number:
$$\langle B^2 \rangle \mu_0(\sigma R)^2 / \rho \propto (R_m - R_m c)^{\alpha}$$



power

Turbulent scaling $P \approx \rho R^5 \Omega^3 \qquad \qquad \text{Kp} = P \ / \ \rho R^5 \Omega^3$

Dynamo

$$P = P(mag) + P(hydro)$$

$$Rm < Rm^c$$
 : $P = P(v_1)$

 $Rm > Rm^{c}$: $P = P(v_2) + P(B)$

with
$$\langle v_2 \rangle \neq \langle v_1 \rangle$$
?
and $v_2' \neq v_1'$?

power, from motor drives

 $Kp = P \,/\, (\rho \, R^5 \, (2\pi F)^3)$



Comparison Karlsruhe & Riga



Stieglitz & Müller, *PoF*, **13** (2001) Müller, Stieglitz, Horanyi, *JFM*, **498** (2004)



Gailitis et al. Phys. Plasmas 11 (2004)





a susceptibility ?



Local fluctuations



Local fluctuations



PSD scaling

PSD of local magnetic fluctuations

- K41 scaling, strong Joule dissipation, passive vector : $E_M(k) \approx k^{-5/3}$
- Equipartition, Alfven waves Iroshnikov-Krainchan : $E_M(k) \approx k^{-3/2}$
- Strong correlation V-B, scale separation, Pouquet et al. : $E_M(k) \approx k^{-3}$
- Significant Joule diss., low Pm, Moffat : $E_M(k) \approx k^{-2} E_V(k)$ if K41 velocity : $E_M(k) \approx k^{-11/3}$ if IK field : $E_M(k) \approx k^{-5}$

Local fluctuations



Comparison Karlsruhe & Riga



Stieglitz & Müller, *PoF*, **13** (2001) Müller, Stieglitz, Horanyi, *JFM*, **498** (2004) Gailitis et al. Phys. Plasmas 11 (2004)

