

# *Bifurcations and multistability in turbulence*



VKS team



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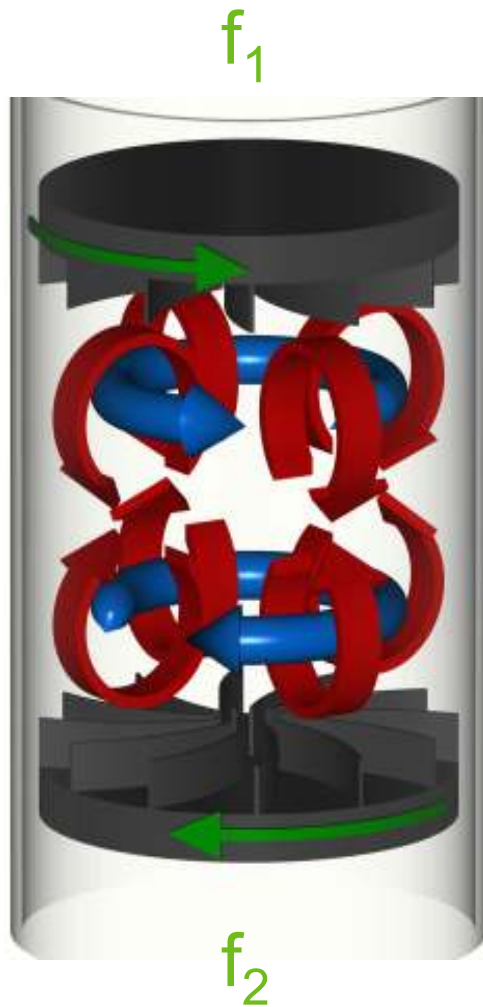
O. Dauchot  
A. Prigent

# *Bifurcations and multistability in turbulence*

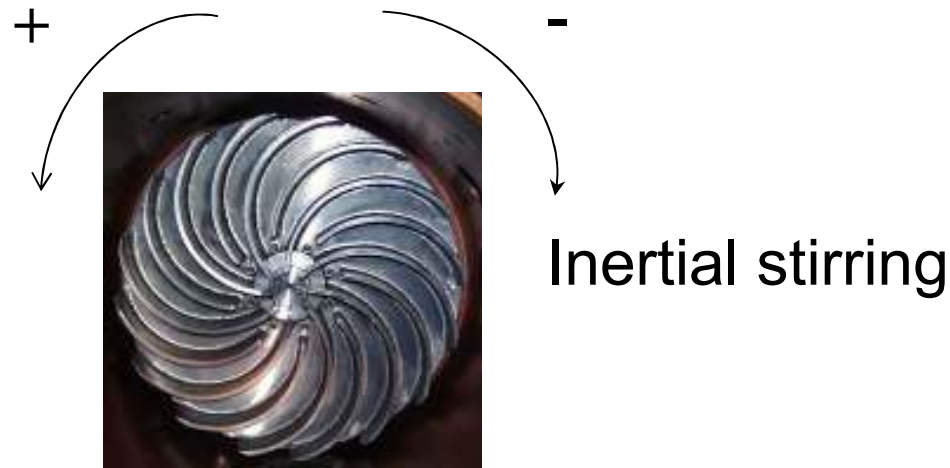
Bifurcations in turbulent flows:

1. von Karman : bifurcation between mean flows
2. Couette flows: turbulent spiral and stripes
3. VKS: - dynamo action  
- multistability

# Turbulent von Karman flow



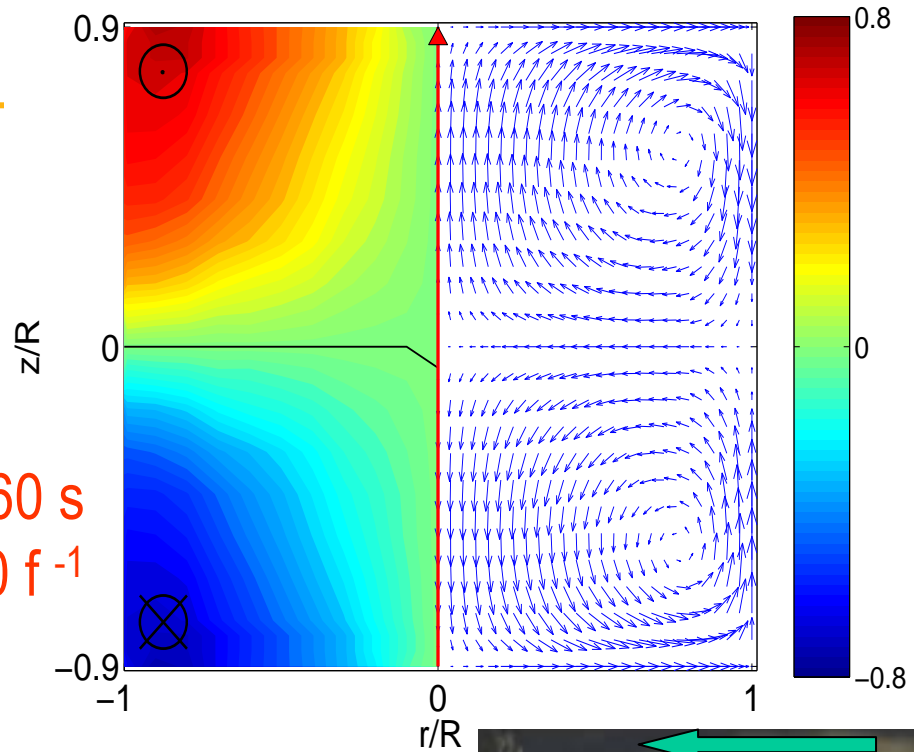
- Axisymmetry
- $R\pi$  symmetry / radial axis
- $R_c = 100$  mm
- $H = 180$  mm
- $f = 2-20$  Hz
- $Re = 2\pi R_c f^2 / \nu = 10^2 - 10^6$
- fluid: water and glycerol-water



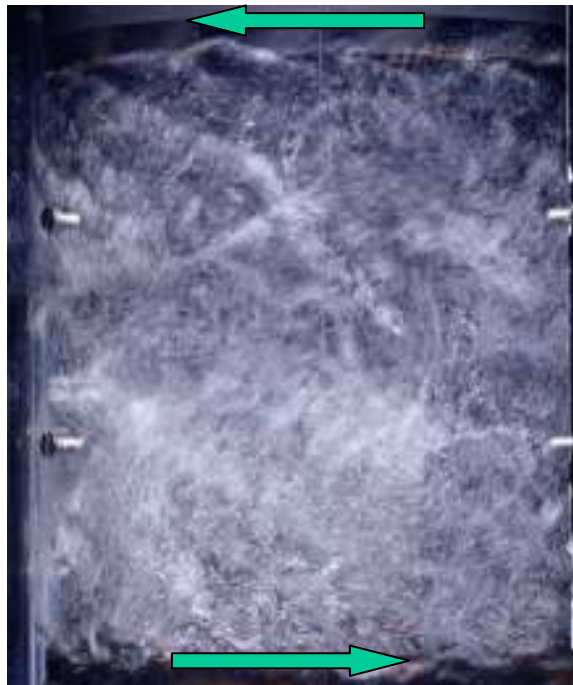
cea

3 « scales »

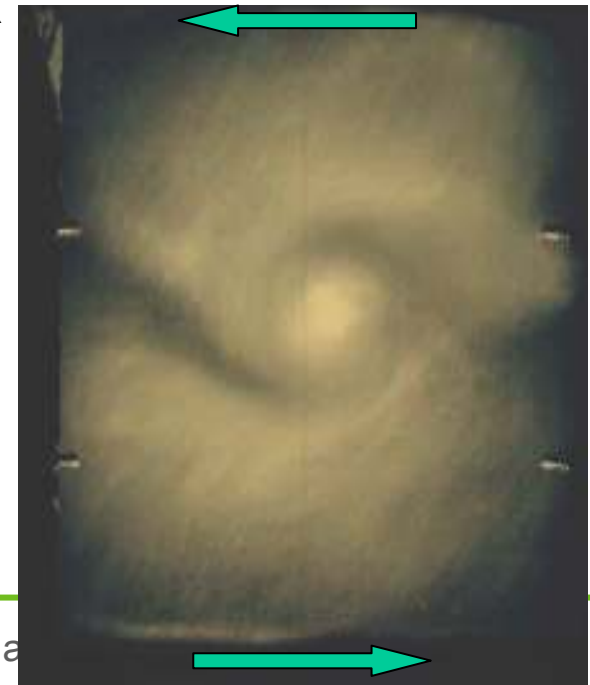
$$Re \simeq 10^6$$



Mean on 60 s  
 $500 f^{-1}$



Mean on 1/20 s  
 $1/2 f^{-1}$

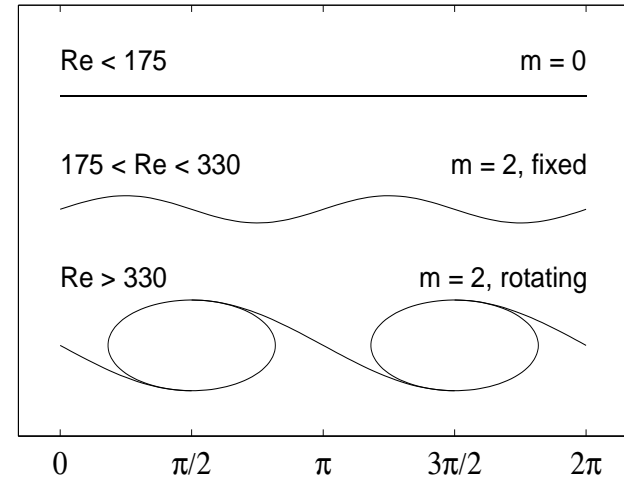
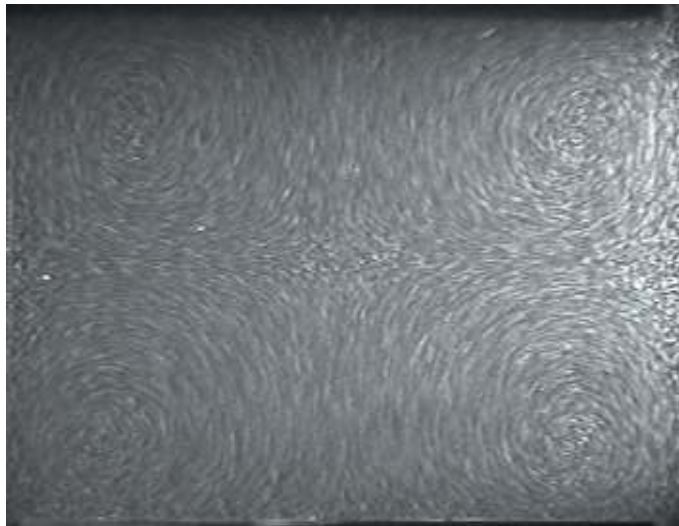


Mean on : 1/500 s  
 $1/50 f^{-1}$



# First bifurcations and symmetry breaking

meridian  
plane: poloidal  
recirculation



***Re = 90***

*Stationary axisymmetric*

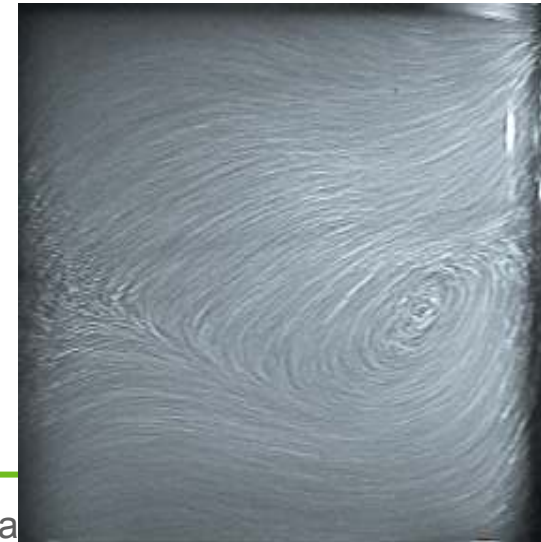
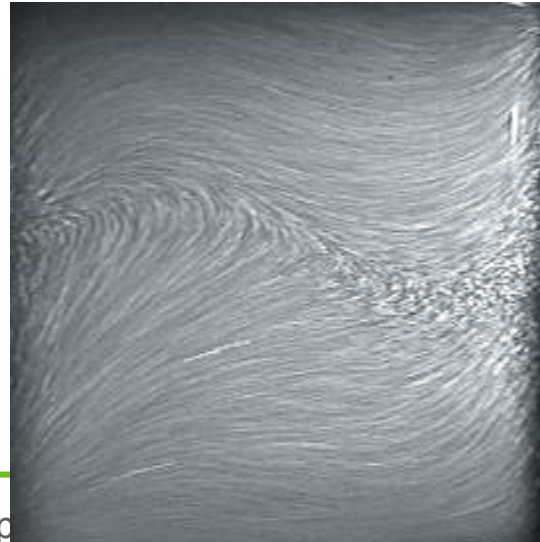
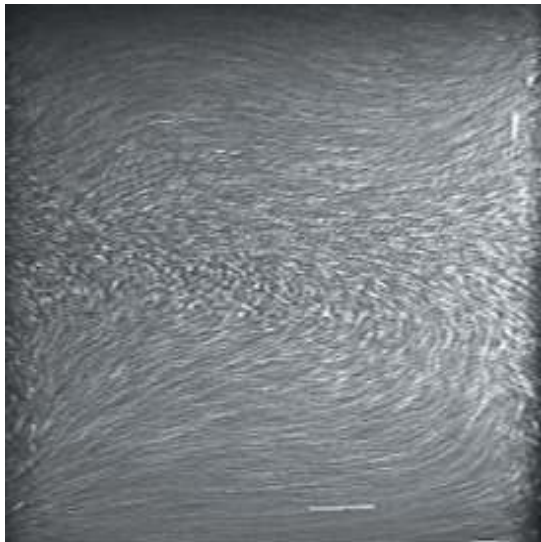
***Re = 185***

*m = 2 ; stationary*

***Re = 400***

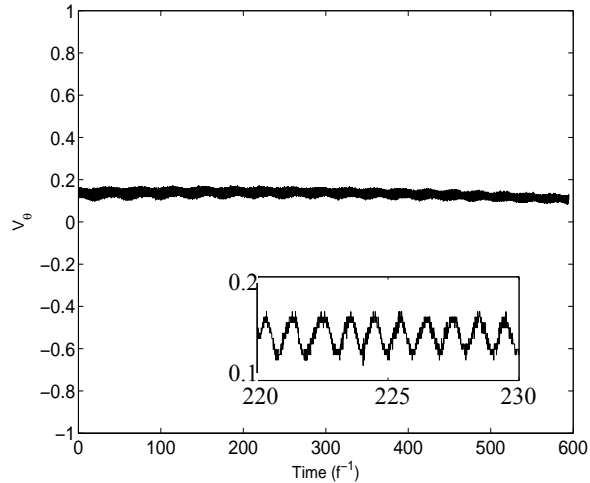
*m = 2 ; periodic*

Tangent  
plane :  
shear  
layer

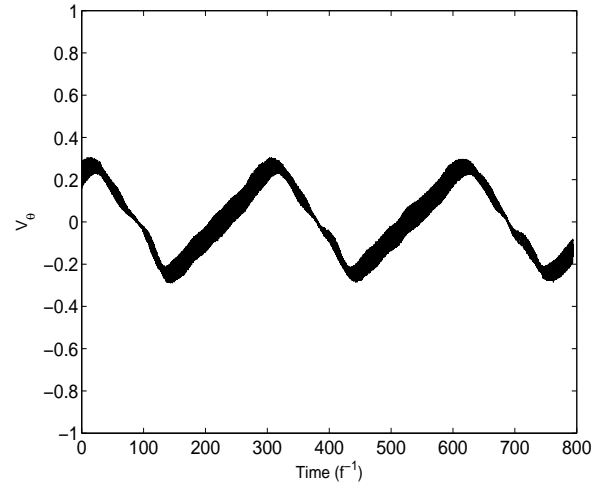


# Time spectra as a function of $Re$

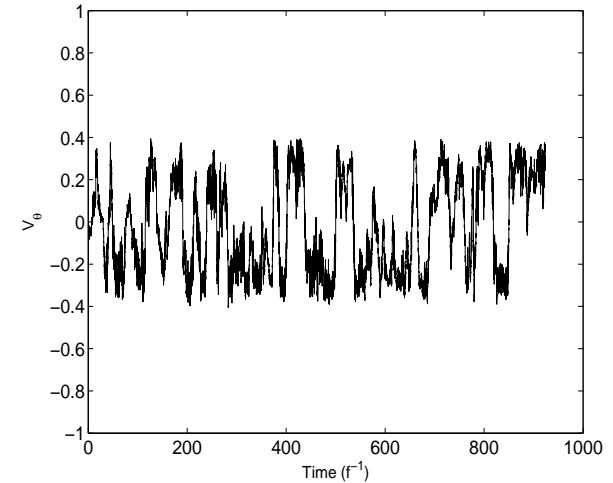
$v_\theta$  en  $\{r = 0.9; z = 0\}$



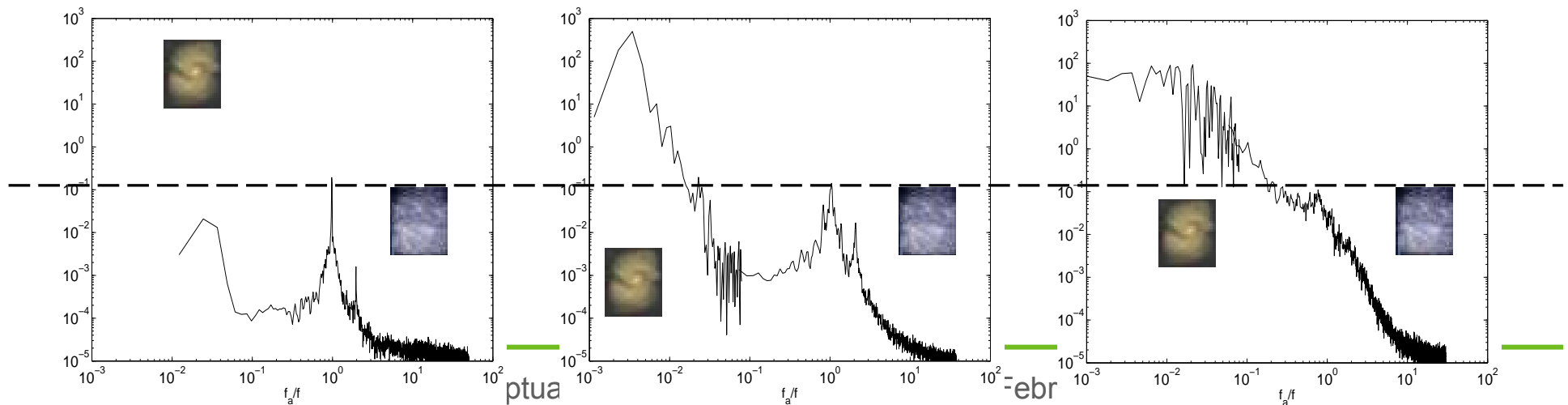
**$Re = 330$**   
Periodic



**$Re = 380$**   
Quasi-Periodic

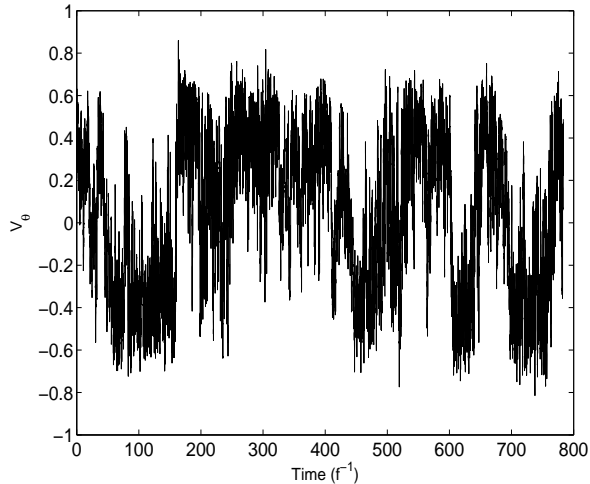


**$Re = 440$**   
Chaotic

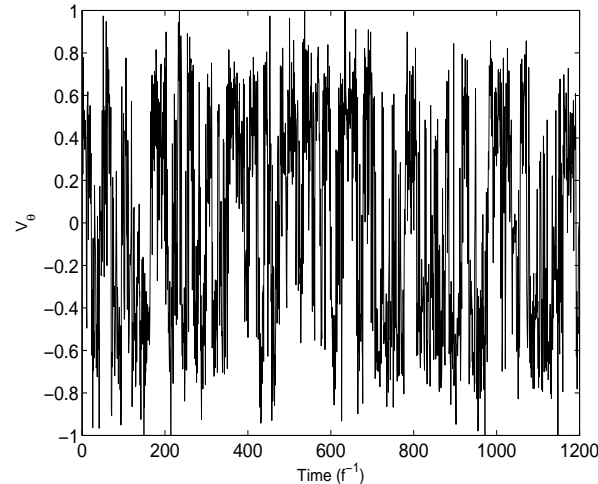


# Time spectra as a function of Re

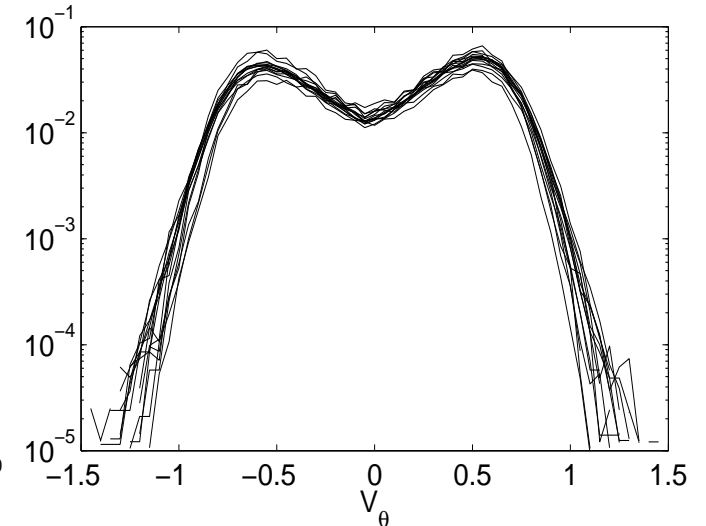
$v_\theta$  en  $\{r = 0.9; z = 0\}$



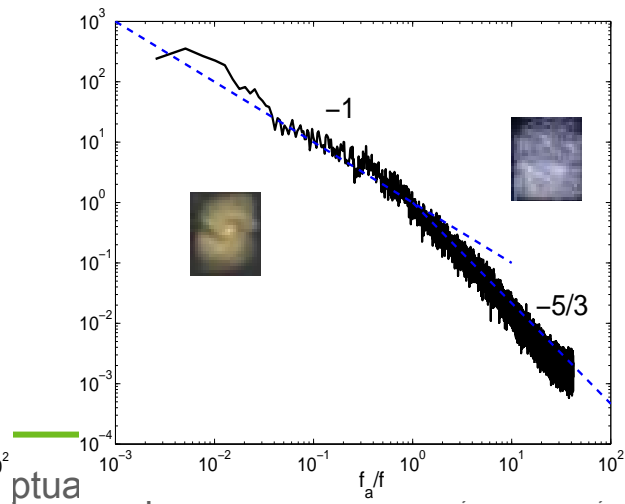
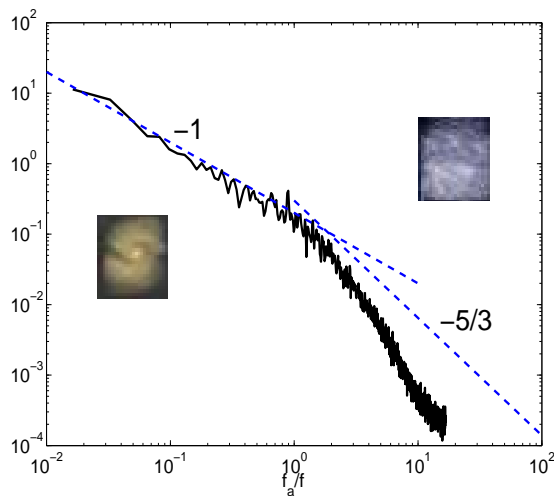
**$Re = 1000$**   
Chaotic



**$Re = 4000$**   
Turbulent

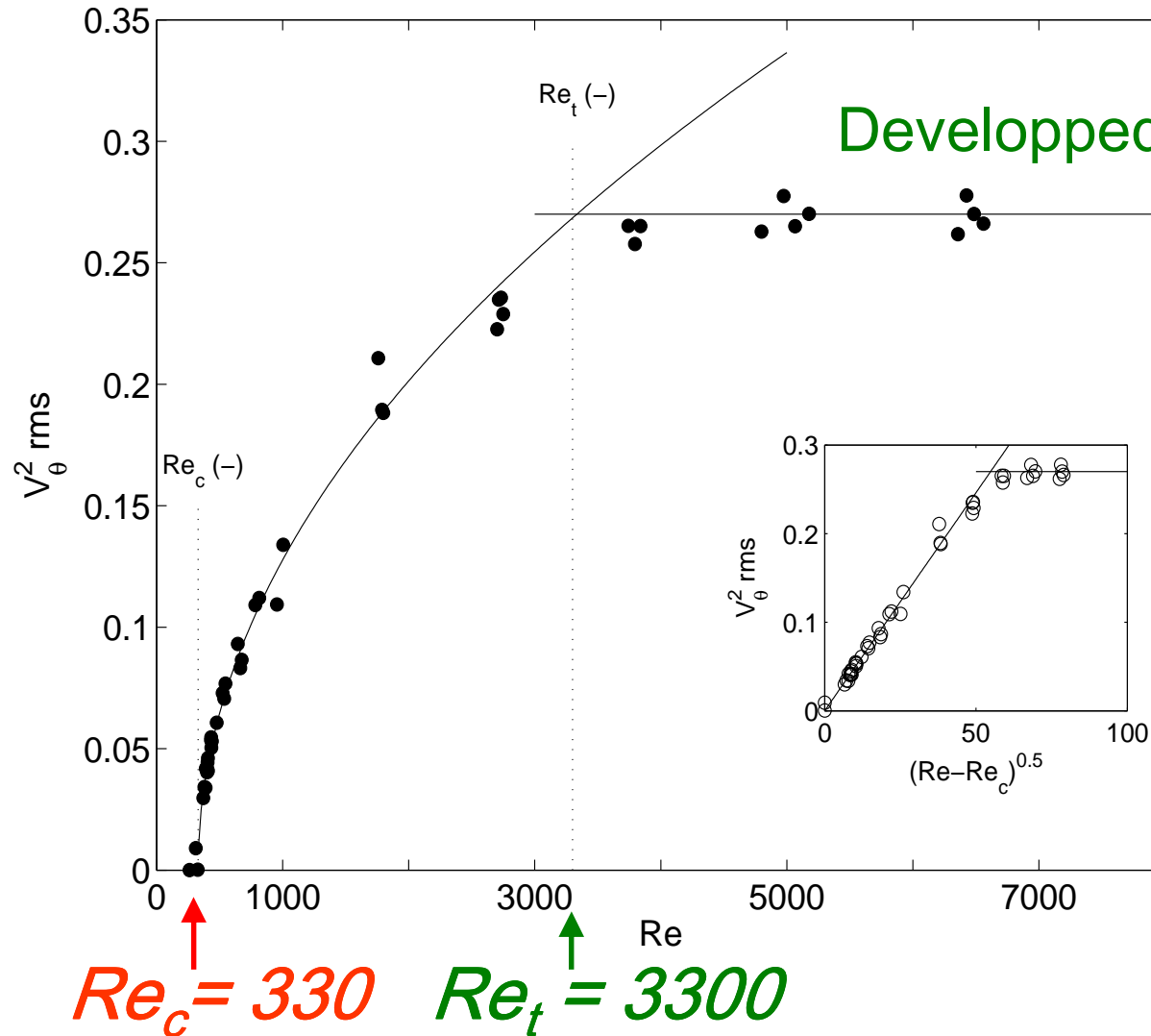


**$2000 < Re < 6500$**



**Bimodal distribution :**  
signature of the  
turbulent shear

# Transition to turbulence: fluctuations kinetic energy



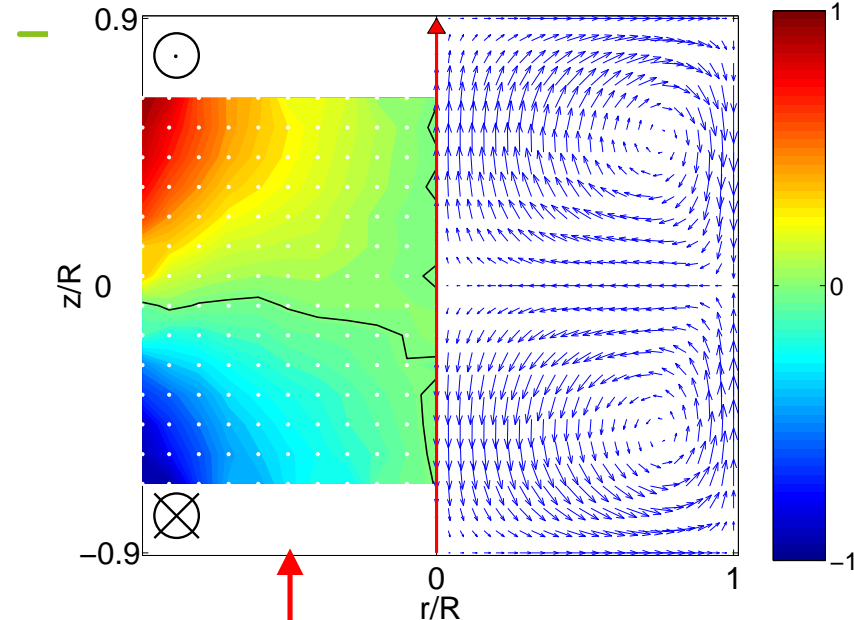
Globally supercritical transition via a Kelvin-Helmoltz type instability of the shear layer and secondary bifurcations

*Ravelet et al. JFM 2008*





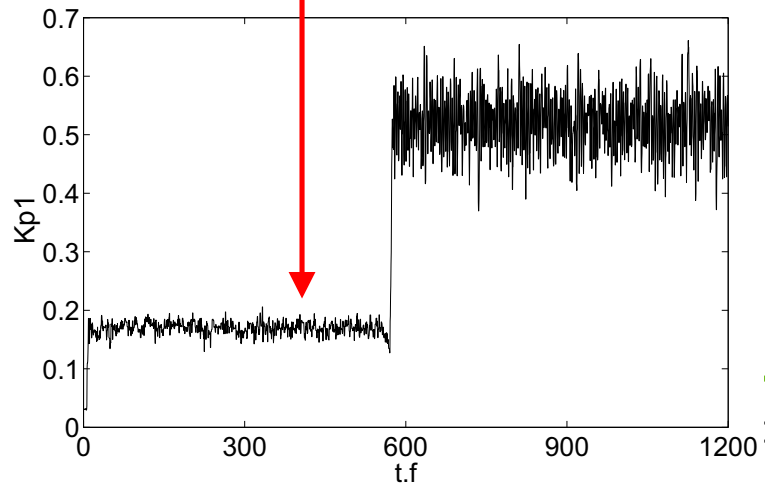
# Turbulent Bifurcation of the mean flow



Symmetry broken:  
2 different mean flows  
exchange stability.

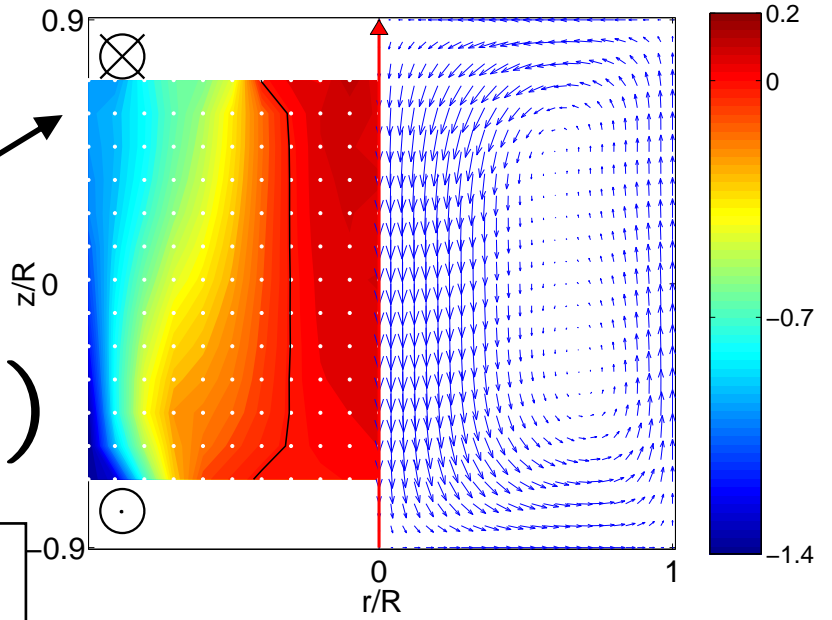
Bifurcated flow (b) : no more shear  
layer broken symmetry

two cells  
one state  
(s)



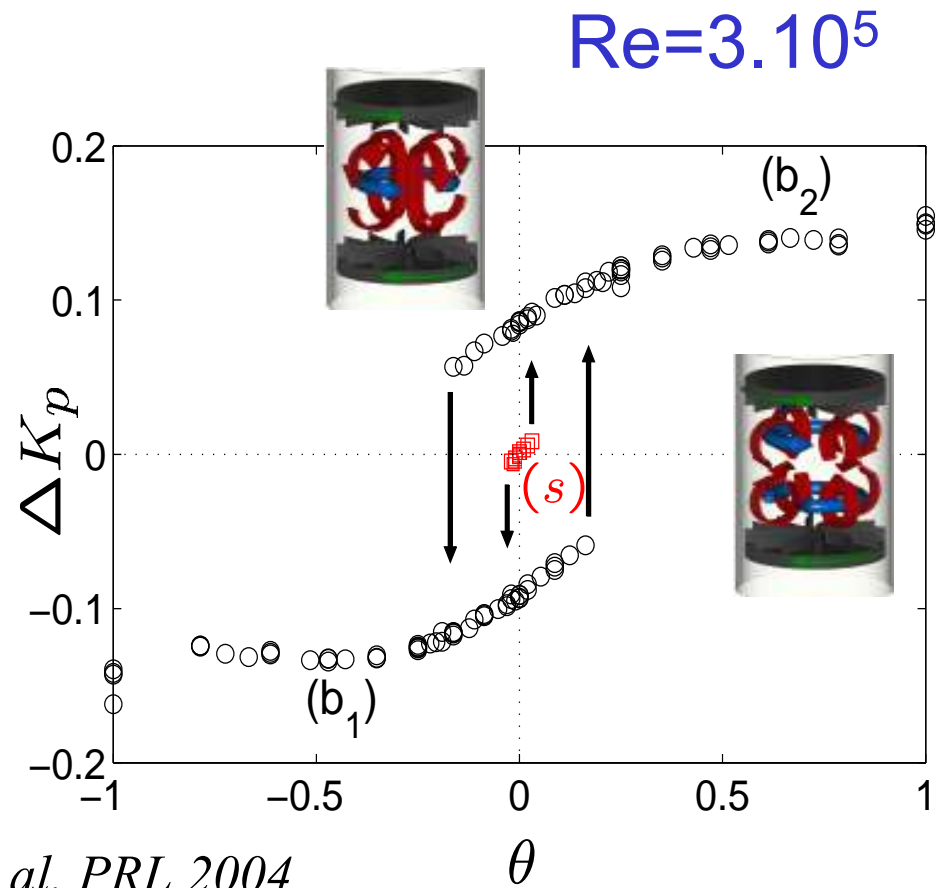
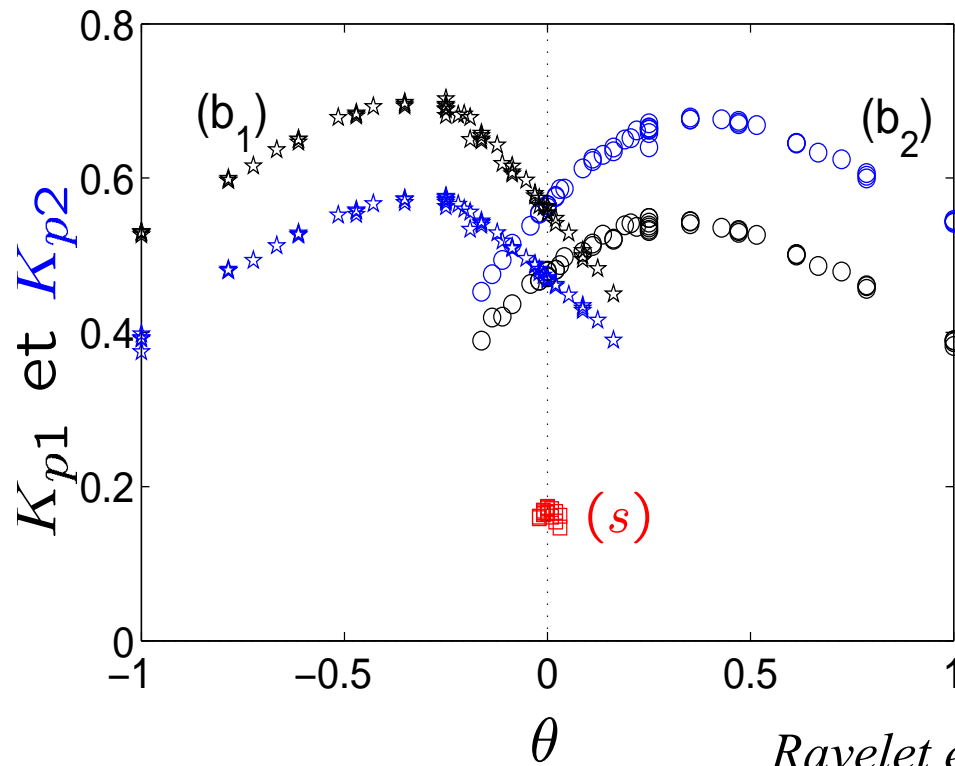
(b<sub>2</sub>)

one cell  
two states



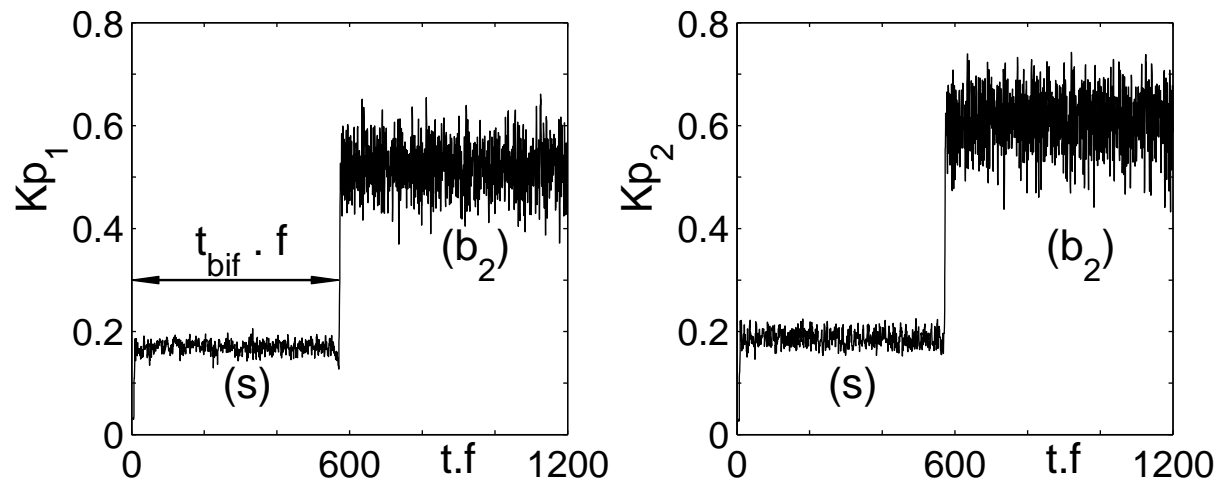
# Turbulent Bifurcation: memory effect?

- $K_p = \text{Torque} / \rho R_c^5 (2\pi f)^2$
- $\theta = (f_2 - f_1) / (f_2 + f_1)$
- $Re = (f_1 + f_2)^{1/2}$

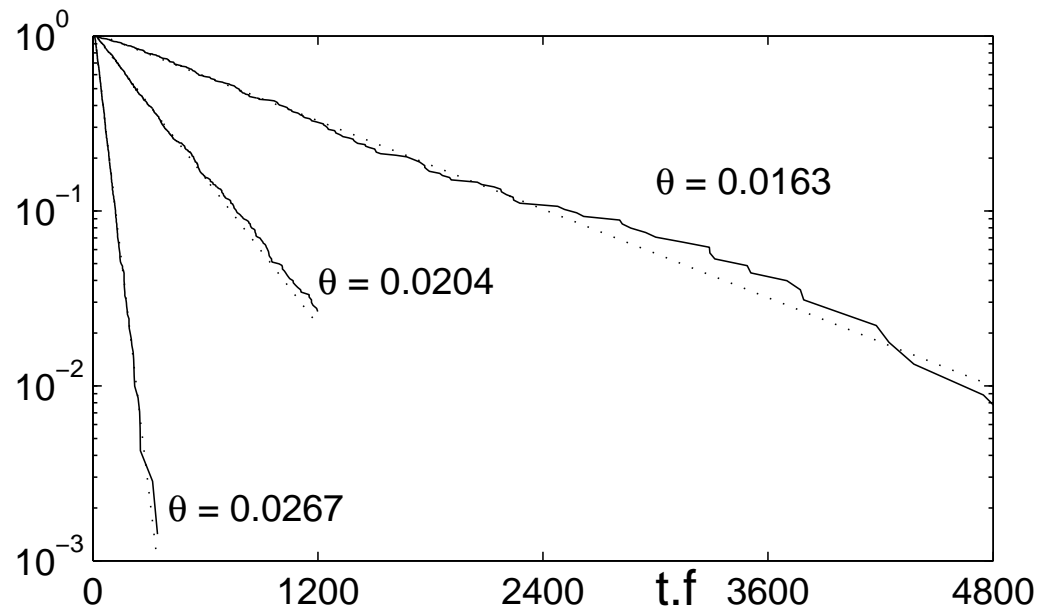


*Ravelet et al. PRL 2004*

# Stability of the symmetric state



Statistics on  
500 runs for  
different  $\theta$

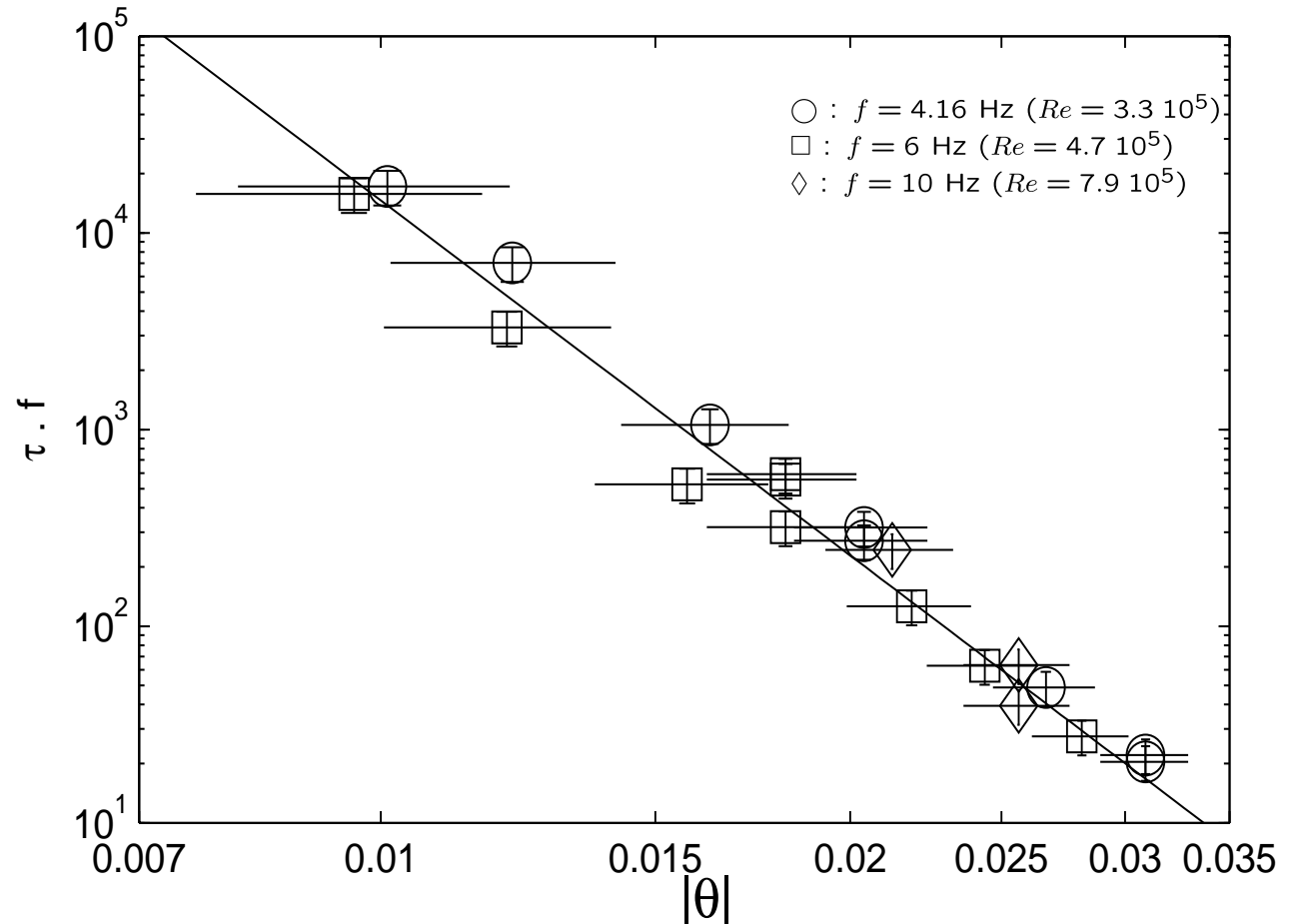


Cumulative distribution  
functions of bifurcation  
time  $t_{bif}$ :

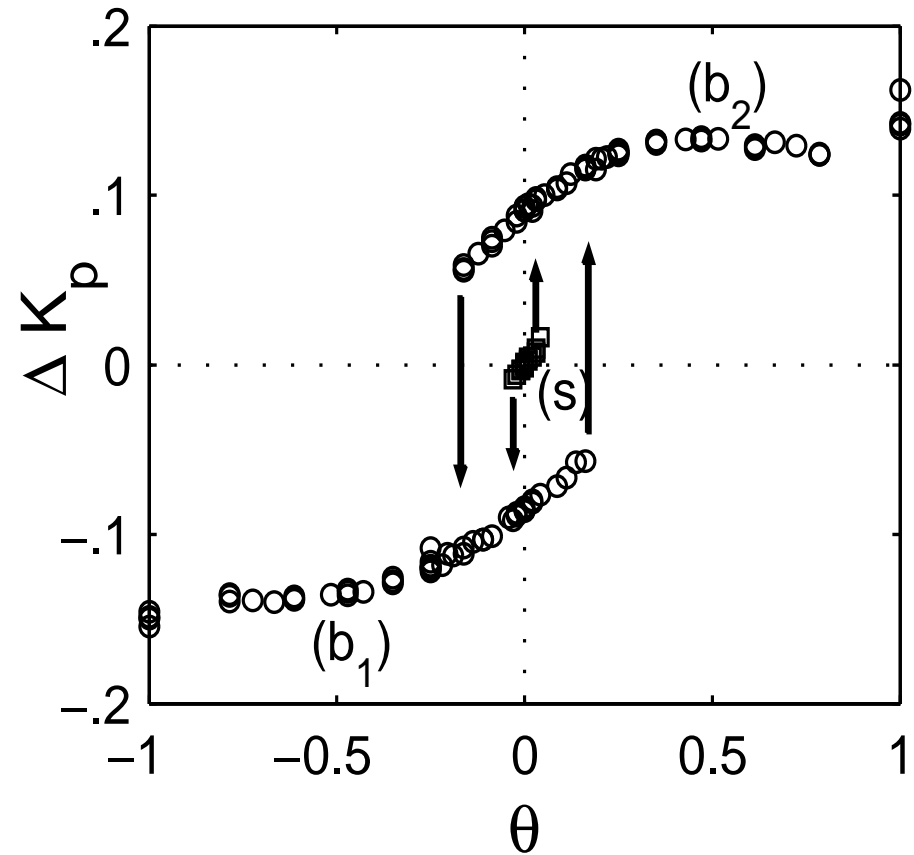
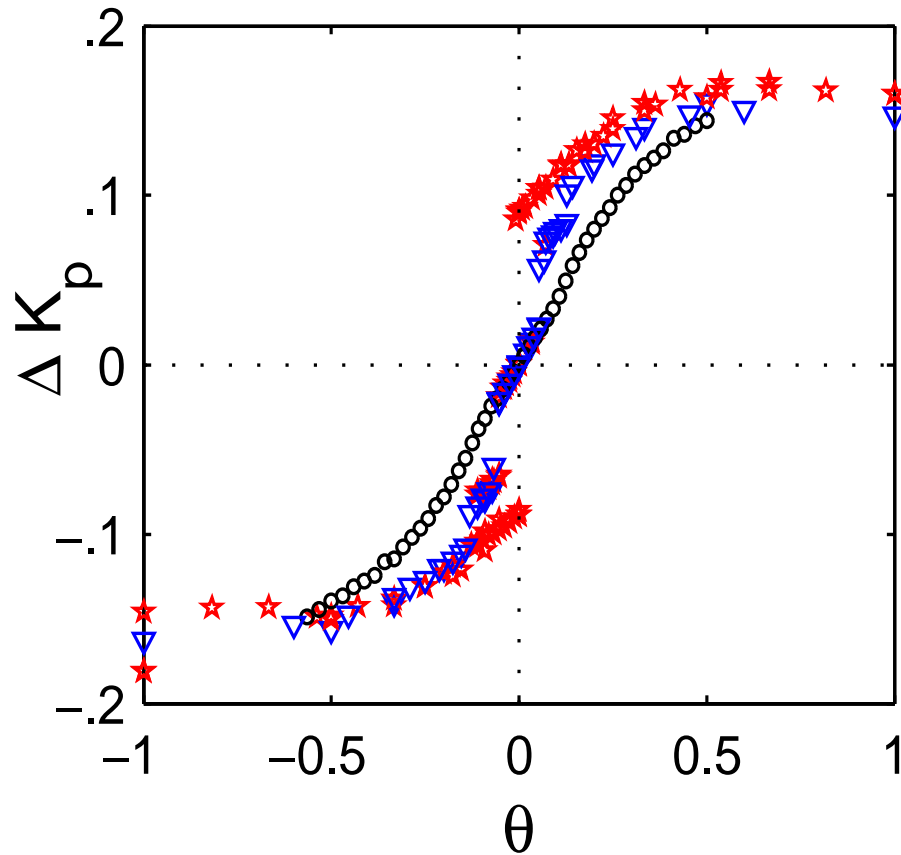
$$P(t_{bif} > t) = A \exp(-(t - t_0)/\tau)$$

- $t_0 f \sim 5$
- $\tau$ : characteristic bif. time

- fit: power law  
exponent = -6
- symmetric state  
marginally stable  
 $\tau \rightarrow \infty$  when  $\theta \rightarrow 0$



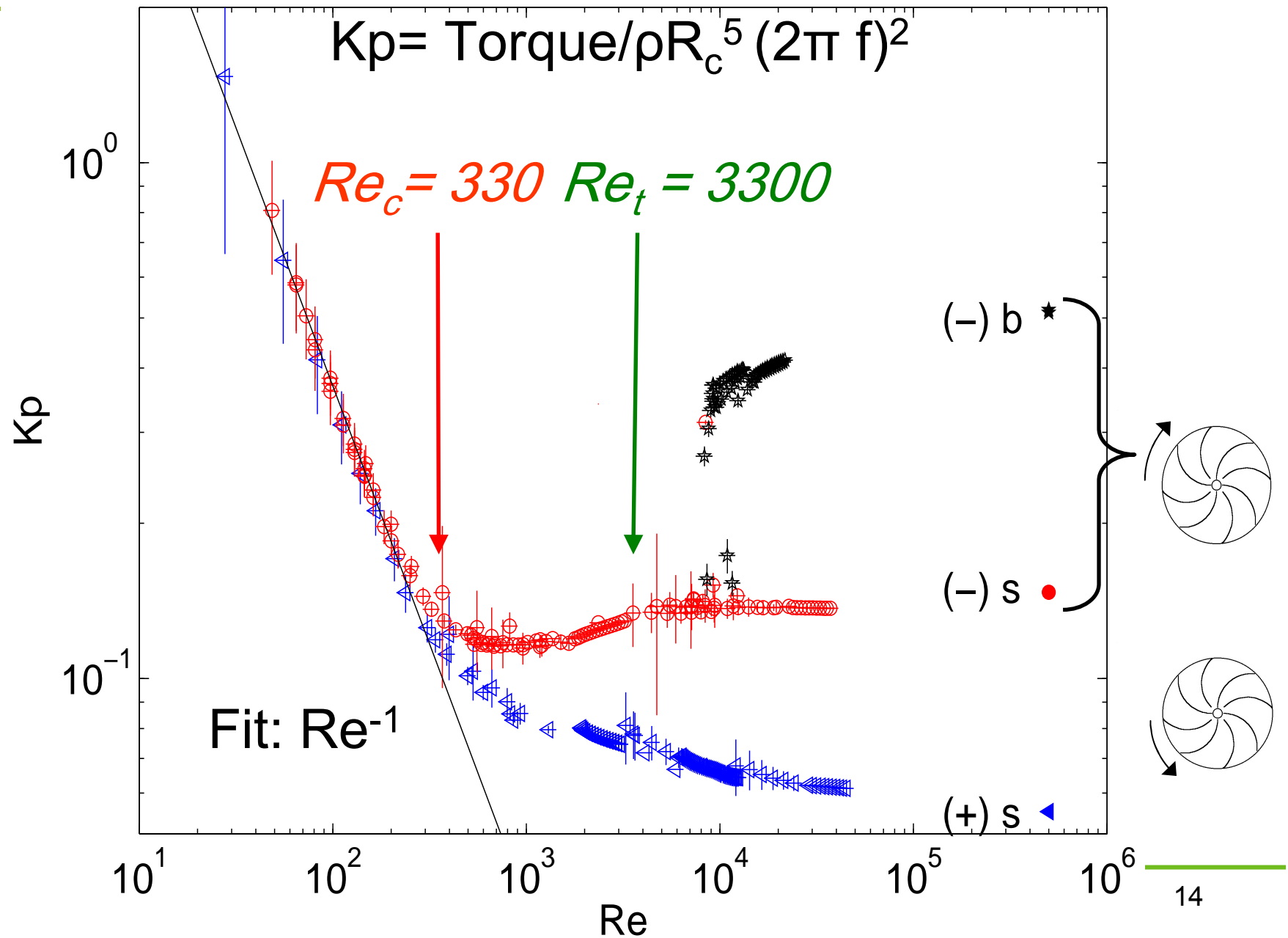
# Mutistability = f(Re)



- :  $Re = 800$
- ▽ :  $Re = 5\,000$
- ★ :  $Re = 10\,000$

$$Re = 3 \times 10^5$$

# Multiplicity of solutions

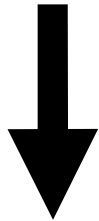




# Torque regulation: stochastic transitions

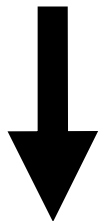
## 1 cell state $\rightarrow$ 2 cells states

$Kp_1 \neq Kp_2 \Rightarrow$  1 cell



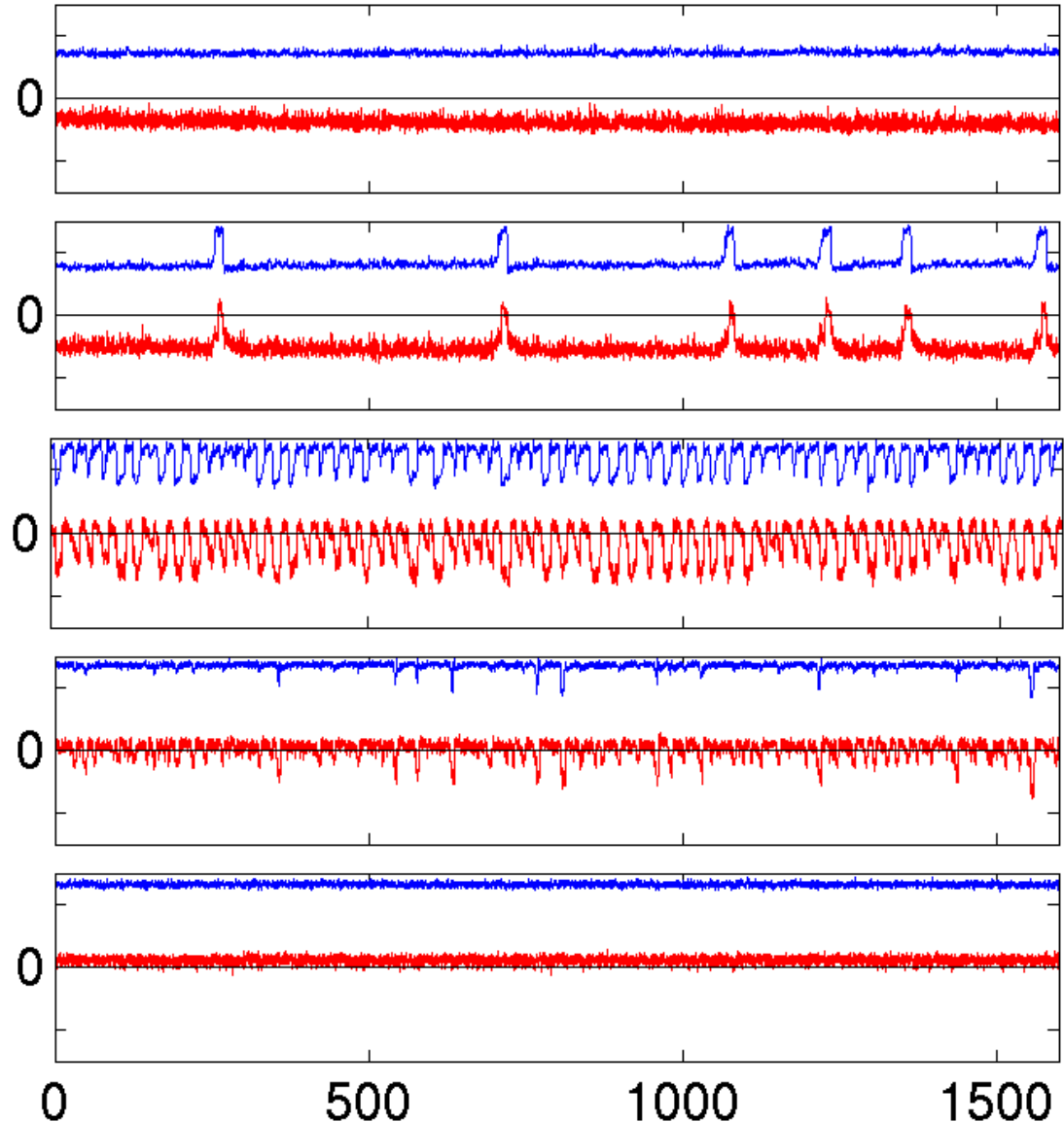
$Kp_1 \sim Kp_2$ ,  
"oscillation"

between 2 states

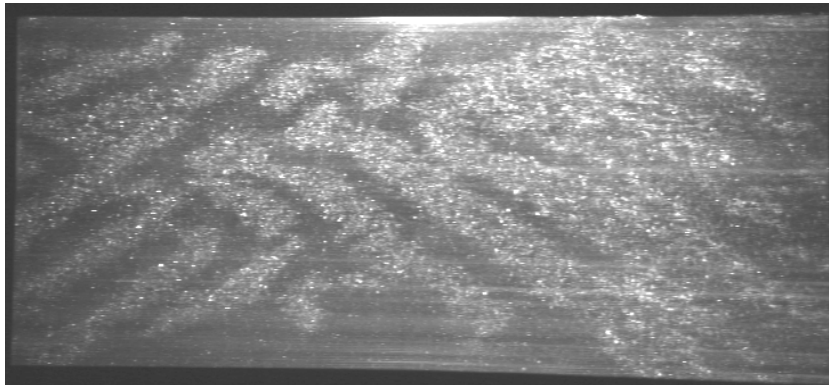
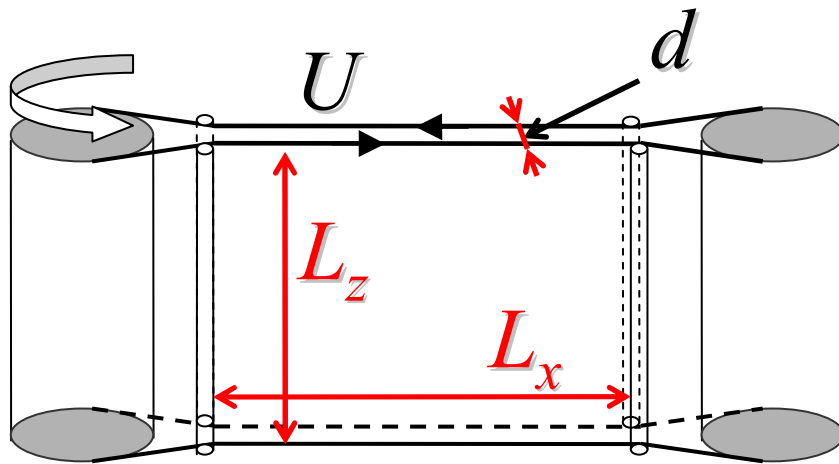


$Kp_1 \approx Kp_2 \Rightarrow$  2 cells

Concep

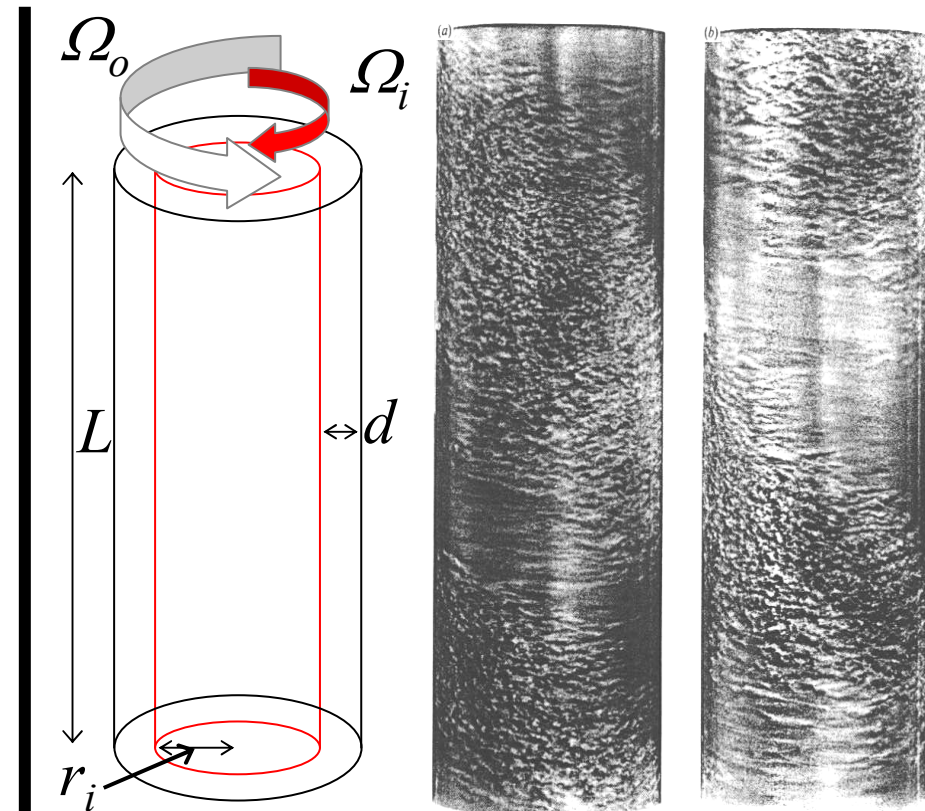


# Couette flows



$$\Gamma_x = L_x / d$$

$$\Gamma_z = L_z / d$$



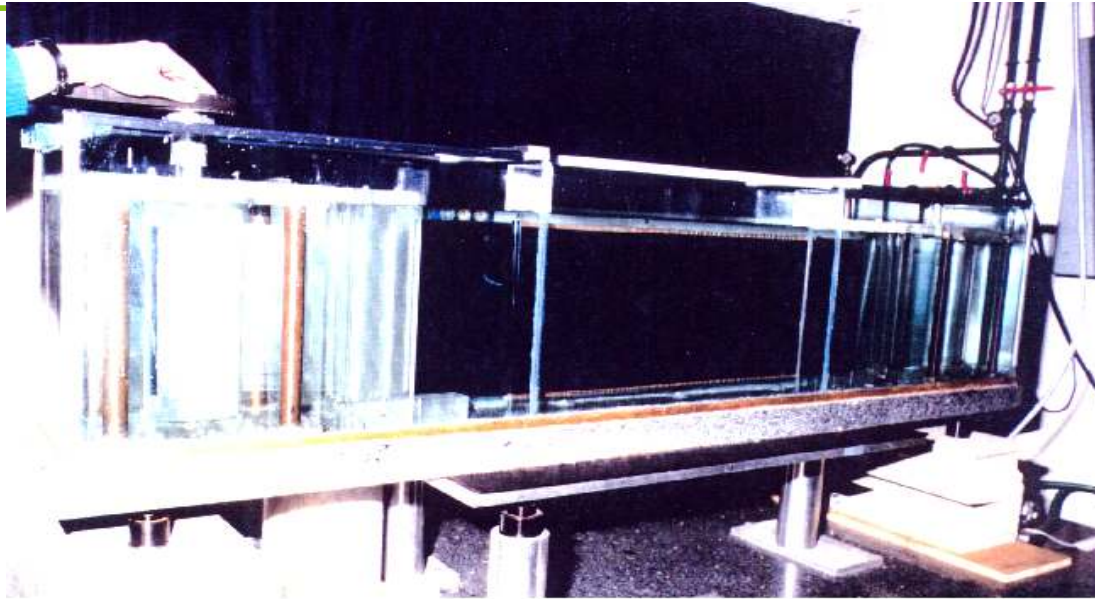
$$\eta = r_i / r_o$$

$$\Gamma_\theta = \pi (r_i + r_o) / d$$

$$\Gamma_z = L / d$$



# Plane Couette flow setup



$$d = 2h = 7, 3.5, 1.5 \text{ mm}$$

$$L_x = 578 \text{ mm}$$

$$L_z = 255 \text{ mm}$$

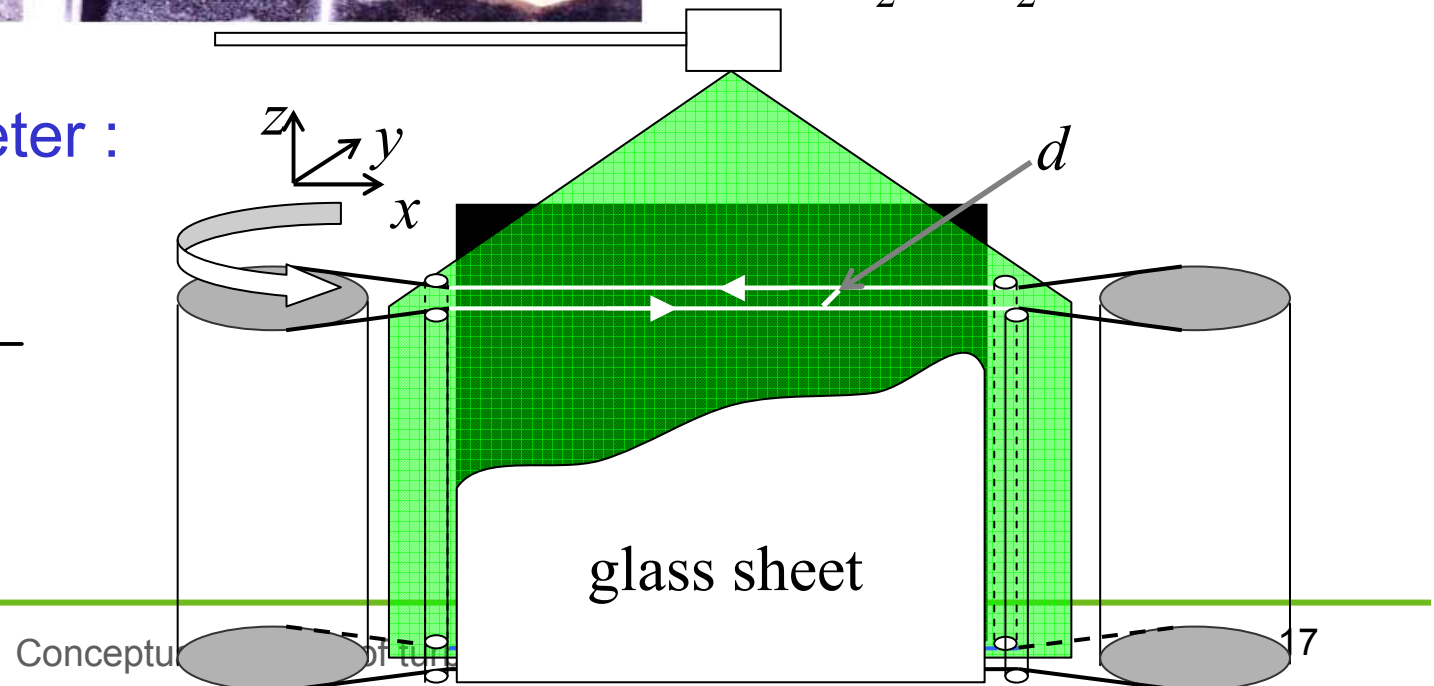
$$\Gamma_x = L_x / d = 385$$

$$\Gamma_z = L_z / d = 170$$

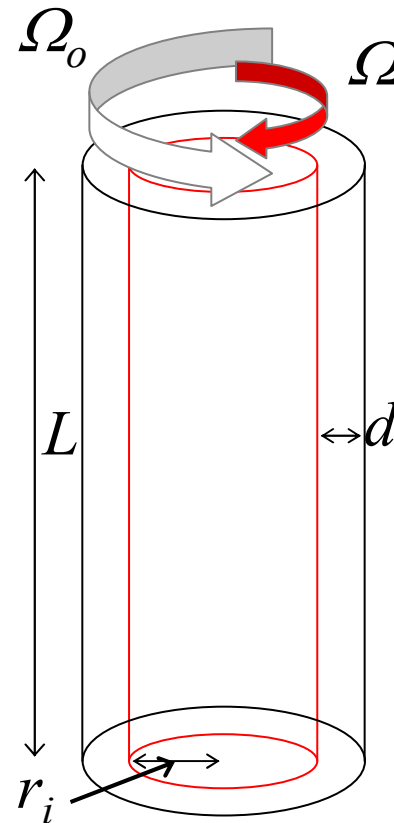
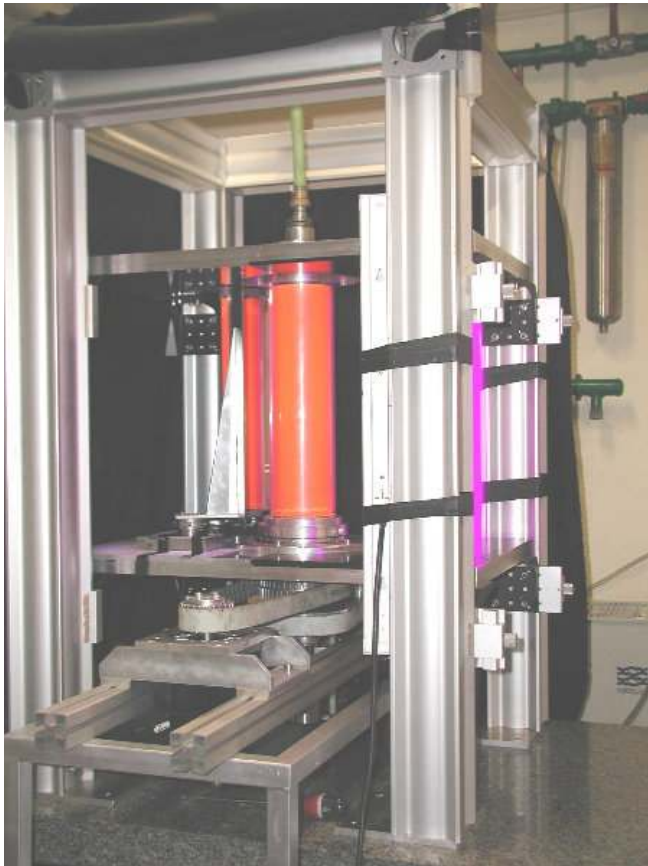
1 control parameter :

$$R_{Cp} = \frac{Uh}{\nu}$$

*Daviaud PRL 92*



# Cylindrical Couette setup



$$\eta = r_i / r_o$$

$$\Gamma_\theta = \pi (r_i + r_o) / d$$

$$\Gamma_z = L / d$$

2 control parameters :

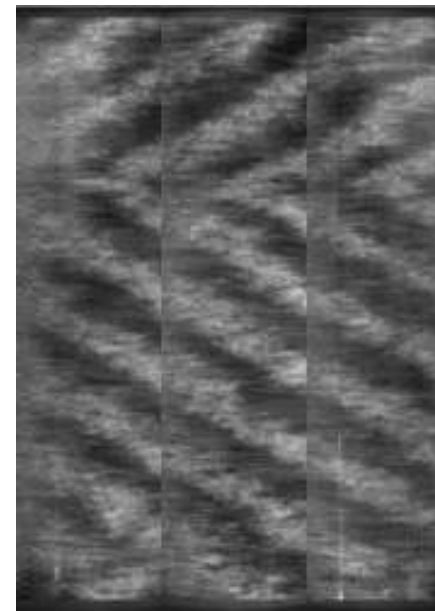
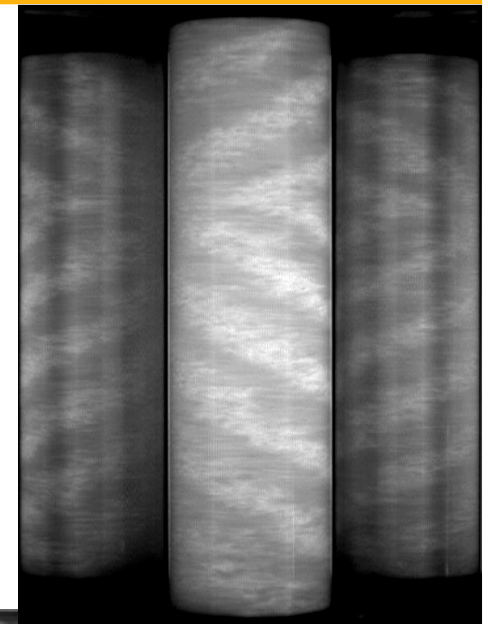
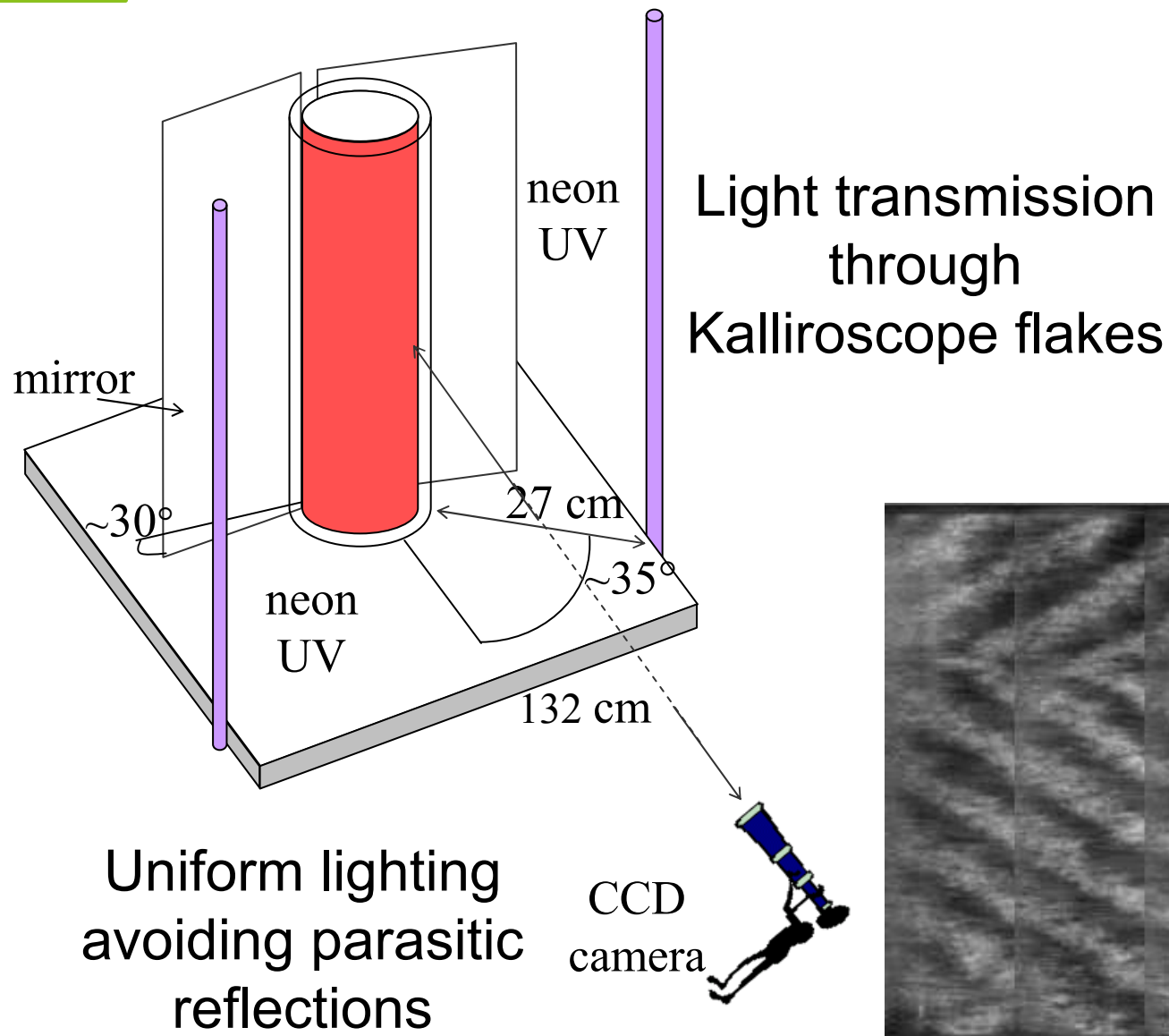
$$R_i = \frac{\Omega_i r_i d}{\nu} \quad \text{and} \quad R_o = \frac{\Omega_o r_o d}{\nu}$$

Physical control parameter :

$$R_{TC} = \frac{|\eta R_o - R_i|}{2(1 + \eta)}$$

Setup	$r_i$ (mm)	$d$ (mm)	$\eta$	$\Gamma_z$	$\Gamma_\theta$
TC $_{\eta 1}$	49.09	0.87	0.983	431	358
TC $_{\eta 2}$	48.11	1.85	0.963	203	167

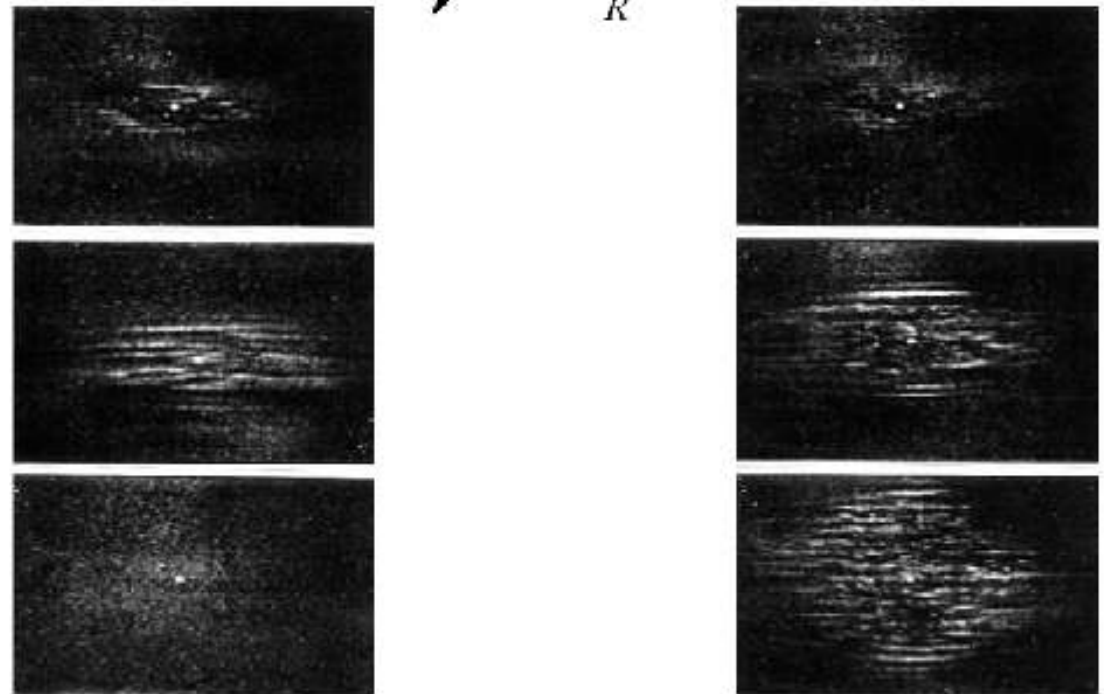
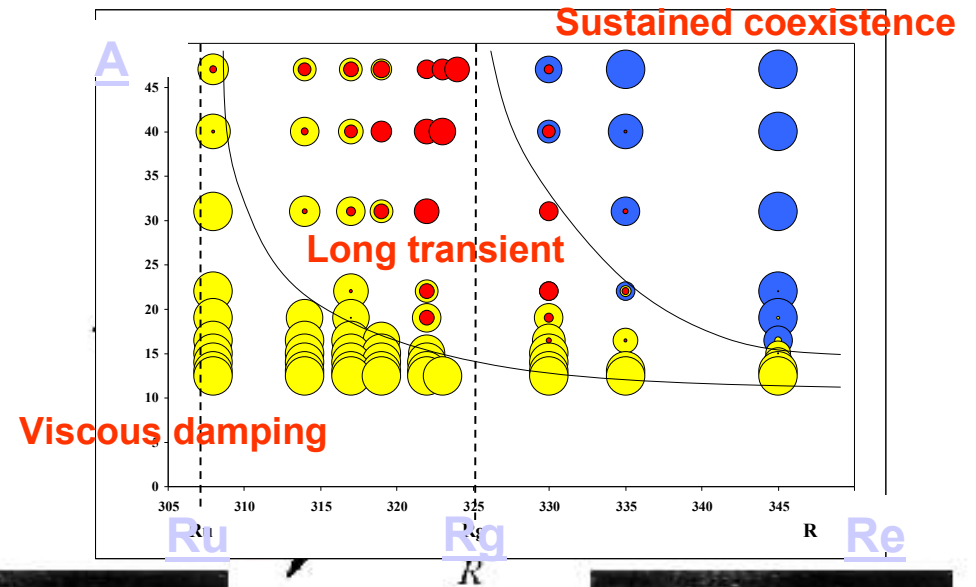
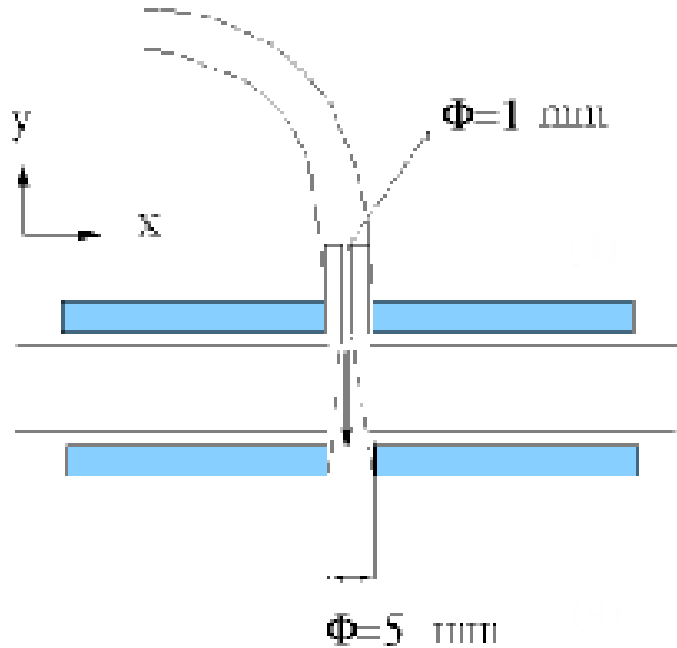
# cea Taylor-Couette flow visualization



*Prigent et al.  
PRL 2002*

# cea Transition from laminar *to* turbulent flow

Response to localized & instantaneous finite amplitude perturbation

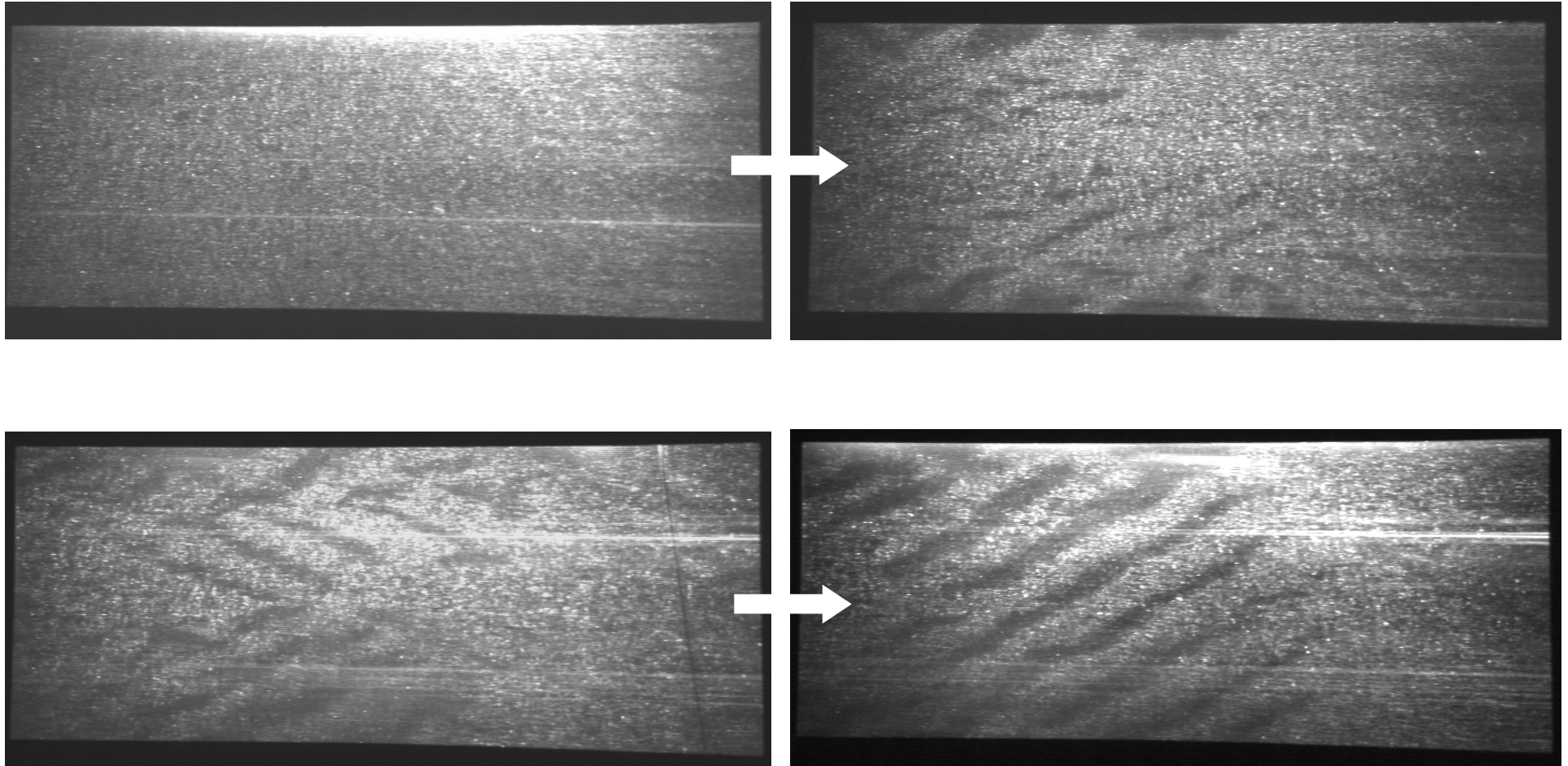


*Dauchot Daviaud POF 95*

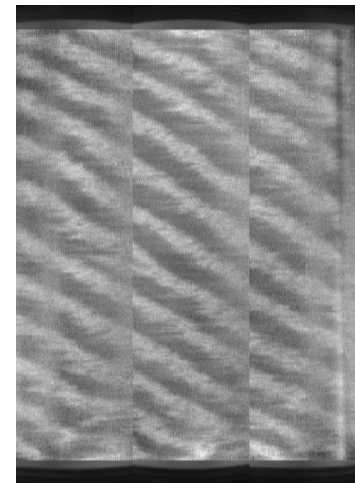
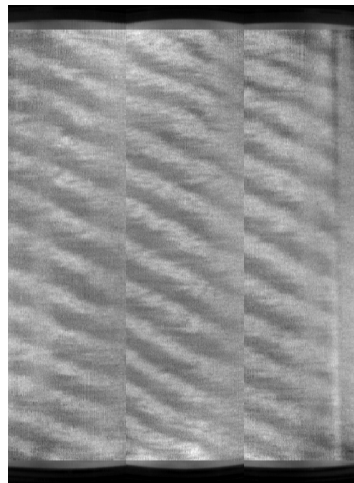
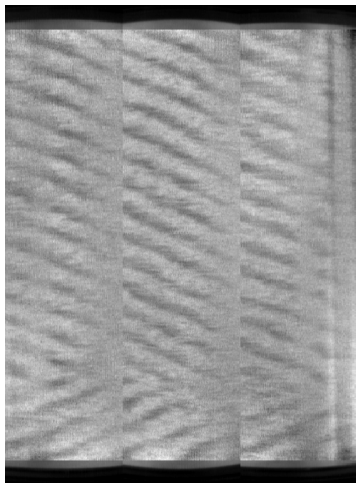
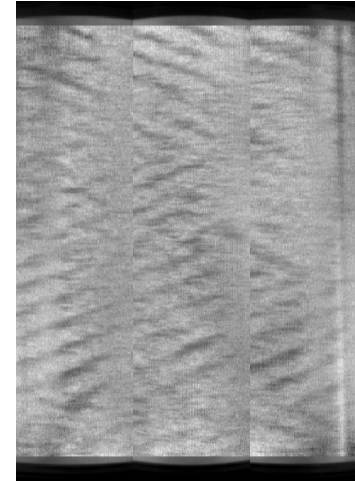
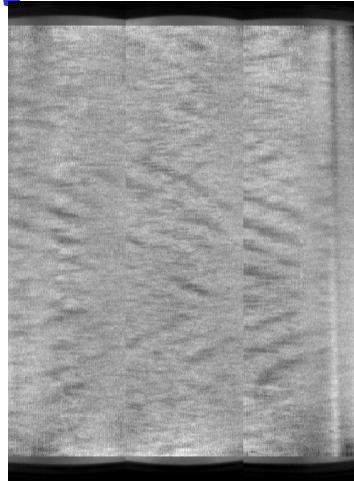
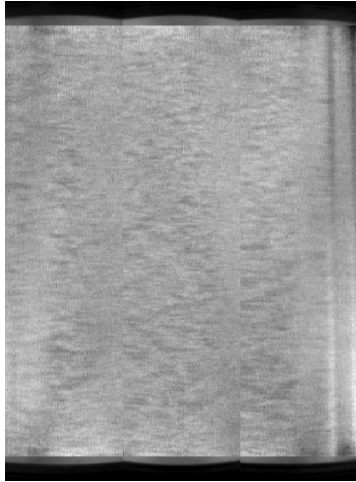
Conceptual Aspe



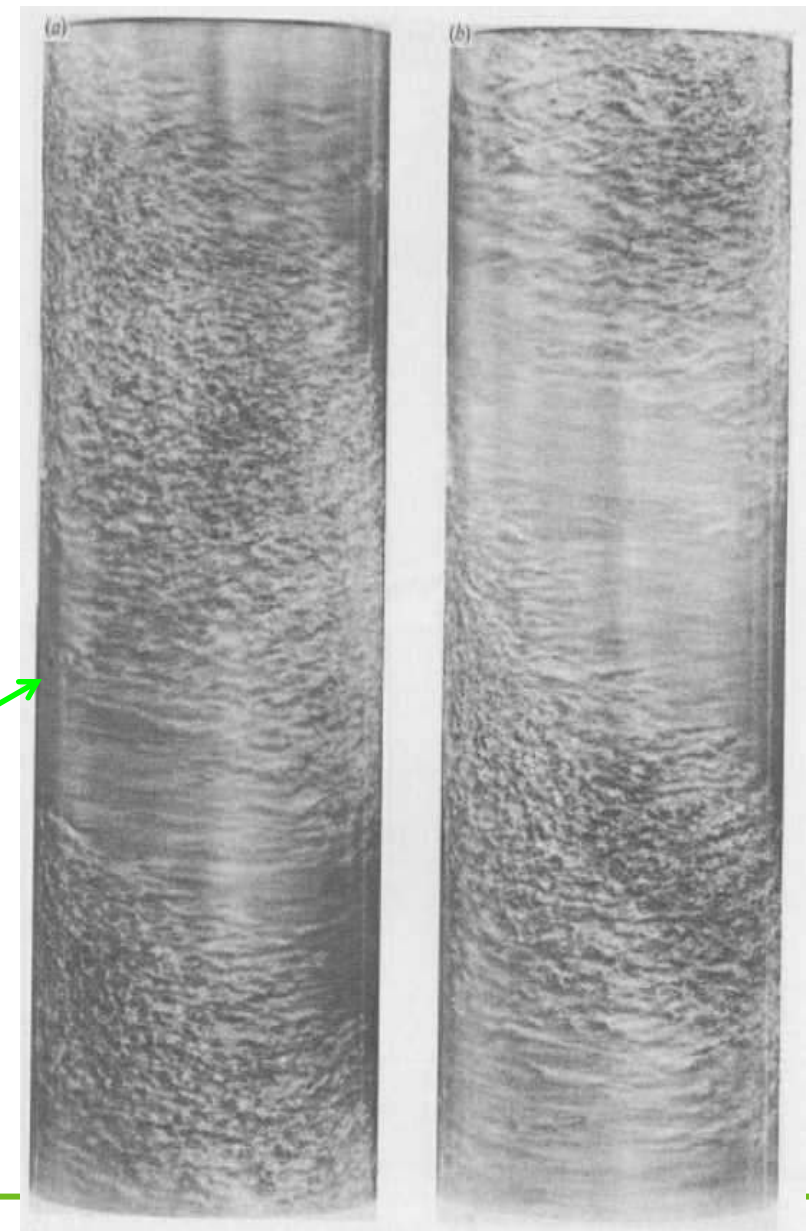
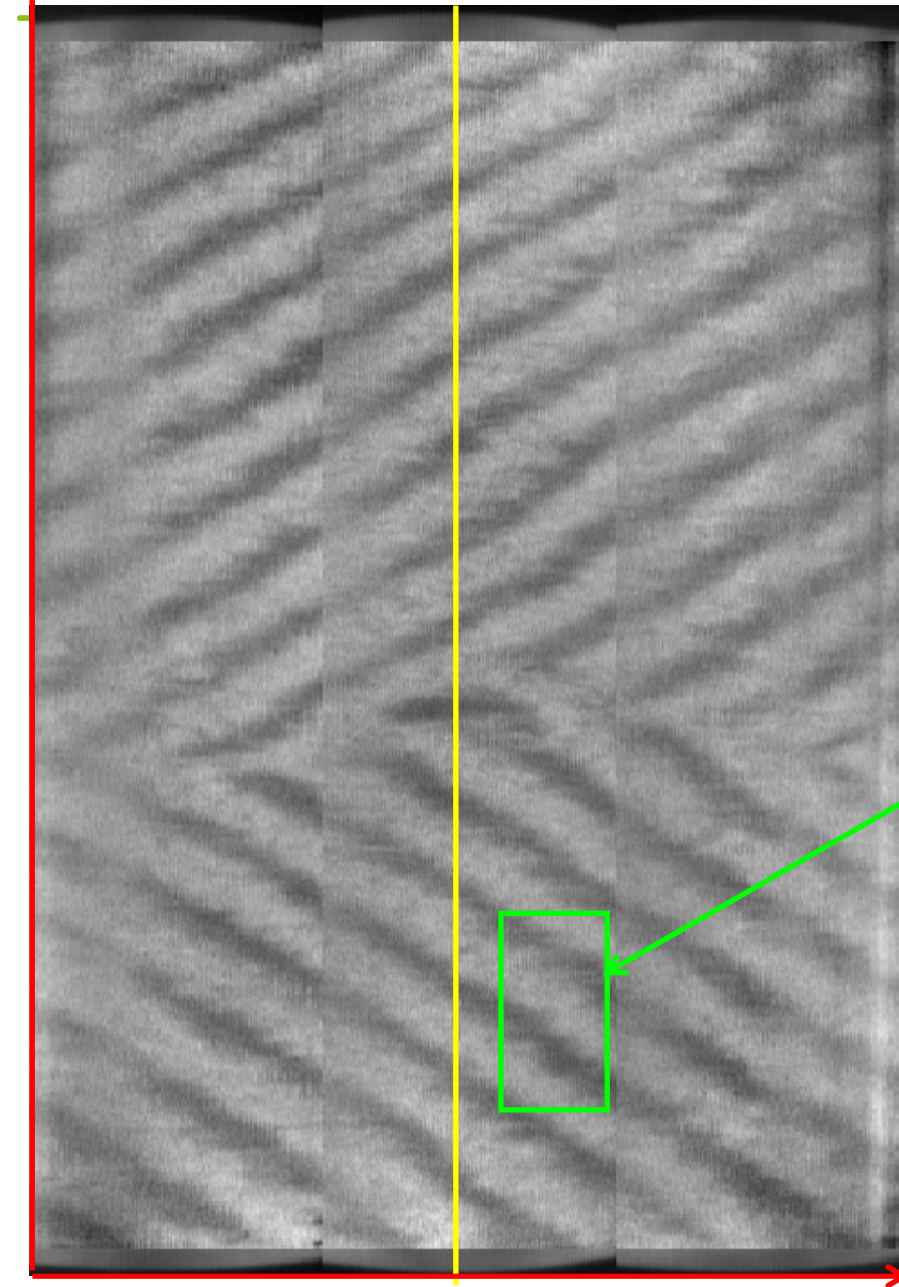
# Transition *from* turbulent to laminar flow in plane Couette flow



cea Transition *from* turbulent to laminar flow  
in Taylor Couette flow



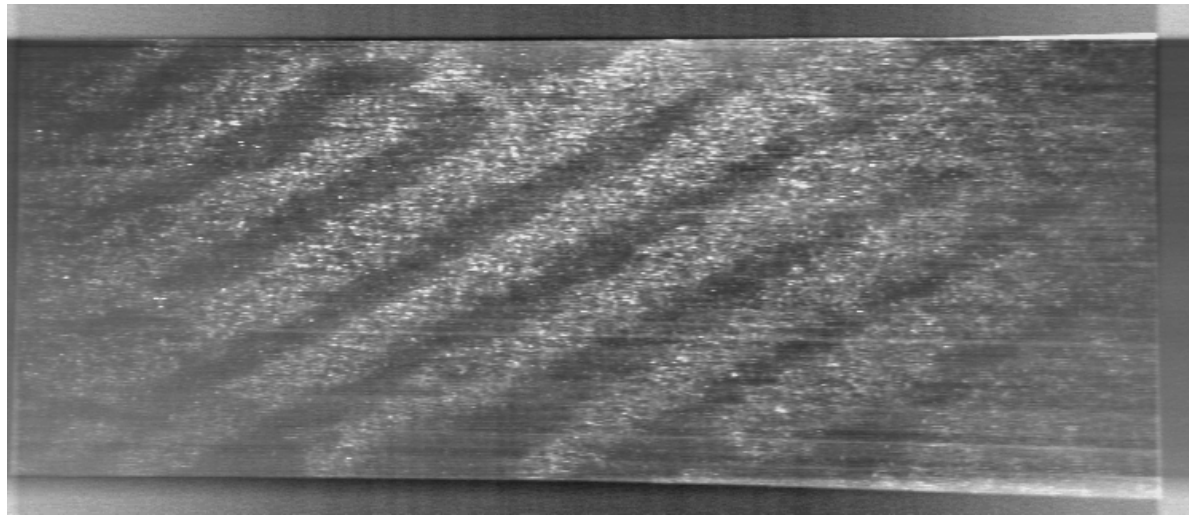
# Spiral Turbulence in extended geometry



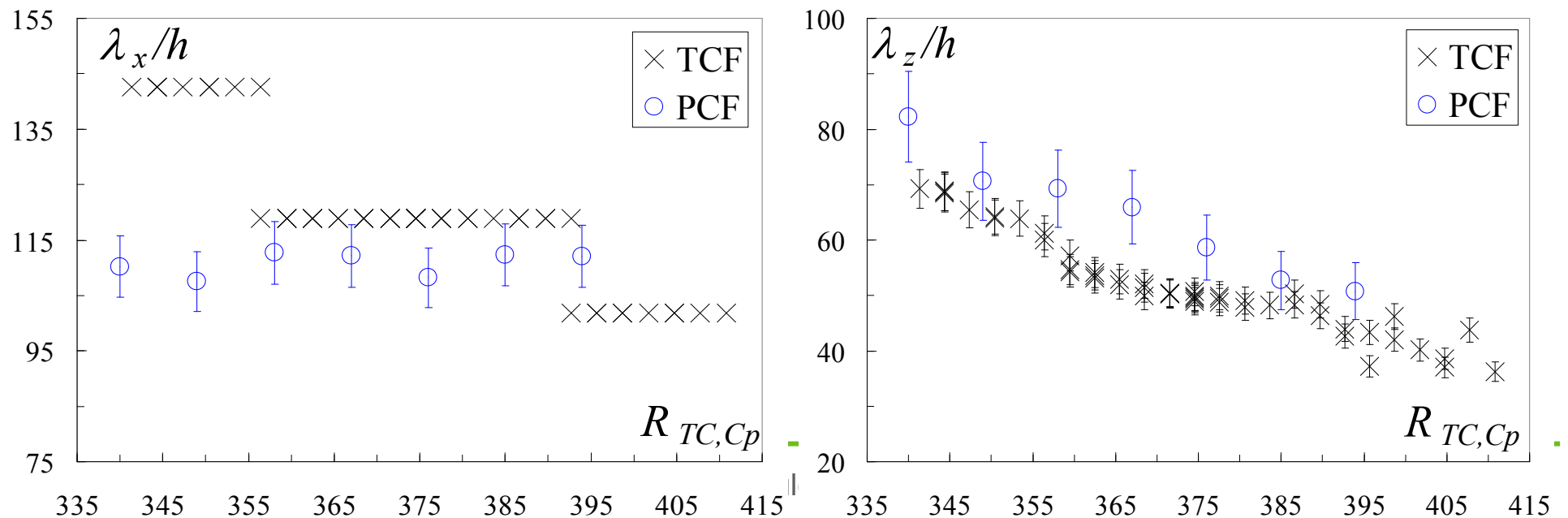
turbulence, Andereck, Liu, Swinney, *J. Fluid Mech* (1986)



# Turbulent stripes in plane Couette flow



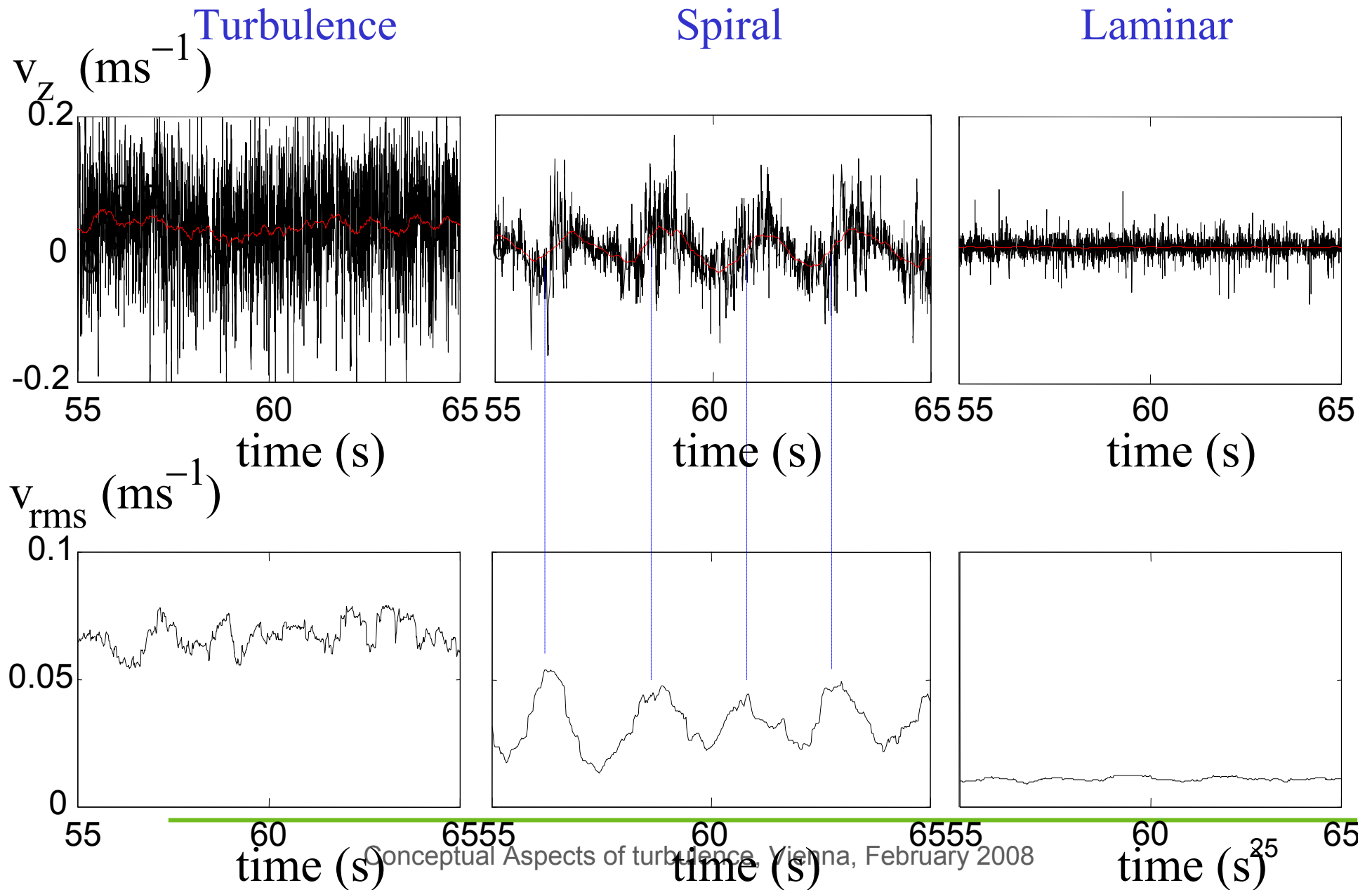
Comparison with Taylor-Couette flow when  $W_i = -W_o$





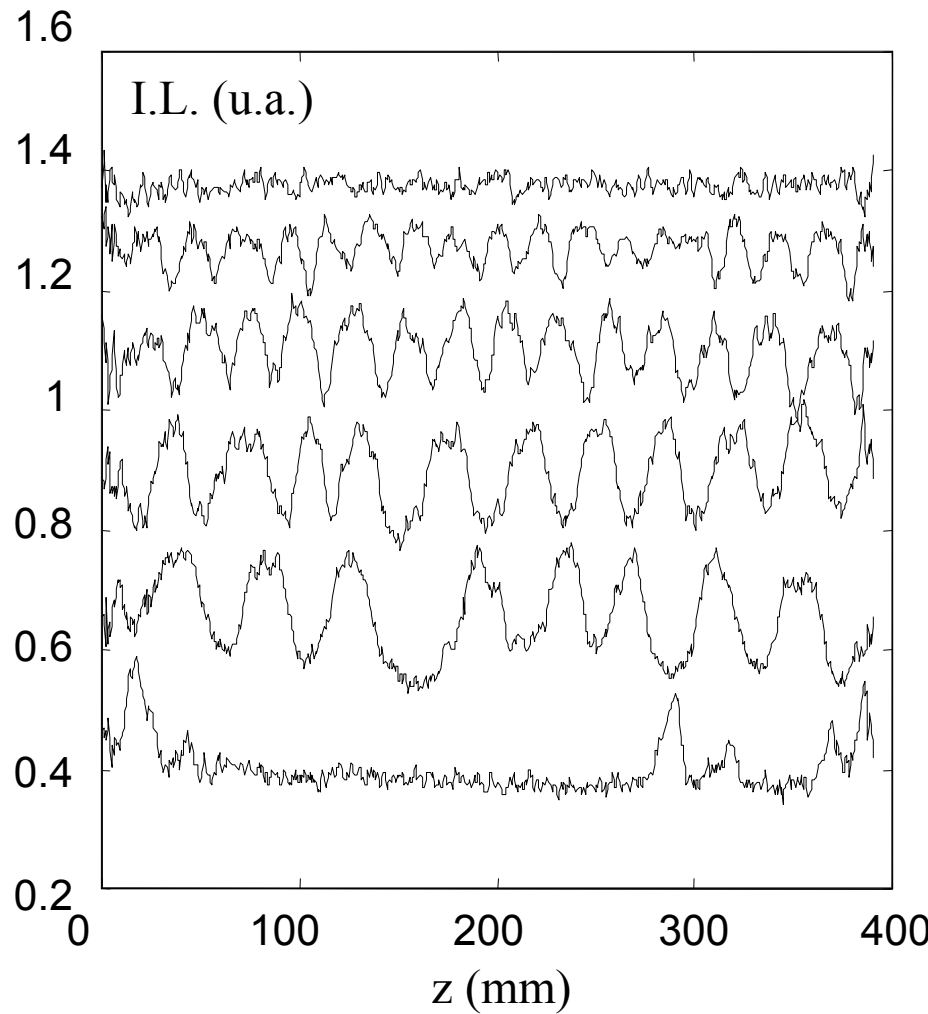


# TC flow: LDV measurements

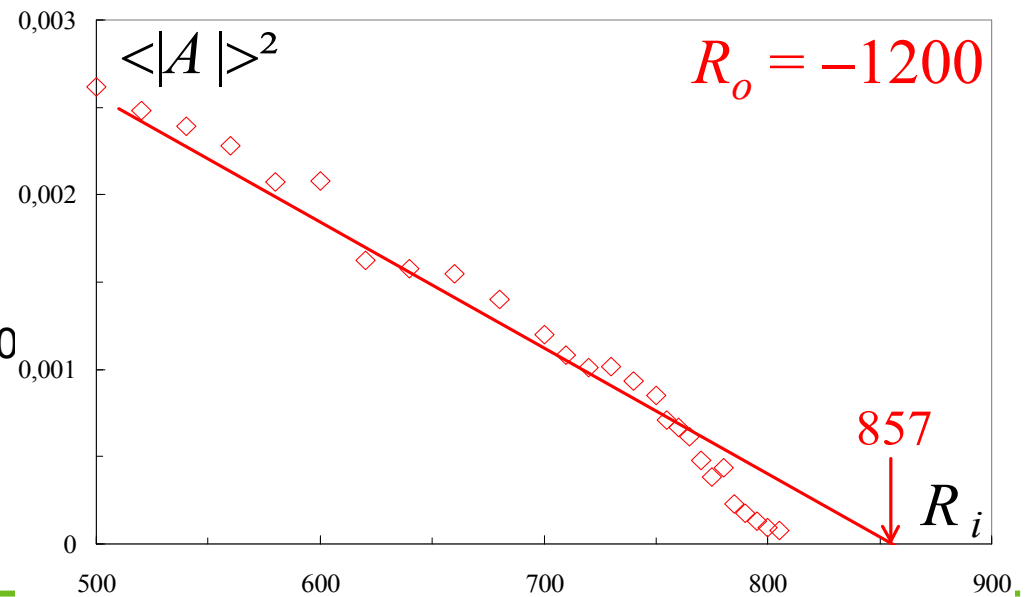
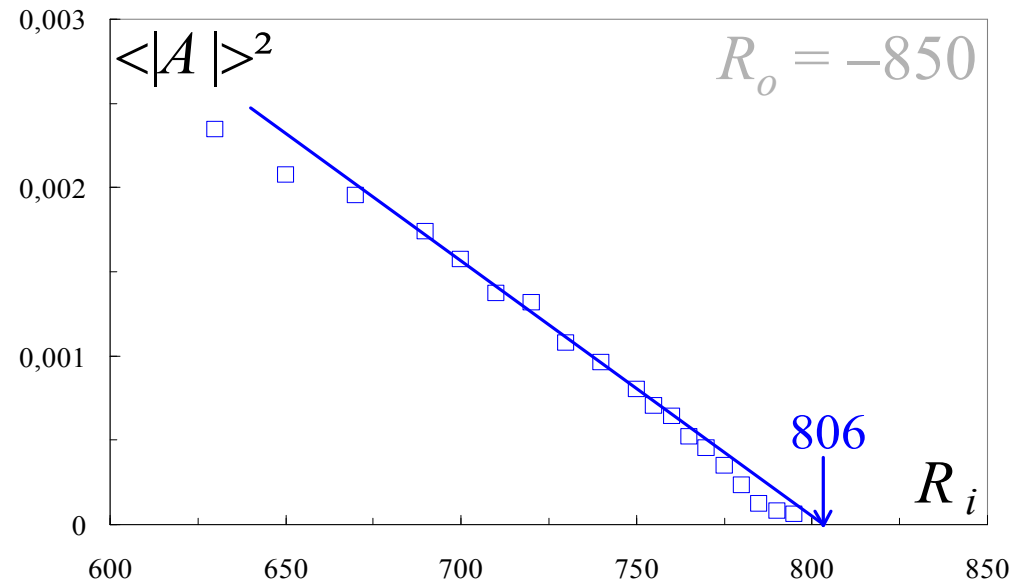




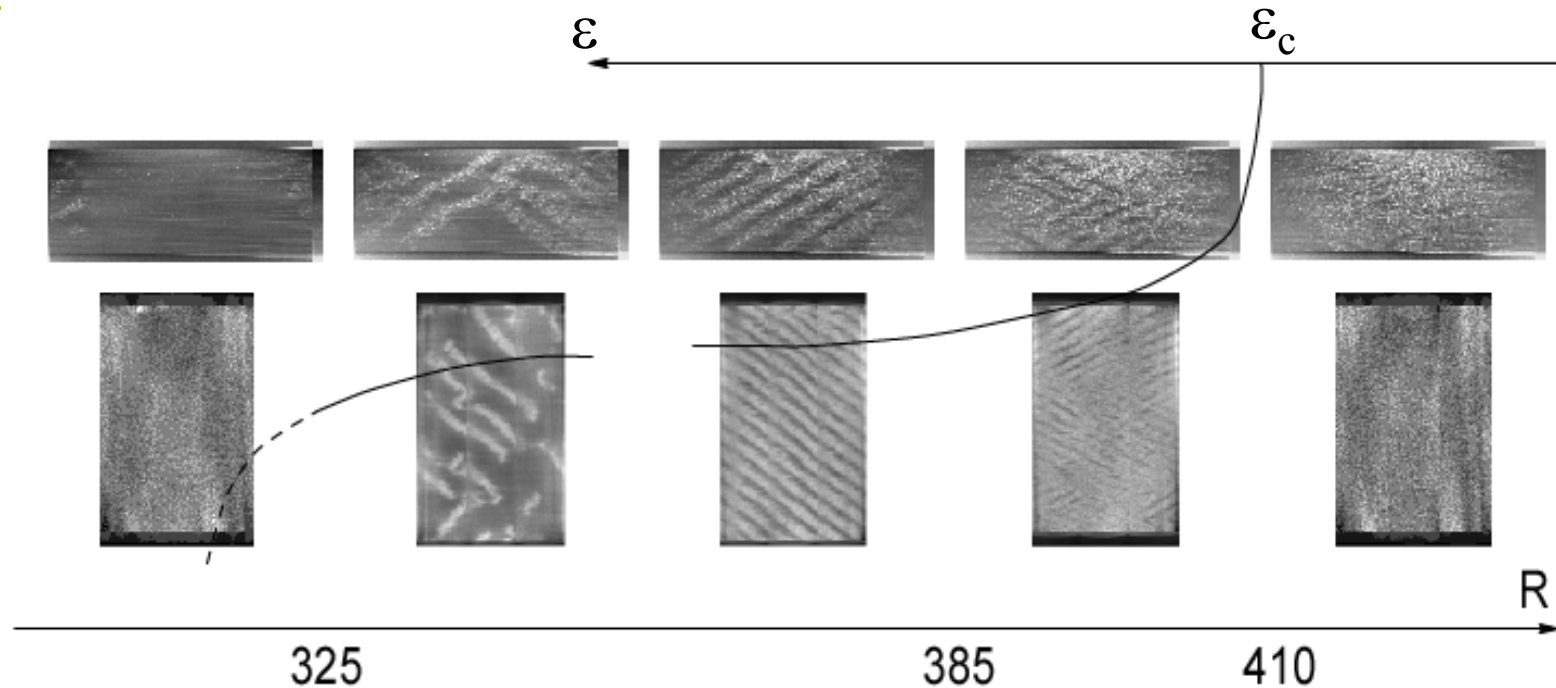
# From Turbulence to Spiral Turbulence



~ supercritical bifurcation



# Couette flows: summary



- A discontinuous transition **from laminar to turbulent flow** (unstable finite amplitude solutions)
- A continuous transition **from turbulent to laminar flow** (Ginzburg-Landau equations + noise)